Woltage (v) voitage is the difference in electric grothin had between two points, that pushes chargel an Electric Circuit, It shows the Components and electrons (Qurrent) through a conducting loop. Interconnections of the circuit using symbols. Electrical components which allows a current through it. opposition to the current flow. in an I lectrical circuit Cirtuit Diagram: - It is a graphical representation of Electrical circuit: It is a closed path of wires and Petini Hons: EC 3251 Circuit Analysis Conductonce: (4) Resisby: Resichance: - (R) Conductance is the reuponcul of resistance It is represented by the letter'R' Resistance Huandand unit of Resistance = is the a measure of the that offer Resistance Unit I DC Circuit Analysis Shop (ohms)

Charge:

Annount of energy or electrons that puss from one body to another.

Collomb is the unit of Electric charge institute of technology

unit of lanductance is Tr (mho)

charge

Current (I)

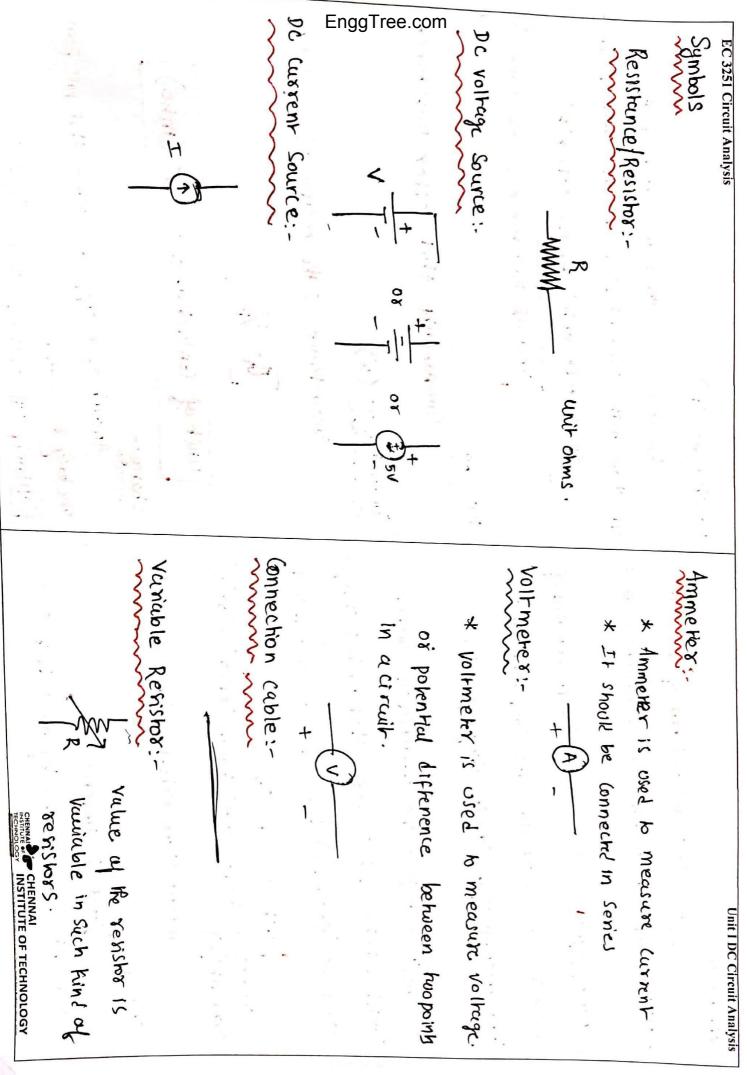
Voltach is represented by the letter vior'E

