## COURSE OBJECTIVES:

The main learning objective of this course is to prepare the students for:

1. Drawing engineering curves.
2. Drawing freehand sketch of simple objects.
3. Drawing orthographic projection of solids and section of solids.
4. Drawing development of solids
5. Drawing isometric and perspective projections of simple solids.

## CONCEPTS AND CONVENTIONS (Not for Examination)

Importance of graphics in engineering applications - Use of drafting instruments - BIS conventions and specifications - Size, layout and folding of drawing sheets - Lettering and dimensioning.

## UNIT I PLANE CURVES ANDFREEHAND SKETCHING 6+12

Basic Geometrical constructions, Curves used in engineering practices: Conics - Construction of ellipse, parabola and hyperbola by eccentricity method - Construction of cycloid - construction of involutes of square and circle - Drawing of tangents and normal to the above curves.

## UNIT II PROJECTION OF POINTS, LINES AND PLANE SURFACE $\mathbf{6 + 1 2}$

Orthographic projection- principles-Principal planes-First angle projection-projection of points. Projection of straight lines (only First angle projections) inclined to both the principal planes Determination of true lengths and true inclinations by rotating line method and traces. Projection of planes (polygonal and circular surfaces) inclined to both the principal planes by rotating object method.

## UNIT III PROJECTION OF SOLIDS 6+12

Projection of simple solids like prisms, pyramids, cylinder, cone and truncated solids when the axis is inclined to one of the principal planes and parallel to the other by rotating object method. Visualization concepts and Free Hand sketching: Visualization principles -Representation of Three Dimensional objects - Layout of views- Freehand sketching of multiple views from pictorial views of objects.
Practicing three dimensional modeling of simple objects by CAD Software(Not for examination)

## UNIT IV PROJECTION OF SECTIONED SOLIDS AND DEVELOPMENT OF SURFACES

Sectioning of above solids in simple vertical position when the cutting plane is inclined to the one of the principal planes and perpendicular to the other - obtaining true shape of section. Development of lateral surfaces of simple and sectioned solids - Prisms, pyramids cylinders and cones.
Practicing three dimensional modeling of simple objects by CAD Software(Not for examination)
UNIT V ISOMETRIC AND PERSPECTIVE PROJECTIONS $\mathbf{6 + 1 2}$
Principles of isometric projection - isometric scale -Isometric projections of simple solids and truncated solids - Prisms, pyramids, cylinders, cones- combination of two solid objects in simple vertical positions - Perspective projection of simple solids-Prisms, pyramids and cylinders by visual ray method.
Practicing three dimensional modeling of isometric projection of simple objects by CAD Software(Not for examination)

Publication of Bureau of Indian Standards:

1. IS 10711-2001: Technical products Documentation - Size and lay out of drawing sheets.
2. IS 9609 (Parts 0 \& 1) - 2001: Technical products Documentation -Lettering.
3. IS 10714 (Part 20) - 2001 \& SP 46 - 2003: Lines for technical drawings.
4. IS 11669-1986 \& SP 46 -2003: Dimensioning of Technical Drawings.
5. IS 15021 (Parts 1 to 4) - 2001: Technical drawings — Projection Methods.

## TEXT BOOKS:

Bhatt N.D. and Panchal V.M., "Engineering Drawing", Charotar Publishing House, $53^{\text {rd }}$ Edition, 2019 Natrajan K.V., "A Text Book of Engineering Graphics", Dhanalakshmi Publishers, Chennai, 2018. Parthasarathy, N. S. and Vela Murali, "Engineering Drawing", Oxford University Press, 2015
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2. Construct a Parabola when the distance of its focus from its directrix is equal to 50 mm . Also draw a tangent and a normal to the curve.


V - Vertex
F - Focus
AB - Directirix
TT - Tangent @ M
NN - Normal @ M
CVF - Axis

CF - 50mm(Given)
VF/ VC-1 (Given)
$V F=25 \mathrm{~mm}$
$\mathrm{VC}=25 \mathrm{~mm}$

SCALE: 1: 1
ALL DINENSIONS ARE IN MM
3. Construct a hyperbola, when the distance of its focus from its directrix is equal to 50 mm and eccentricity is $3 / 2$. Also draw a tangent and a normal to the curve.
HYPERBOLA

CF - 50mm(Given)
VF/ VC - 3/2 (Given)
$\mathrm{VF}=30 \mathrm{~mm}$
$V C=20 \mathrm{~mm}$
8. With $\mathrm{C} 1, \mathrm{C} 2, \mathrm{C} 3 \ldots$ etc as centers and radius equal to $\mathrm{R}(36 \mathrm{~mm})$, draw arcs cutting
6. Draw perpendiculars at $1^{\prime}, 2^{\prime}, 3^{\prime} \ldots$ etc upto the line CB and name it $\mathrm{C} 1, \mathrm{C} 2, \mathrm{C} 3 \ldots$ etc.
7. Draw horizontal lines parallel to PA at $1,2,3$, etc. 4. Divide the circle $\left(1,2,3\right.$ etc) and the tangent $\left(1^{\prime}, 2^{\prime}, 3^{\prime}\right.$ etc) into same no. of equal parts
5. Draw a line CB parallel and equal to $P A$ 3. Draw a line PA tangential to and equal to the circumference of the circle Steps for construction:
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9. Involutes of a Triangle, P EnggTree.gmexagon


INVOLUTES

1. Involute of a Triangle ( 21 mm side)
2. Involute of a Pentagon ( 17 mm side)


## Projection of Points

## Objectives

$>$ To draw the projections of a point in the four quadrants.
$>$ To identify the position of the point in different quadrants.

## Notation

To obtain the projections of points in space, standard notations are followed:

1. The actual points in space are denoted by capital letters $A, B, C, D$, etc.,
2. The front views are denoted by the corresponding lowercase letters with dashes like $a^{\prime}, b^{\prime}, c^{\prime}, d^{\prime}$, etc., and their top views are denoted by the corresponding lowercase letters like $a, b, c, d$, etc.
3. Projectors are always drawn as continuous thin lines using a 2 H pencil.
4. The visible points are drawn with a H pencil.
5. Lettering is always drawn with a HB pencil.

Quadrant system: The picture planes used for obtaining the orthographic projections are called the Principal planes of projection or reference planes or co- ordinate planes of projection.
VP: The plane in front of observer is the vertical plane. (VP) or it is also called a Frontal plane.
Front View (FV): The projection on the VP is called the Front View (FV) or Vertical Projection or front elevation or Elevation.
HP: The plane which is Horizontal and perpendicular to VP is Horizontal Plane.
Top View (TV): The projection on the HP is called the Top View (TV) or Horizontal Projection or Plan.
Note: The planes HP and VP are called Principal Planes.
Reference Line: The line of intersection of HP and VP is called reference line, which is denoted by $\mathrm{X}-\mathrm{Y}$.

## First quadrant

Second quadrant
Third quadrant --- Below HP and behind VP
Fourth quadrant
--- Above HP and in front of VP
--- Above HP and behind VP
--- Below HP and in front of VP

## ORIENTATION OF POINT IN SPACE

(1) In quadrant I (Above H.P \& In Front of V.P.)
(2) In quadrant II (Above H.P \& Behind V.P.)
(3) In quadrant III (Below H.P \& Behind V.P.)
(4) In quadrant IV (Below H.P \& In Front of V.P.)
(5) In Plane (Above H.P. \& In V.P.)
(6) In Plane (Below H.P. \& In V.P.)
(7) In Plane ( In H.P. \& In front of V.P.)
(8) In Plane ( In H.P. \& Behind V.P.)
(9) In Plane ( In H.P. \& V.P.)



POSITION: 3 (III Qua.)

## POINT -Below H.P. <br> $A_{3}$ Behind V.P.

## CONCLUSIONS:

| In 3D | In 2D |
| :---: | :---: |
| Point, Below <br> H.P. | F.V. <br> Below XY |
| Point Behind <br> V.P. | T.V. <br> Above XY |



## POSITION: 5




## POSITION: 7

POINT $/$ In H.P. In Front of V.P.

## $\mathrm{A}_{7}$ Point

$$
\mathbf{a}_{7}^{\prime}-\mathrm{F} . \mathrm{V} .
$$

$$
\mathbf{a}_{7}-\mathrm{T} \cdot \mathrm{~V}
$$



Projection of a Point in the I-Quadrant

Point A is $\mathbf{2 0 ~ m m}$ above the HP and $\mathbf{3 0 ~ m m}$ in front of the VP


1. Draw the reference line $X Y$ and name it as VP and HP respectively above and below the XY line.
2. Draw a line perpendicular to XY.
3. On the perpendicular line mark a point a 30 mm below XY . (Top view)
4. On the perpendicular line mark a point a' 20 mm above XY. (Front view)
5. Erase the unwanted lines.
6. The points a and a' are the projections of the point $A$ in the $I$-quadrant.

## Projection of a Point in the II-Quadrant

Point $B$ is 25 mm above the HP and 35mm behind the VP.


1. Draw the reference line $X Y$ and name it as VP and HP respectively above and below the XY line.
2. Draw a line perpendicular to $X Y$.
3. On the perpendicular line mark a point b 35 mm above XY .(Top view)
4. On the perpendicular line mark a point b' 25 mm above XY.(Front view)
5. Erase the unwanted lines.
6. The points $b^{\prime}$ and $b$ are the projections of the point $B$ in the II- quadrant.

## Projection of a Point in the III-Quadrant

Point C 35 mm below the HP and 25 behind the VP.


1. Draw the reference line $X Y$ and name it as VP and HP respectively above and below the XY line.
2. Draw a line perpendicular to $X Y$.
3. On the perpendicular line mark a point 'c' 25 mm above XY . (Top view)
4. On the perpendicular line mark a point 'c' 35 mm below XY. .(Front view)
5. Erase the unwanted lines.
6. The points $c$ and $c^{\prime}$ are the projections of the point $C$ in the III- quadrant.

## Projection of a Point in the IV-Quadrant

Point D 30mm below the HP and 40 mm in front of the VP.


1. Draw the reference line $X Y$ and name it as VP and HP respectively above and below the XY line.
2. Draw a line perpendicular to $X Y$.
3. On the perpendicular line mark a point 'd' 40 mm below XY.(Top view)
4. On the perpendicular line mark a point ' $d$ ' 30 mm below XY.(Front view)
5. Erase the unwanted lines.
6. The points $d$ and d' are the projections of the point $D$ in the IV- Quadrant.

## Additional problems

1. Draw and state the quadrants in which the following points are located. Assume any distances.
2. A - front view below $X Y$ line and Top view above $X Y$ line
3. B - Front and Top views below $X Y$ line.
4. C - Front and Top views are above XY line.
5. D - Front view above XY line and Top view below XY line.

Solution: A lies in 3rd Quadrant C lies in 2nd Quadrant

$B$ lies in 4th Quadrant D lies in 1st Quadrant

2. Draw the projections of the following points on the same $X Y$ line, keeping convenient distance between each projector. Name the quadrants in which they lie.

1. E-30 mm below HP and 25 mm behind VP.
2. F-35 mm below HP and 30 mm in front of VP.
3. G-On HP and 30 mm in front of VP.
4. H-On HP and 35 mm behind VP.


E-3rd ${ }^{\text {rd }}$ Quadrant $\quad$ F-4 ${ }^{\text {th }}$ Quadrant $\quad$ G-4 ${ }^{\text {th }}$ Quadrant $\quad$ H-3 ${ }^{\text {rd }}$ Quadrant
3. Draw the projections of the following points on the same XY line, keeping convenient distance between each projectors. Name the quadrant in which they lie.

1. $\mathrm{M}-30 \mathrm{~mm}$ below HP and 25 mm behind VP.
2. N-35 mm below HP and 30 mm infront of VP.
3. P - on HP and 30 mm infront of VP.
4.Q - on HP and 35 mm behind VP.

## Solution:

M - 3rd Quadrant
P-1st as well as 4th Quadrant

N - 4th Quadrant
Q-2nd as well as 3rd Quadrant

4. Draw the projections of the following points on the same XY line, keeping convenient distance between each projectors. Name the quadrants in which they lie.

1. A -30 mm above HP and 35 mm in front of VP.
2. B-35 mm above HP and 40 mm behind VP. 3.C - 40 mm above HP and on VP.
3. D - 35 mm below HP and 30 mm in front of VP.

## Solution:

A - 1st Quadrant
B - 2nd Quadrant
C- 1st as well as 2nd Quadrant
D - 4th Quadrant

5. Draw the projections of the following points on the same XY line, keeping convenient distance between each projectors. Name the quadrants in which they lie.

1. P-20 mm above HP and 35 mm infront of VP.
2. Q-30 mm above HP and 40 mm behind VP.
3. R-40 mm above HP and on VP.
4. $\mathrm{S}-35 \mathrm{~mm}$ below HP and 30 mm infront of VP.

Solution: $\quad \mathrm{P}=1$ st Quadrant
R-1st as well as 2nd Quadrant

6. Draw the projections of the following points on the same XY line, keeping convenient distance between each projectors. Also state the quadrants in which they lie.

1. P-25 mm above HP and 35 mm infront of VP.
2. Q-30 mm above HP and 40 mm behind VP.
3. R-40 mm above HP and on VP.
4. S- 35 mm below HP and 30 mm in front of VP.

Solution: P-1st Quadrant
Q-2nd Quadrant
R-1st as well as 2nd Quad. S - 4th Quadrant

7. Draw the projections of the following points on the same XY line, keeping convenient distance between each projectors and state the quadrants in which they lie.

1. P-10 mm above HP and 15 mm infront of VP.
2. Q -15 mm above HP and 25 mm behind VP.
3. R-25 mm below HP and in VP. $4 . \mathrm{S}-40 \mathrm{~mm}$ above HP and in VP.

## Solution:

P-1st Quadrant
Q-2nd Quadrant

R-3rd as well as 4th Quadrant $\quad$ S-1st as well as 2nd Quadrant

8. A point 30 mm above $X Y$ line is the front view of two points $A$ and $B$. The top view of $A$ is 40 mm behind VP and the top view of $B$ is 45 mm in front of VP. Draw the projections of the points and state the quadrants in which the points are situated.
SOLUTION: A - 2nd Quadrant $\quad B=1$ st Quadrant

9. A point 30 mm above $X Y$ line is the front view of 3 points $P, Q$ and $R$. The top view of $R$ is 40 mm behind VP, the top view $Q$ is on $X Y$ line and top view of point $P$ is 45 mm in front of VP. Draw the projections of the points and state the quadrants in which the points are situated.

## SOLUTION:

P-1st Quadrant
R-2nd Quadrant $\quad$ Q-1st as well as 2nd Quadrant

10. A point $A$ is 20 mm above HP and 25 mm in front of VP. Another point $B$ is $\mathbf{2 5}$ mm behind VP and 40 mm below HP. Draw their projections when the distance between their projectors parallel to XY line is zero mm . Add the right side view only to point $B$.

## SOLUTION:


11. A point $P$ is 15 mm above HP and 25 mm in front of VP. Another point $Q$ is $\mathbf{2 5}$ mm behind VP and 40 mm below HP. Draw their projections when the distance between their projectors parallel to XY line is zero mm. Add the right side view only to point Q .