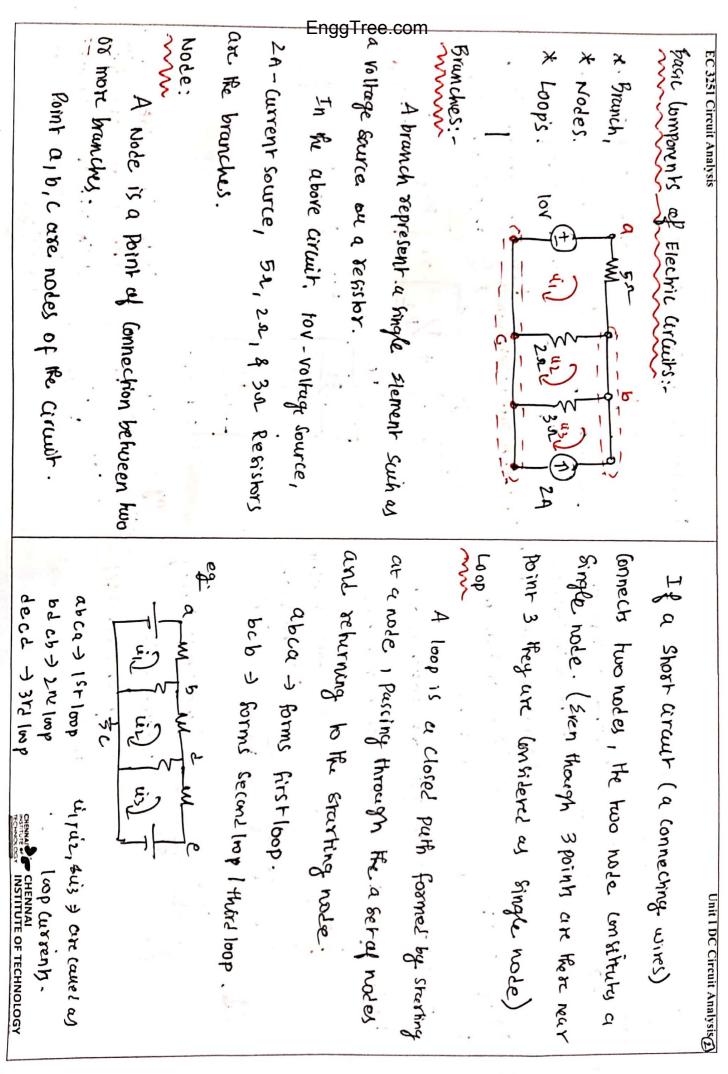
unit is volts (v)