## SOLUTION:


12. The common point 40 mm below $X Y$ line represents not only the front views of three points $A, B$ and $C$ but also the top view of point $C$. The top view of point $B$ is lies on $X Y$ line and top view of point $A$ lies 50 mm above it. Draw the projections of the points and add the right side view to the point A only. Also state in which the quadrants the points lie.

## Solution:

A - 3rd Quadrant
B - 3rd as well as 4th Quadrant
C - 4th Quadrant

13. A point $P$ is on HP and 35 mm in front of VP. Another point $Q$ is on VP and below HP. The line joining their front views makes an angle of 30 deg. to $X Y$ line, while the line joining their top views makes an angle of 45 deg. with XY line. Find the distance of the point Q from HP.

## Solution:

$$
\mathrm{L}=20.21 \mathrm{~mm}
$$

Q is 20.21 mm below HP

14. A point $R$ is 25 mm above HP and 20 mm in front of VP. Another point $S$ is on HP and 30 mm behind VP. The distance between their projectors measured parallel to the line of intersection VP and HP is 50 mm . Find the distance between top views of points $R$ and $S$.

## Solution:

The distance between top views of points $R$ and $S$ is 70.71 mm

15. A point $M$ is on HP and 30 mm in front of VP. Another point N is 20 mm below HP and 20 mm in front of VP. The distance between their projectors measured parallel to XY line is 50 mm . Find the distance between front views of the point M and N .

## Solution:

The distance between front views of M and N are 53.85 mm

16. A point $P$ is on HP and 30 mm in front of VP. Another point $Q$ is on VP and 40 mm above HP. The distance between their projectors parallel to XY line is 50 mm . Find the distance between their front and top views of the points P and Q .

## Solution:

Distance between their front views of $P$ and $Q$ is 64.03 mm
Distance between their top views of $P$ and $Q$ is 58.31 mm

17. Two points $R$ and $S$ are on HP. The point $R$ is 35 mm in front of VP, while $S$ is 50 mm behind VP. The line joining their top views makes an angle of 40 deg . with XY. Find the horizontal distance between the two projectors.

## Solution:

ANSWER: $\mathrm{D}=101.3 \mathrm{~mm}$

18. Two points $P$ and $Q$ are on HP. The point $P$ is 30 mm behind $V P$, while $Q$ is 50 mm in front of VP. The line joining their top views makes an angle of 40 deg . with XY. Find the horizontal distance between their projectors parallel to XY line.

## Solution:

## ANSWER: D = 95.3 mm


19. A point $M$ is 30 mm in front of VP and 20 mm above HP, another point N is 15 mm behind VP and 25 mm below HP. The horizontal distance between the points parallel to XY line is 50 mm . Draw the projections of the points $\mathbf{M}$ and $\mathbf{N}$ and join their front and top views. Draw the right side view for the point N only.

## Solution:



## Projections of a Straight Line

## Introduction

The shortest distance between any two points is called a "straight line". Different surfaces and planes form the configuration or shape of any object. Revolving or moving straight lines in different ways obtains these surfaces and planes.

Thus a straight line is the basic conceptual figure using which any object like a machine component or a structural element is represented. Thus projection of a straight line is the foundation of Engineering Drawing.

We have studied the projections of given points, Joining the respective projections of two points therefore gives the projection of the straight line joining the two points. As per ISO convention the first angle of projection is used.

## Objectives

$>$ Define straight line.
> Draw the projections of a straight line located at different positions with respect to the VP and the HP.


## ORIENTATION OF LINE IN SPACE

The position of straight line in space can be described following

1. Lines parallel to VP and perpendicular to HP
2. Lines perpendicular to VP and parallel to HP
3. Lines parallel to both VP and HP
4. Lines parallel to VP and inclined to HP
5. Lines inclined to VP and parallel to HP
6. Lines inclined to both VP and HP

## Perpendicular to the HP and Parallel to the VP



A Line $A B 25 \mathrm{~mm}$ is parallel to the VP and perpendicular to the HP
20 mm in front of the and 10 mm above the HP

1. Draw the line $X Y$.
2. Draw a line perpendicular to $X Y$ using a 2 H pencil.
3. Mark b' 10 mm above XY on the perpendicular line.
4. Mark a' 25 mm above $\mathrm{b}^{\prime}$.
5. $a^{\prime} b^{\prime}$ is the front view, join $a^{\prime}, b^{\prime}$ using a $H$ pencil.
6. Mark a (b) 20 mm below $X Y$; a (b) is the top View.
7. Erase the unwanted Lines.


## Perpendicular to the VP and Parallel to the HP



A Line AB of length 25 mm is perpendicular to the VP and Parallel to the HP. The point $A$ is 20 mm above the HP and 10 mm in front of the VP.

1. Draw the line $X Y$.
2. Draw a line perpendicular to $X Y$ using a $2 H$ pencil.
3. Mark "a" 10 mm below XY on the Perpendicular line.
4. Mark "b" 25 mm below "a".
5. Join "a" and "b" using an H pencil to get the top view.
6. Mark $a^{\prime}\left(b^{\prime}\right) 20 \mathrm{~mm}$ above XY line on the Perpendicular line
7. Erase the unwanted Lines


## Parallel to the HP and Inclined to the VP



A line $P Q$ of length 40 mm is parallel to the $H P$ and inclined at an angle of $35^{\circ}$ to the $V P$.
The end $P$ is 20 mm above the HP and 15 mm in front of the VP.

1. Draw the line XY.
2. Draw a line perpendicular to XY using a 2 H pencil
3. Mark " p "' and " p " respectively 15 mm above XY and 20 mm below XY on the perpendicular line
4. From "p" draw a line at an angle of $35^{\circ}$ to $X Y$ and mark " $q$ " such that $p q=40 \mathrm{~mm}$ true length.
5. pq is the top view of the given line in the I-Quadrant.
6. From " q " draw a projector (perpendicular line) to intersect the horizontal line drawn from " $p^{\prime}$ " at " $q$ ' ".
7. $\mathrm{p}^{\prime} \mathrm{q}$ ' is the front view.
8. Erase the unwanted line.


## Parallel to the VP and Inclined to the HP



Orthographic Projections


A line PQ of length 40 mm is parallel to the VP and inclined at an angle of $30^{\circ}$ to the HP .
The end $P$ is 15 mm above the HP and 20 mm in front of the VP.

1. Draw the line $X Y$.
2. Draw a perpendicular line to $X Y$ using $2 H$ pencil.
3. Mark $p^{\prime} \& p 15 \mathrm{~mm}$ above XY \& 20 mm below XY on the perpendicular line.
4. From $p^{\prime}$ draw a line at angle of $30^{\circ}$ to XY and mark $q^{\prime}$. such that
$p^{\prime} q^{\prime}=40 \mathrm{~mm}=$ True length
5. $\mathrm{p}^{\prime} \mathrm{q}$ ' is the required Front View
6. From q' draw a projector (perpendicular line) to intersect the horizontal line draw from $p$ at $q$.
7. $p q$ is the required Top View
8. Erase the unwanted Line.


## Parallel to the HP and the VP



A Line CD 30 mm long is parallel to both planes. The line is 40 mm above the HP and 25 mm in front of the VP.

1. Draw the line $X Y$.
2. Draw a line perpendicular to XY using a 2 H pencil.
3. Draw another perpendicular line 30 mm from the previous line.
4. Mark "c'" and "d' " on the Perpendicular lines and join them to get the front view.
5. Mark "c" 25 mm below line XY; join "c" and "d" to get the top view.
6. Erase the unwanted Lines.


## Inclined to the HP and the VP




The line pq is inclined to both the VP and the HP.
A line PQ of length 80 mm . is inclined at an angle of $45^{\circ}$ to the VP and inclined at an angle of $30^{\circ}$ to the HP. The end P is 20 mm above the HP and 30 mm in front of the VP.