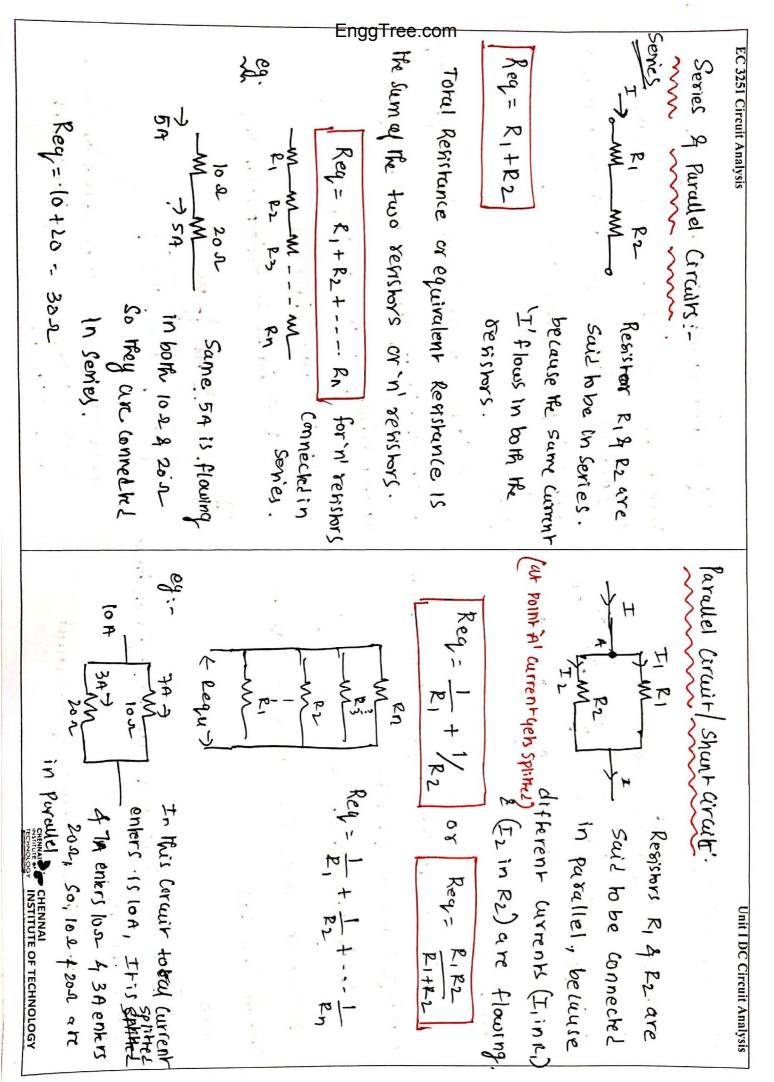
Current is the rate of flow of electric

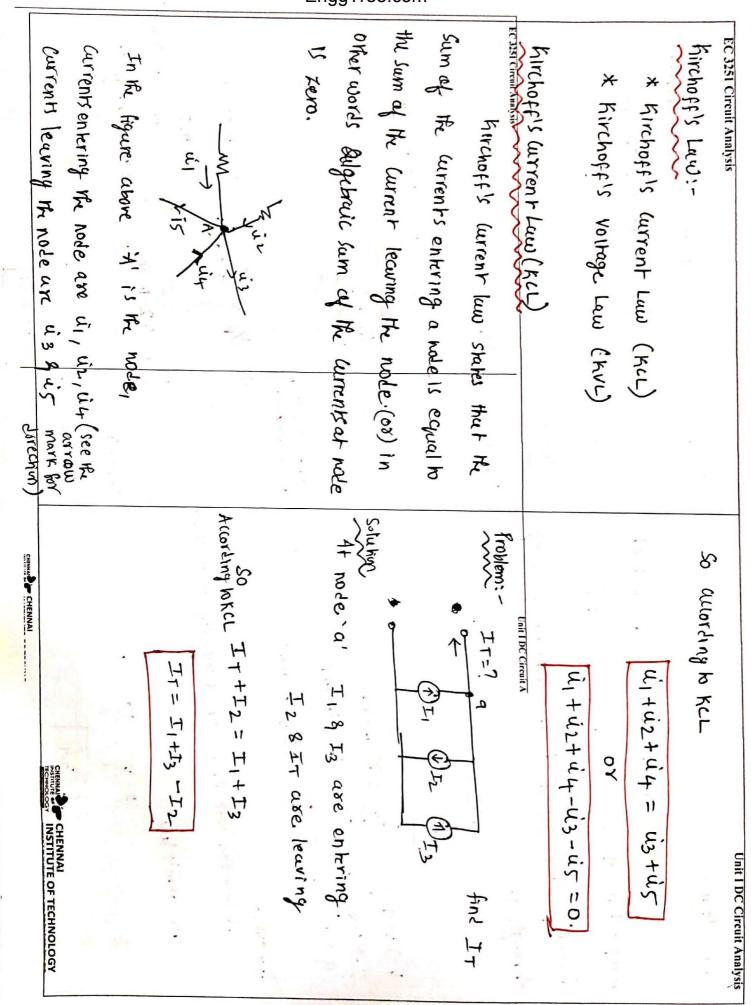
current is represent I by the letter I'.

unit is amperes (A)









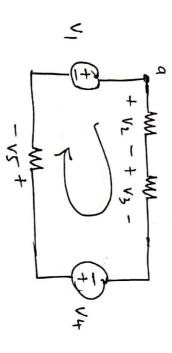


firchoff's vollage Law: 1 fvl)

algebraic sum of our voltages around a closed path or loop is zero. Kirchoff's vollege law states that the

or in otherworls. In a close arail.