1. Draw the line $X Y$.
2. Mark " $p$ " below $X Y$ line and draw $45^{\circ}$ line and mark $q_{2}$ at 80 mm
3. Mark " $p$ '" above XY line and draw $30^{\circ}$ line and mark " $q_{1}$ " " at 80 mm
4. Draw locus of " $q_{1}$ " " and " $q_{2}$ "
5. Project from " $q_{1}$ " " and " $p$ " as centre rotate, it cuts locus of " $q_{2}$ " at " $q$ "
6. Joint " $p$ " and " $q$ " to get top view
7. Project from " $q_{2}$ " and " $p$ ' " as centre rotate, it cuts locus of " $q_{1}$ " at " $q^{\prime}$ "
8. Joint "p'" and "q'" to get front view

Finding true length of a line and its inclination with HP and VP
True length and inclination is determine from the final top and front view of the straight line by following two methods

1. Rotating method
2. Rotating trapezoidal plan method

Projection of straight line on its various positions

| S.No | Position of the line | Front view | Top view | Traces |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Lines parallel to both VP and HP | True length and is parallel to $X Y$ | True length and is parallel to $X Y$ | NO TRACES |
| 2 | Lines perpendicular to VP and parallel to HP | Point | True length and is Perpendicular to XY | Only VT <br> No HT |
| 3 | Lines parallel to VP and perpendicular to HP | True length and is Perpendicular to XY | Point | Only HT <br> No VT |
| 4 | Lines parallel to HP and inclined to VP | Shorter than true length and is parallel to XY | Has true length and true inclination | Only VT <br> No HT |
| 5 | Lines inclined to HP and parallel to VP | Has true length and true inclination | Shorter than true length and is parallel to XY | Only HT <br> No VT |
| 6 | Lines inclined to both VP and HP | Shorter than true length, inclined to XY and angle is not true inclination | Shorter than true length, inclined to $X Y$ and angle is not true inclination | Has Both HT and VT |

## Problems- Projection of Lines

## Lines parallel to both VP and HP

1.A line CD 50 mm long has its end $\mathrm{C}, 15 \mathrm{~mm}$ above the HP and 25 mm in front of the VP.The line is kept parallel to both HP and VP .draw its projections


## Lines perpendicular to one plane and parallel to another plane

2.A line 55 mm long has its end $E 15 \mathrm{~mm}$ above the HP and 25 mm in front of the VP. The line is kept perpendicular to HP and parallel to VP. Draw its projections.

3. A line GH 50 mm long has its end G 20 mm above the HP and 25 mm in front of the VP. The line is kept perpendicular to VP and parallel to HP. Draw its projections.


## Lines inclined to one plane and parallel to another plane

4. A line AB 55 mm long is lying on the HP and makes an angle of $35^{\circ}$ with the VP. Its end $A$ is 25 mm in front of VP. Draw the projections of the line.

5. A line $A B 50 \mathrm{~mm}$ long has its end $A 30 \mathrm{~mm}$ above HP and 25 mm in front of VP. The line is kept inclined at $40^{\circ}$ to HP and parallel to VP. Draw its projections and make its traces.

6. A line AB 50 mm long has its end $\mathbf{A} 25 \mathrm{~mm}$ above HP and 25 mm in front of VP. The line is inclined at $45^{\circ}$ to VP and parallel to HP. Draw its projections and also make its traces.

7. A line AB 65 mm long has its end A 20 mm above HP and 30 mm in front of VP. Its top view has a length of 45 mm and parallels to HP. Draw its projections and find the inclination of the line with HP.

8. A line AB 60 mm long has its end A 30 mm above HP and 15 mm in front of VP. Its front view has a length of 45 mm and parallels to HP. Draw its projections and find the inclination of the line with VP.


Answer: $\theta=46^{\circ}$
10. A line AB has its end A 30 mm above HP and 20 mm in front of VP. It is inclined at $25^{\circ}$ to the VP and parallels to HP. Draw its projections, if the distance between the end projectors to be 55 mm . Find the true length of the line also.


Answer: TL=60mm

## Lines inclined to one plane and parallel to another plane

11. A line 70 mm long has one end 15 mm above HP and 30 mm in front of VP. The line is inclined at $35^{\circ}$ to the HP $45^{\circ}$ to the VP. Draw the projection of the line.

12. One end of a line $A B 70 \mathrm{~mm}$ long, is 10 mm above HP and 25 mm in front of VP. The line is inclined at $25^{\circ}$ to the HP $45^{\circ}$ to the VP. Draw the projections and find its traces.

13. A line AB 75 mm long has one end $A 20 \mathrm{~mm}$ above HP and 25 mm in front of VP. The end $B$ is 50 mm above the HP and 60 mm infront of VP. Draw the projection of the line and find its inclination with HP and VP.


Answer: $\quad \theta=24^{0} \phi=28^{0}$
14. One end of a line $A B$ is 10 mm above HP and 20 mm in front of VP. The other end is 45 mm above HP and 65 mm in front of VP the distance between the end projector is 40 mm . Draw the projection of the line and find its inclination and length.


Answer: $\theta=30^{\circ} \phi=40^{\circ} \mathrm{TL}=70 \mathrm{~mm}$
15. A line AB 65 mm long in the front view has its end $A 20 \mathrm{~mm}$ above HP and 15 mm in front of VP. The end $B$ is 45 mm in front of VP. Draw the projection of the line and find its inclination with HP and VP. The distance between the ends projectors passing through the end point is 50 mm . Draw the projection of the line and find its inclination.
Answer: $\theta=35^{\circ}$

$$
\phi=25^{0} \mathrm{TL}=71 \mathrm{~mm}
$$


16. A line $A B 80 \mathrm{~mm}$ long has its end $A 10 \mathrm{~mm}$ above HP and in the VP. Draw the projection of the line makes an angle of inclined at $50^{\circ}$ to the HP and $30^{\circ}$ to the VP.

17. One end $A$ of a line $A B$ is 60 mm long 30 mm above HP and 25 mm in front of VP. The top and front view has a length of 35 mm and 55 mm respectively. Draw the projection of the line and find its inclination.
Answer: $\theta=55^{0} \quad \phi=25^{\circ}$

18. A line $A B 75$ mm long has one of its ends 60 mm in front of the VP and $\mathbf{2 0} \mathbf{~ m m}$ above the HP and the other end is 20 mm in front of VP and is above HP. The top view of the line is 55 mm long. Draw the projection.

19. The top view of a line is 65 mm long and is inclined at $30^{\circ}$ to the reference line. One end is 20 mm above the HP and 10 mm in front of VP. The other end is 60 mm above the HP and is front view of VP. Draw the projection of the line and find its inclination and length.


Answer: $\theta=32{ }^{\circ} \phi=25^{\circ} \mathrm{TL}=76 \mathrm{~mm}$
20. One end $A$ of a line $A B$ is 70 mm long 15 mm above HP and 20 mm in front of VP. The top and front view has a length of 35 mm and 55 mm respectively. Draw the projection of the line and find its inclination.


Answer: $\theta=21^{\circ} \quad \phi=41^{\circ}$
21. One end $A$ of a line $A B$ is 70 mm long 20 mm above HP and 25 mm in front of VP. The line inclined at $50^{\circ}$ to the HP and $30^{\circ}$ to the VP. Draw the projection of the line and mark the point O on it, which is 35 mm away from one end of the line.

22.A line $A B 60 \mathrm{~mm}$ long has one of its ends 10 mm in front of the VP and $\mathbf{2 0} \mathbf{~ m m}$ above the HP. The line inclined at $40^{\circ}$ to the HP and $50^{\circ}$ to the VP. Draw the projection.

23. A straight line $A B$ has one of its ends 25 mm in front of the VP and 20 mm above the HP and the other end is 60 mm above HP and is in front of VP. The ends of the lines are on the same projector. Draw the projection and find the true length, inclinations Answer: $\theta=45^{\circ} \phi=45^{\circ} \mathrm{TL}=57 \mathrm{~mm}$

24.A line measuring 65 mm long has one of its ends 45 mm in front of the VP and 20 mm above the HP.the top view of the line is 45 mm long. The other end is above HP and is 20 mm in front of VP. The ends of the lines are on the same projector. Draw the projection and find the true length, inclinations

Answer: $\theta=46^{\circ} \phi=23^{\circ}$

25. The front view of line $A B$ measures 60 mm and make an angle of $45^{\circ}$ with $X Y$ line. The end $A$ is in HP. The vertical trace of the line is 10 mm below XY. The top view is inclined $30^{\circ}$ to $X Y$. Draw the projections, locate its traces.
Answer: $\theta=41^{\circ} \phi=26{ }^{\circ}$


## Midpoints Problems

26. The midpoint of line $A B 70 \mathrm{~mm}$ long, is 25 mm above the HP and 40 mm in front ofVP. It's inclined at $35^{\circ}$ to HP and $45^{\circ}$ to the VP. Draw its projections

27. The projection of line measuring 80 mm in the top view and 70 mm in the front view the midpoint of the line is 45 mm , in front of the VP and 35 mm above HP .One end is 10 mm in front of VP and nearer to it. The other end is nearer to HP. Draw the projection and find the true length, inclinations

28.A straight line $A B$ has one of its end $A, 10 \mathrm{~mm}$ in front of the VP and nearer to it. the midpoint m of the line is 50 mm , in front of the VP and 40 mm above the HP.the front and top view measures 90 mm and 120 mm respectively. Draw the projection and find the true length, inclinations

b $\mathrm{b}_{2}$

## PROJECTIONOFPLANES

A plane is a two dimensional object having length and breadth only.Its thickness is always neglected .Various shapes of plane figures are considered such as square, rectangle, circle, pentagon, hexagon, etc.

## TYPES OF PLANE FIGURES



RECTANGLE


TYPES OF PLANES

## PERPENDICULAR PLANES

Planes which are perpendicular to one of the principal planes of projection and inclined or parallel to the other

## OBLIQUE PLANES

Planes inclined to both the reference planes
TRACE OF PLANE

## HORIZONTAL TRACE

The Intersection line of the plane surface with H.P VERTICAL TRACE
The Intersection line of the plane surface with V.P ORIENTATION OF PLANES IN SPACE
The position of Planes in space can be described following

1. Planes Parallel to VP and Perpendicular to HP
2. Planes Perpendicular to VP and Parallel to HP
3. Planes Parallel to both VP and HP OR both Perpendicular VP and HP
4. Planes Perpendicular to VP and Inclined to HP
5. Planes Inclined to VP and Perpendicular to HP
6. Planes Inclined to both VP and HP
7. PLANE SURFACE PARALLEL TO VP AND PERPENDICULAR TO HP

8. PLANE SURFACE PARALLEL TO HP AND PERPENDICULAR TO VP

9. Planes parallel to both VP and HP / Both Perpendicular VP and HP



## 4. Planes Perpendicular to VP and inclined to HP


5. Planes Inclined to VP and Perpendicular to HP

6. Planes Inclined to both VP and HP


## PROBLEMS IN PROJECTION OF PLANES

1. Rectangle 30 mm and 50 mm sides is resting on HP on one small side which is $30^{\circ}$ Inclined to VP, While the surface of the plane makes $45^{\circ}$ inclination with HP. Draw it's projections.

2. A regular pentagon of 30 mm sides is resting on HP on one of its sides with its surface $45^{\circ}$ inclined to HP. Draw its projections when the side in HP makes $30^{\circ}$ angle with VP.

3. A circle of 50 mm diameter is resting on Hp on end A of its diameter AC which is $30^{\circ}$ inclined to Hp while it's TV is $45^{\circ}$ inclined to VP. Draw its projections.

4. A rectangle ABCD of size40x25 has the corner A, 10mm above HP and 15 mm in front of VP. All the sides of the rectangle are equally inclined to HP and parallel to VP. Draw the projection of lamina.

5. A rectangular lamina $A B C D$ is perpendicular to VP and inclined at $45^{\circ}$ to the HP. Draw its projections and obtains the traces.

(1)
6. A circle of 50 mm diameter inclined at $30^{\circ}$ to the HP and perpendicular to VP has its centre 30 mm in front of VP. Draw its front, top and side views.

7. A regular hexagon of 25 mm side has its one edge on HP. The surface of the lamina is perpendicular to VP and inclined at $40^{\circ}$ to HP. Draw the three views of the plane and locates the traces.

8. A hexagonal plate of 30 mm side has a corner at 20 mm from VP and 50 mm from HP. Its surface is inclined at $45^{\circ}$ to the VP perpendicular to HP. Draw the projections of the plate.

9. A circular lamina of diameter 50 mm lies in a plane inclined at $40^{\circ}$ to VP and perpendicular to HP. Draw its front and top views.

10. A square plate of side 40 mm has its surface perpendicular to both HP and VP. One of the sides of the plate is inclined at $30^{\circ}$ to HP. Draw its projections and also its traces.

11. A square $A B C D$ of 50 mm side has its corner $A$ on the ground its diagonal AC inclined at $30^{\circ}$ to the HP and the diagonal BD inclined at $45^{\circ}$ to the VP and parallel to the HP. Draw its projections.

12. A square lamina $A B C D$ of 40 mm side has its corner $A$ on the ground its diagonal AC inclined at $45^{\circ}$ to the HP and apparently inclined at $30^{\circ}$ to the VP. Draw its projections.

13. Draw the projection of a pentagonal sheet of 25 mm side resting on VP, having its surface inclined at $30^{\circ}$ to VP. Its one side is parallel to VP and inclined at $45^{0}$ to HP

14. Draw the projection of a hexagonal of 30 mm side, having one of its side in HP and top view inclined at $65^{\circ}$ to VP. And the surface inclined at $35^{\circ}$ to HP.

15. A circular plate of diameter 60 mm has the end $A$ of the diameter $A B$ in the HP and the plate is inclined at $45^{\circ}$ to the HP. Draw its projections when the diameter AB appears to be inclined at $60^{\circ}$ to the VP in the top view.

16. A regular hexagonal lamina of 25 mm side has a central square hole of 20 mm size. Draw the front and top views when the surface of the lamina is inclined at $45^{\circ}$ to the HP. A side of lamina is inclined at $35^{\circ}$ to VP

17. ABCDE is a thin pentagonal plate of 30 mm sides. The edge $A B$ in the VP and the edge CD is parallel to the HP. The corner $D$ is 30 mm away from the VP. Obtain the projection of the plane and find its inclinations with the reference plane

18. A hexagonal lamina of side 30 mm is resting on one of its sides and inclined at 400 to the HP. its surface is inclined at 350 to the VP. Draw the projections

19. A circular lamina of diameter 60 mm has the end $A$ of the diameter $A B$ in the HP and the end $B$ on the VP. Draw its projections when the surface inclined at $40^{\circ}$ to the HP and $50^{\circ}$ to VP.

20. A thin circular plate with 60 mm diameter appears in the front view as an ellips of major and minor axes are 60 mm and 40 mm length respectively. Draw the projection of circular plate when one of the diameters in parallel to both the reference plane.


## PROJECTIONS OF SOLIDS

## Introduction

An object having three dimensions, i.e., length, breadth and height is called as solid. In orthographic projection, minimums of two views are necessary to represent a solid. Front view is used to represent length and height and the top view is used to represent length and breadth.