Sum of the potential raise = Sum of the potential drops



let Sturts from pointa's + traverse the loop. + V2 + V3 - V4 + V5 - V1 = 0

V1+V4= V2+V3+V5

VI & V4 = Poknikal raise, VL, U3 EV5- Poknikal

'R' then a vollage drop vi ocurs at the resistor R, with the polunity shown. Concept to rembon ber; -If courrent I' flows in to a restably

Unit I DC Circuit Analysis

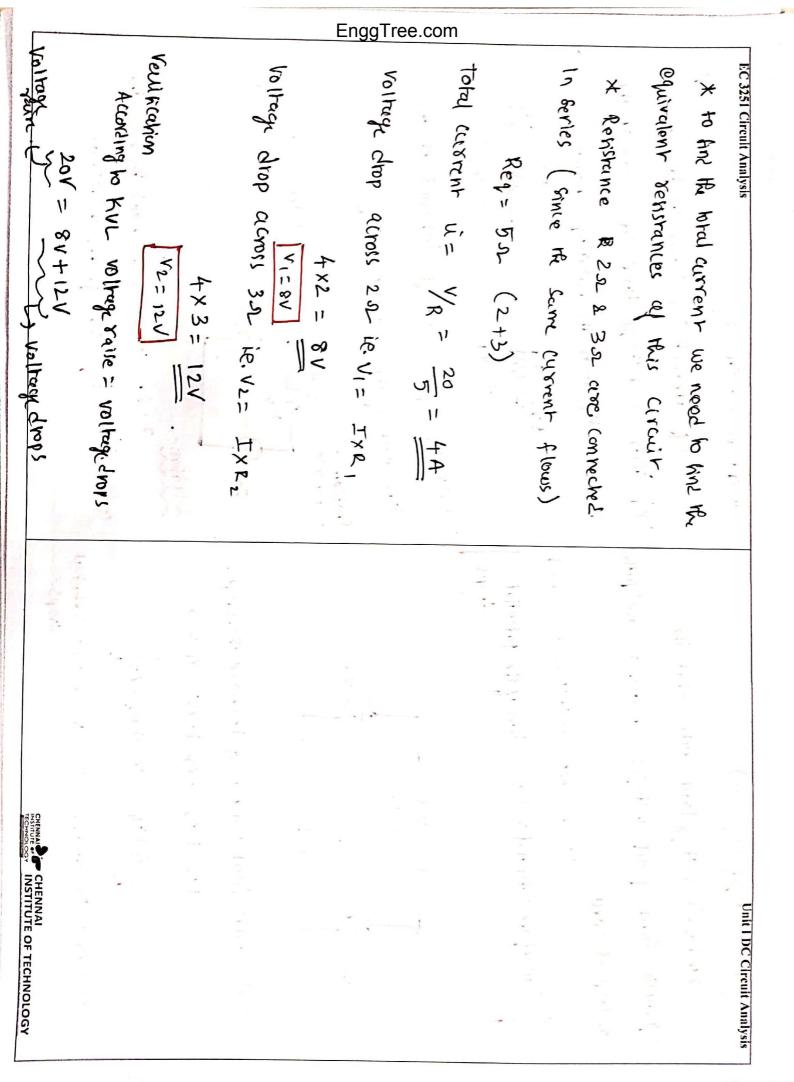
MM TZ

direction of the current entry, incaescul Polarity of the voltage depends on 1 \sqrt{2}