Sometimes the above two views are not sufficient to represent the details. So a third view called as side view either from left or from right is necessary.

## Objectives

At the end of this session, you will be able to
> Classify the different types of solids
> Draw the projections of solids in various positions in the given quadrant

## Classification of Solids

- Solids are classified into two groups. They are
> Polyhedra
> Solids of Revolution


## Polyhedra

A solid, which is bounded by plane surfaces or faces, is called apolyhedron.
Polyhedra are classified into three sub groups; these are

1. Regular Polyhedra
2. Prisms
3. Pyramids

## 1. Regular Polyhedra

Polyhedra are regular if all their plane surfaces are regular polygons of the same shape and size. The regular plane surfaces are called "Faces" and the lines connecting adjacent faces are called "edges".


## Tetrahedran



A

Octahedran


02

Hexahedran


## 2. Prisms:

A prism has two equal and similar end faces called the top face and the bottom face or (base) joined by the other faces, which may be rectangles or parallelograms.


Triangular prism





## 3. Pyramids:

A pyramid has a plane figure as at its base and an equal number of isosceles triangular faces that meet at a common point called the "vertex" or "apex". The line joining the apex and a corner of its base is called the slant edge. Pyramids are named according to the shapes of their bases.


Triangular Pyramid
O Apex or Vertex



Square Pyramid


## Rectangular Pyramid

Pentagonal Pyramid
Hexagonal Pyramid


Solids of Revolution:
If a plane surface is revolved about one of its edges, the solid generated is called a Solid ofRevolution.


## Cone

A cone can be generated by the revolution of a right-angled triangle about one of its perpendicular sides, which remains fixed. A cone has a circular base and an apex. Theline joining apex and the centre of the base is called the "Axis" of the cone.


## Sphere

A sphere can be generated by the revolution of a semi-circle about its diameter that remains fixed.

## Cylinder

A right circular cylinder is a solid generated by the revolution of a rectangular surface aboutone of its sides, which remains fixed. It has two circular faces. The line joining the centres of the top and the bottom faces is called "Axis".
FRUSTUMS AND TRUNCATED SOLIDS
When a solid is cut by a plane parallel to its base, thus removing the top portion, the remaining lower portion is called frustum. When a solid is cut by a plane inclined to its base, thus removing the top cut portion, the remaining lower portion of the solid is called truncated.

(a) Frustum of Solids

(b) Truncated Solids

## Terms used in solids

Face
Lateral face
Axis
Base
Corners
Apex/vertex

- The surface formed by closed figure.
- A face other than end face or base
- A imaginary line joining the centres of ends or base and apex
-The resting face of solid
-The intersection of edges
- The point at which the lateral edge meetEdge - The line of
intersection of faces Regular solid - Solid which has equal faces
Oblique solid - Solid which has its axis inclined to the base
Generators - An imaginary edge on the lateral surfaces of cylinder/cone
Slant edge - The edge joining apex and corner
Frustum - Solid is cut parallel to the base and removing the top portion
Truncated - Solid is cut inclined to the base and removing the top cut portion


## Projections of Solids

## Perpendicular to the HP



1. A cube of 50 mm side is resting with one of its square faces on the HP.
2. Draw the line $X Y$.
3. Draw the top view as a square (Side 50 mm ) and name its corners.
4. Draw projectors at each corner of the top view through line $X Y$.
5. Draw the front view as a square (Side 50 mm ) and name its corners.
6. Dimension the completed drawing.

7. A square prism of base 30 mm and height 60 mm is resting with its base on the HP and one of its vertical faces perpendicular to the VP.
8. Draw the line $X Y$
9. Draw the top view as square and name its corners.
10. Draw projectors from each corner of the top view through XY.
11. Draw the front view as shown and name its corners.
12. Dimension the completed drawing.


## Perpendicular to the VP



## Parallel to the HP and the VP



1. A square prism of base 30 mm and axis 60 mm long lies on the HP , such that its axis is parallel to both the HP and the VP.
2. Draw the line $X Y$.
3. Draw the projections (top and front views) of the solid in simple position (an edge ofits base is perpendicular to the VP).
4. Rotate the front view through $90^{\circ}$.
5. Draw projectors from the rotated front view and the initial top view and name the pointsof intersection.
6. Join the points correspondingly to get the final top view.



## Parallel to the HP and Inclined to the VP



1. A hexagonal prism of base 30 mm and height 60 mm lies on one of its rectangular faces lies on the HP, such that its axis is inclined at $45^{\circ}$ to the VP.
2. Draw the line $X Y$.
3. Draw the projections of the prism in simple position.
4. Rotate the axis of the top view through $45^{\circ}$ with respect to XY.
5. Draw projectors from the rotated top view and the initial front view and name the points of intersection..
6. Join all the points correspondingly to get the final front view.


## Parallel to the VP and Inclined to the HP


$\left(3^{\prime}, 4^{\prime}\right)$ rests on the HP.
4. Draw projectors from the rotated front view and the initial top view and name the points of intersections.
5. Join the points correspondingly to get the final top view.


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2. A pentagonal pyramid of base 25 mm and axis 55 mm long lies on one of its longer edgeson the HP and its axis is parallel to the VP.
3. Draw the line $X Y$.
4. Draw the projection of solid in simple position.
5. Rotate the Front view such that one of the slant edge o'd' will lie on XY Line.
6. Draw projectors from the rotated front view and the initial top view and name it.
7. Join the points correspondingly to get the final top view.

## Inclined to the VP and the HP



1. A square prism of base 20 mm and axis 40 mm long has its axis inclined at $60^{\circ}$ tothe HP and an edge of its base is inclined at $45^{\circ}$ to the VP.
2. Draw the line $X Y$.
3. Draw the projection of the prism placed in the simple position.
4. Rotate the front view axis through $60^{\circ}$.
5. Draw projectors from the rotated front view and the initial top view and name the points
of intersection.
6. Join all the points correspondingly to get the final front view.

7. A cone of base 30 mm diameter and axis 60 mm long has its axis inclined at $45^{\circ}$ tothe HP and $30^{\circ}$ to the VP.
8. Draw the line XY.
9. Draw the projections of the cone placed in the simple position.
10. Rotate the axis of the front view through $45^{\circ}$.
11. Draw projectors from the rotated front view and the initial top view and name the points of intersection.
12. Join the points correspondingly to get the top view.
13. Rotate the axis of the rotated top view through $30^{\circ}$.
14. Draw projectors from the rotated top view and the rotated front view and name the points of intersection.
15. Join all the points correspondingly to get the final front view.


Positions of solids with respect to reference plane

| S.No | Positions of solids | Step -1 | Step -2 | Step -3 |
| :---: | :--- | :---: | :---: | :---: |
| 1 | Axis of the solid perpendicular to <br> HP and parallel to VP | Draw plan first | Draw elevation <br> next | -- |
| 2 | Axis of the solid perpendicular to <br> VP and parallel to HP | Draw elevation <br> first | Draw plan next | --- |
| 3 | Axis parallel to both VP and HP | Side view | Elevation | Plan |
| 4 | Axis of the solid inclined to VP <br> and parallel to HP | Draw elevation axis <br> perpendicular to VP | Tilt the plan | Get final <br> elevation |
| 5 | Axis of the solid inclined to HP <br> and parallel to VP | Draw plan axis <br> perpendicular to HP | Tilt the <br> elevation | Get final <br> elevation |
| 6 | Axis of the solid inclined to both <br> HP and VP | Draw plan, edge <br> perpendicular to VP |  | Tilt the plan <br> get elevation |

## Axis of the solid perpendicular to VP and parallel to HP

Case (i) : Base edge parallel to HP Case (ii) : Base edge perpendicular to HP
Case (iii): Base edge inclined to HP Case (iv) : Base edges equally inclined to HP


## Axis of the solid perpendicular to HP and parallel to VP

Case (i) : Base edge parallel to VP
Case (iii): Base edge inclined to VP

Case (ii) : Base edge perpendicular to VP
Case (iv): Base edges equally inclined to VP


Axis perpendicular to HP and parallel to VP:
1.(a) A hexagonal pyramid of base side 25 mm and height 50 mm is resting on its base on HP. Draw the projections when one base edge is parallel to VP.
(b) A tetrahedron of side 35 mm rests on the ground on one of its faces with an edge of that face making $45^{\circ}$ with the VP. Draw its projections.