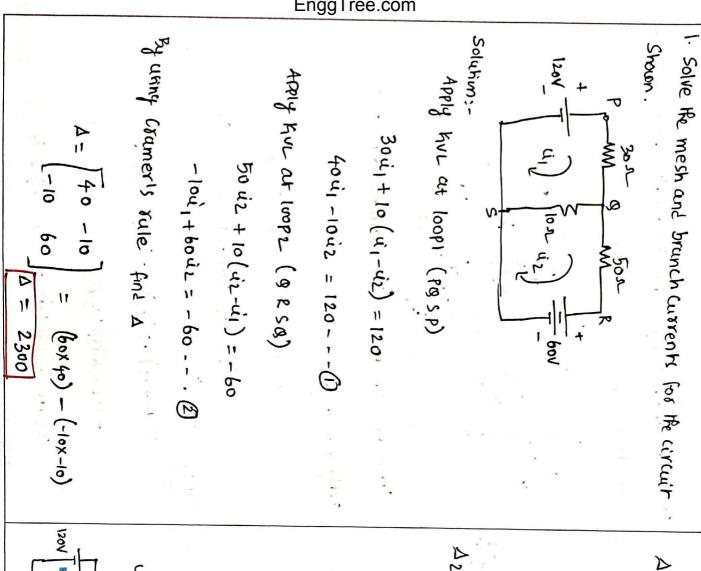
Problems

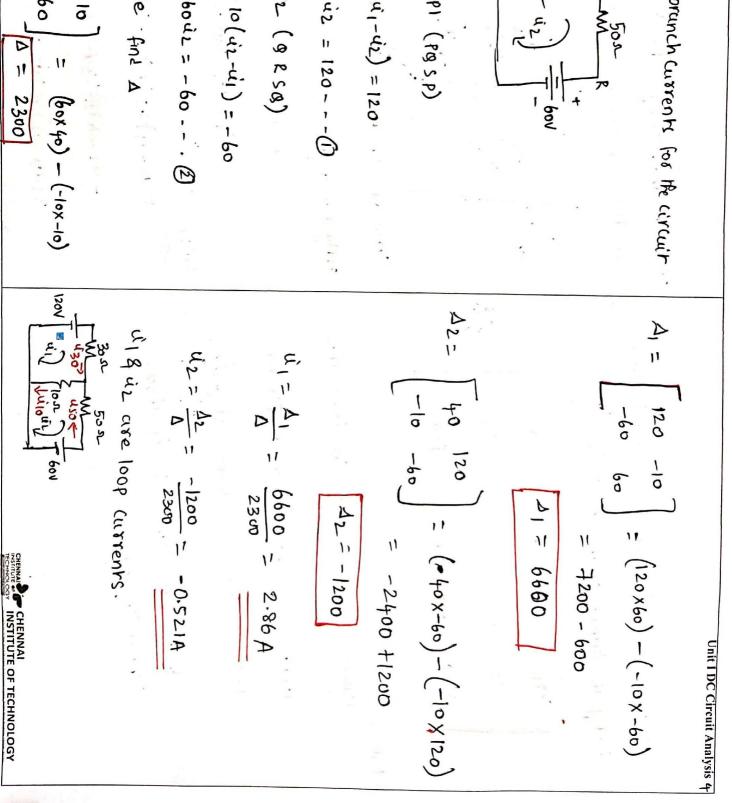
for the circuit shown. find the voltages v, 8vzt

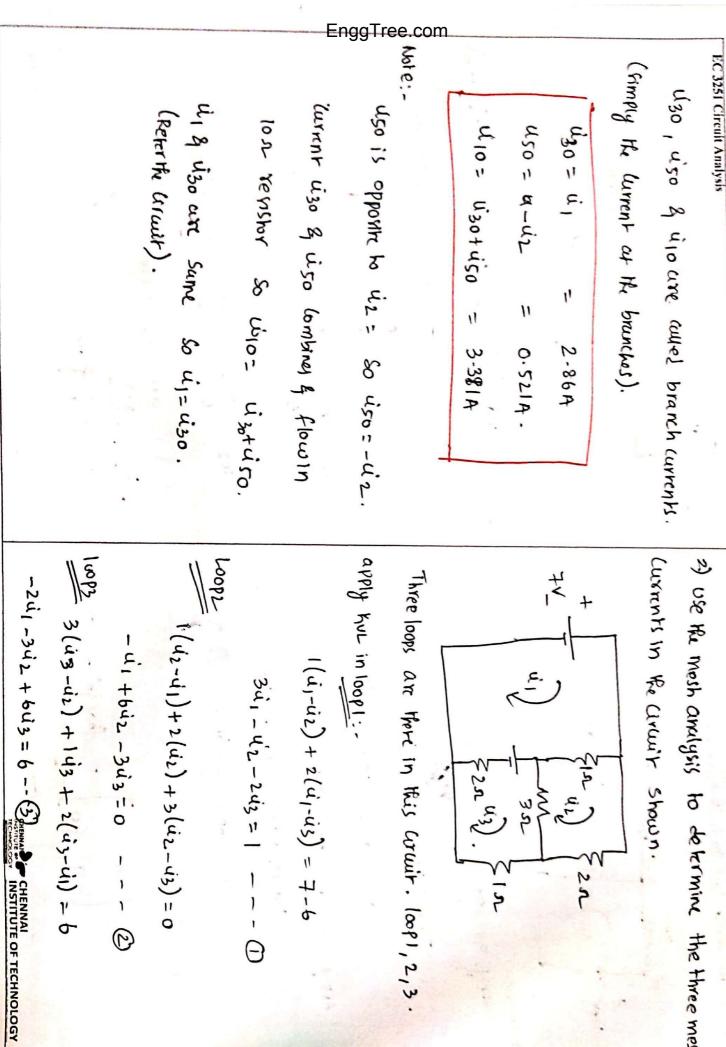
Solution: current flowing through the To find v, 2 vz, we need to find resting. CHENNAI CHENNAI 丞