2.(a) A triangular prism of base side 25 mm and height 40 mm is resting on its base on HP. Draw the projections of solid when one of the rectangular face is parallel to VP
(b)A cube of side 30 mm rests on one of its faces with the vertical faces equally inclined to VP. Draw the projection of the solid.

3.(a) A hexagonal prism of side 25 mm and height 55 mm is resting on its base onthe HP with one rectangular face is parallel to VP. Draw its projections.
(b) draw the projection of right circular cylinder of base diameter 35 mm and axis 55 mm when it rests on its base.
(c) draw the projections of a right circular cone of the base 35 mm diameter andheight 55 mm when resting with its base on the HP

5.(a) A cone of base diameter 35 mm and height 55 mm rests on HP on a point of its base circle. Draw its plan and elevation when the base is kept parallel to the VP and its apex is away from the VP
(b) A cube of side 30 mm is resting on the HP on one its edges with the faces containing the resting edge are equally inclined to HP and vertical faces parallel to VP. Draw its projections.

6.(a) A tetrahedron of side 35 mm is placed with a face parallel to VP with a side of the face parallel to HP. Draw its projections.
(b) draw the projections of a square prism of base 25 mm side and axis 50 mm height, when it is lying on the ground on one of its longer edges, such that the lateral faces are equally inclined to HP and the axis is perpendicular to VP. Alsodraw the right side view.



## Axis parallel to VP and inclined to HP:

Axis inclined to one of the principal planes and parallel to the other. When the axis of a solid is inclined to any plane, the projections are obtained in two stages. In the first stage, the axis of the solid is assumed to be perpendicular to the plane to which it is actually inclined and the projections are drawn. In second stage, the position of one of the projections is altered to satisfy the given condition and the other view is projected from it. This method of obtaining the projections is known as the change of position method.
In the change of reference line method, or auxiliary plan method an auxiliary plane is introduced as stipulated and the required final front view is projected on it. This means that a new reference line is to be drawn to represent the auxiliary plane and the required projection drawn

## Axis parallel to VP and inclined to HP - Problems:

8 .A hexagonal prism of base side 25 mm and axis height 55 mm resting on HP with one of its base edges, such that the axis is inclined at $30^{\circ}$ to the HP and parallel to VP. Draw the projections of the prism.

9. A hexagonal pyramid of base side 25 mm and axis height 55 mm is resting on HP with one of its base corners, such that the axis is inclined at $45^{\circ}$ to HP and parallel to VP. Draw the projections of the pyramid.

10. A hexagonal prism of base side 25 mm and axis height 55 mm resting on HP with one of its base corners, such that the axis is inclined at $55^{\circ}$ to the HP and parallel to VP. Draw the projections of the solid.

11.(a) Draw the projections of tetrahedron of side 35 mm kept such that a face is inclined at 350 to HP and perpendicular to VP with one of its edge on HP.
(b) Draw the projections of a pentagonal pyramid of base side 25 mm and axisheight 60 mm with a triangular face perpendicular to HP and VP

13.(a) A cylinder of diameter 35 mm and axis height 55 mm is resting on the groundon its base. It is then tilted such that a solid diagonal is vertical. Draw its projections.


14(a) A cone of diameter 50 mm axis height 70 mm is lying on HP on one of its base point with its axis inclined at $40^{\circ}$ to HP and parallel to VP. Draw the projections.

(b) A cone of diameter 35 mm axis height 55 mm is lying on ground with one of itsgenerators parallel to VP and on the HP. Draw its projections.


15 (a). Draw the projections of a cube of side 30 mm when its rests on one of itscorners with a diagonal of the solid vertical.

(b) A cone of diameter 40 mm and axis height 60 mm is freely suspended from oneof its base points, such that the axis is parallel to VP. Draw the projections


16(a) A pentagonal pyramid of base side 25 mm and axis 55 mm long lies with one ofits slant edges on HP such that its axis is parallel to VP. Draw its projections.

(b) A pentagonal prism of base side 30 mm and axis length 60 mm rests on the HP on one of the base corners with the base edges containing it being equally inclined to HP. The axis is inclined at $45^{\circ}$ to the HP and parallel to the VP. Draw the projections.


17(a) A hexagonal pyramid side of base 25 mm and axis 50 mm long, rests with one of its base on the HP and its axis is inclined at $30^{\circ}$ to the HP and parallel to VP. Draw its projections

(b) A right pentagonal pyramid of base side 35 mm and attitude 60 mm rest on oneof its base edge in HP, the base being lifted up until the highest corner in it is $\mathbf{2 0}$ mm above HP. Draw its projections when the edge on which it rests is made perpendicular to VP.


## Axis parallel to HP and inclined to VP - Problems:

18(a) Draw the projections of a cylinder of diameter 35 mm and axis 55 mm long is resting on HP on one of its generators with its axis inclined at $50^{\circ}$ to VP. Draw its projections

(b) A square prism of base side 25 mm and axis length 50 mm lies on HP on one its longer edges with its faces equally inclined to the HP. Draw its projections when its axis is inclined at $50^{\circ}$ to the VP


19 (a) A pentagonal prism of base side 25 mm and axis length 55 mm resting on HP on one of its rectangular faces with its axis inclined to $45^{\circ}$ to VP. Draw its projections.

(b) A tetrahedron of edges 35 mm rests on one of its edges on the VP. The resting edge is perpendicular to HP and one of the triangular faces containing the resting is inclined at $35^{\circ}$ to the VP. Draw its projections.


20(a) A pentagonal pyramid of base side 25 mm and axis length 55 mm resting on VP on one of its rectangular faces with its axis inclined to $45^{\circ}$ to HP. Draw its projections.

(b) A square pyramid of base side 40 mm and axis length 60 mm resting on VP on one of its triangular faces with its plane containing axis parallel to HP and 30 mm above it. Draw its projections.


21(a) A pentagonal prism of base side 25 mm and axis length 55 mm resting on a lateral edge on HP. The rectangular faces containing that edge is inclined to $30^{\circ}$ to HP. When the axis inclined $40^{\circ}$ to the VP. Draw its projections.

(b) A cone of base 40 mm diameter and axis 50 mm long touches the VP on a point of its base circle. Its axis is inclined at $30^{\circ}$ to the VP and parallel to HP. Draw its projections.


22(a) draw the projection of pentagonal prism 30 mm side of base and 70 mm long lying on one of its longer edges on HP with one of rectangular faces perpendicularto HP such that the axis makes $60^{\circ}$ with VP.

(b) A cone of base diameter 50 mm and axis length 60 mm is resting on VP on one of its generators with its axis parallel to HP. Draw its projections.


23(a) A hexagonal pyramid of base side $\mathbf{2 5 m m}$ and axis length 60 mm is resting on VP on one its triangular face with its axis parallel to HP. Draw its projections.

(b) Draw the projections of a square pyramid of 32 mm side of base and axis 55 mm . It is resting on HP on one of its base corners with a base side containing the corners making $30^{\circ}$ with HP. The axis is inclined at $30^{\circ}$ to VP and is parallel to HP. The vertex is away from the VP


## 24. Draw the projection of cube of side 35 mm when it is resting on one of itscorners

 on VP and an edge containing that corner is inclined at $40^{\circ}$ to VP

## SUMMARY

1. Prism -- Axis parallel to VP and perpendicular HP


1-Axis inclined at $30^{\circ}$ to HP and parallel to VP.
2 - Base inclined at $50^{\circ}$ to HP.
3 - Longer edge containing the resting corner makes an angle of $40^{\circ}$ to HP.
4 - Solid diagonal vertical.

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1-Axis inclined at $30^{\circ}$ to HP and parallel to VP.
2 - Base inclined at $50^{\circ}$ to HP.
3 - Rectangular face containing the resting edge makes an angle of $40^{\circ}$.


1-Axis inclined at $45^{\circ}$ to HP and parallel to VP. 2 - Base inclined at $50^{\circ}$ to HP.
3 - Generator inclined at $40^{\circ}$ to HP. 4 - Solid diagonal vertical.


1- Axis inclined at $40^{\circ}$ to HP and parallel to VP.
2- Base inclined at $50^{\circ}$ to HP.
3- Generator inclined at $40^{\circ}$ to HP.
4- Point diametrically opposite to the resting point is being lifted toheight of 30 mm from HP.
5- Apex is being lifted to height of 40 mm from HP.
6- Resting or lying on HP with one of its generators.
7- Generator perpendicular to HP and parallel to VP.
8- Freely suspended from a base point.



1- Axis inclined at $40^{\circ}$ to HP and parallel to VP.
2- Base inclined at $50^{\circ}$ to HP.
3- Triangular face containing the resting edge makes an angle at $40^{\circ}$ to VP.
4- Base edge and the corner opposite to the resting edge is being lifted toa height of 30 mm from VP.
5- Apex is being lifted to height of 40 mm from HP.
6- A triangular face perpendicular to VP and HP.
7- Lying on the wall with one of its triangular face.


1- Axis inclined at $40^{\circ}$ to HP and parallel to VP.
2- Base inclined at $50^{\circ}$ to HP.
3- Triangular face containing the resting edge makes an angle at $40^{\circ}$ to HP.
4- Base edge and the corner opposite to the resting edge are being lifted to a height of 30 mm from HP.
5- Apex is being lifted to height of 40 mm from HP.
6- A triangular face perpendicular to HP and VP.
7- Lying on the wall with one of its triangular face.
8- Freely suspended from a base point.

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Sectioning of above-solids in simple vertical position when the cutting plane is inclined to the one of the principal planes and perpendicular to the other - obtaining true shape of section. Development of lateral surfaces of simple and sectioned solids - Prisms, pyramids cylinders and cones.

## Different Positions of Cutting Plane:

1. Cutting Plane Perpendicular to VP and Parallel to HP.(Top View is True shape of the section)
2. Cutting Plane Perpendicular to HP and Parallel to VP. (Front View is True shape of the Section)
3. Cutting Plane Perpendicular to VP and Inclined to HP. (True shape is perpendicular to the given to $\theta^{\circ}$ )
4. Cutting Plane Perpendicular to HP and Inclined to VP. (True shape is perpendicular to the given to $\phi^{\circ}$ )
5. Cutting Plane Perpendicular to both HP and HP. (Side View is True shape of the section)


6. 


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2. A Section plane cuts the solid axis at a distance 35 mm from the vertex. Draw the sectional top view, front view and true shape of the section, Also draw the lateral surface development of the Iruncated pyramid.

cesses)
4. A thread is wound on the lateral surface of the Cone of diameter 50 mm and axis 65 mm , starts from left base extreme base point and ends at the same point after one revolution. Draw the path traced by the thread in top view and front view.

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Principles of isometric projection - isometric scale -Isometric projections of simple solids and truncated solids - Prisms, pyramids, cylinders, cones- combination of two solid objects in simple vertical positions - Perspective projection of simple solids-Prisms, pyramids and cylinders by visual ray method.

Isometric axes: The three lines meeting at the point and making 120 。angles with each other is called isometric axes.

Isometric lines : All lines parallel to these axes are called isometric lines.
Isometric planes: The planes formed by isometric axes and the parallel planes are called isometric planes.
Isometric Scale : A correct isometric projection is drawn with the use of a special isometric scale.The conversion of true length into isometric length is called isometric scale.

Ratio of Isometric length to True length: Isometric length $/$ True length $=0.82$



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08. A sphere of radits 50 mm is keot contrally over a frustum of a square pyramid of side 120 mm at the bottom, 80 mm at the tpp and having a height of 100 mm . Draw the isometric projection of the solid.
09. A spuare pyramid of side 30 mm , axis length 50 mm is centrally placed on the top of a cube of side 50 mm . Draw the isometric projection of solids.


10- A cone of base diameter 30 mm and height 40 mm rests centrally over a frustum of a hexagonal pyramid of base side 40 mm , top base 25 mm and 60 mm height. Draw the isometric projection of the solids.
11- A cylindrical slab of thickness 30 mm and diameter 50 mm is surmounted by a square pyramid of side 30 mm and height 40 mm . Draw the isometric view of the combination if the axis of cylinder and pyramid
coincide with each other



Problem-11 : Solution

> Problem-10 : Solution

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Perspective projection is a method of pictorial projection, where the three dimensional object is drawn more realistically than isometric drawings. The perspective drawings show three - dimensional objects as they appear to the eye or as they are seen in a photograph.

Following are the certain terminologies that are used, while drawing a perspective view:
Ground Plane (GP): It is a horizontal plane on which the object is assumed to be situated.
Picture Plane (PP): It is a transparent plane situated between the observer and the object, through which the object is viewed. The perspective view is formed on this picture plane.
Ground Line (GL): The line of intersection of the picture plane with the ground plane is called the ground line.
Station Point (SP): Location of the eye of the observer while viewing the object, measured from the ground plane and from the picture plane.
Horizon Plane (HP): This imaginary plane is at the level of the eye, i.e. the station point. It is a plane parallel to the ground plane.
Horizon Line (HL): It is a line which the horizon plane intersects the picture plane. It is parallel to the ground line.
Central Plane (CP): It is an imaginary plane passing through the station point (SP) and perpendicular to both the Picture Plane (PP) and Ground Plane (GP).

01 -A regular hexagonal pyramid of base edge 20 mm and height 35 mm rests on its base on the ground plane with one of its base edges touching the picture plane. The station point is 30 mm above the ground plane and 40 mm in front of the PP. The central plane is 30 mm to the right of the axis. Draw the perspective projection of the pyramid by visual ray method. Use the top view and the front view.

02 -A hexagonal pyramid of base side 30 mm and axis height 50 mm is resting on GP on its base with a side of base parallel to and 25 mm behind the PP. The station point is 60 mm above $G P, 90 \mathrm{~mm}$ in front of $P P$ and lies in a central plane which is 55 mm to the left of the axis of the pyramid. Draw the perspective view of the pyramid by visual ray method.

Problem-01 : Solution


Problem-02 : Solution


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Q1, Q2: A Pentagonal (or-Hexagonal) Prism of side $28 / 23 \mathrm{~mm}$ and Height 70 mm rests with its base in the ground and one of its rectangular faces is Parallel and 15 mm behind the Picture Plane(PP). The station Point is 45 mm in front of PP, 70 mm above the Ground and 40 mm Right to the Axis of the Prism. Draw the Perspective view of the Prism.


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Projection of the solid plane and 80 mm axis. 30 mm infront of the picture Station Point is 45 mm Right to mm beight picture plane. Th with its base and one of its Square Prism of side 40 mm and
height 70 mm lies on the ground

N A rectangular prism, sides of base 50
$m m \times 30 \mathrm{~mm}$ and height 55 mm rests
with its base on the ground plane. A


$\qquad$





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