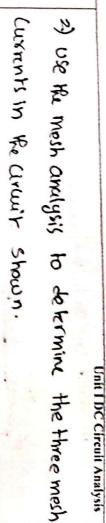


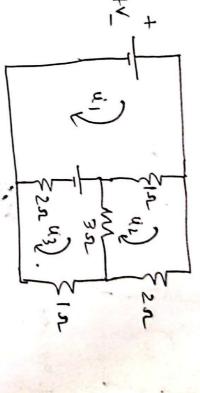
EC 3251 Circuit Analysis











Three loops are there in this cormit. 10091, 2,3

apply kul in
$$|000p1:$$

$$|(\dot{a}_1 - \dot{a}_2) + 2(\dot{a}_1 - \dot{a}_3) = 7 - 6$$

$$3\dot{a}_1 - \dot{a}_2 - 2\dot{a}_3 = 1 - - - 0$$
Loon,

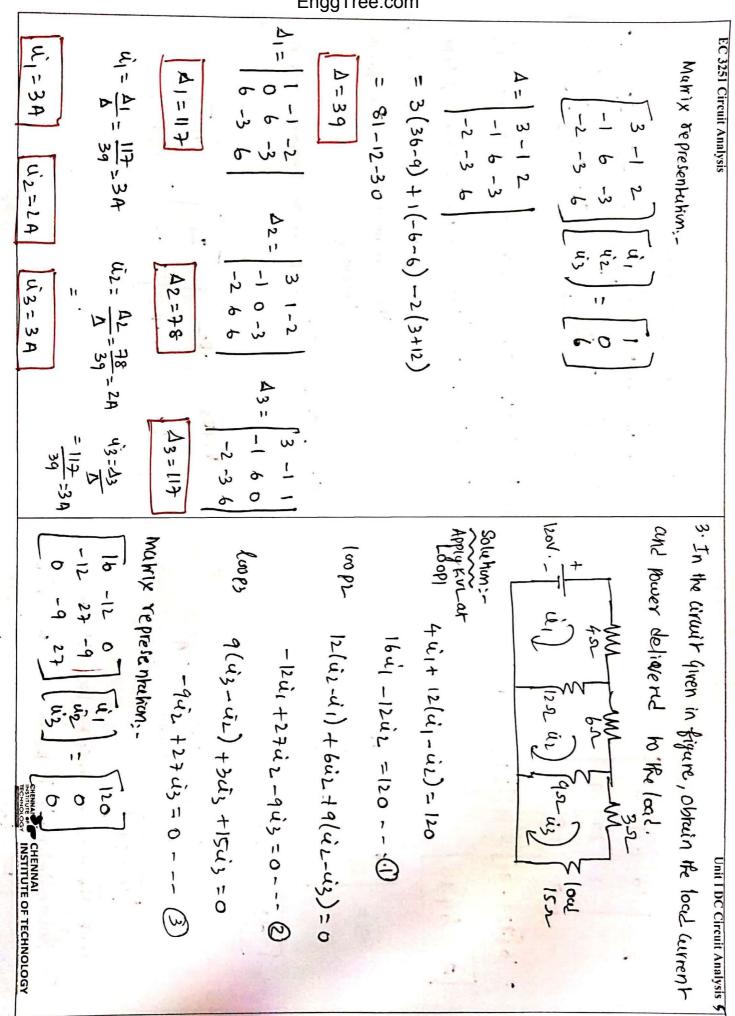
$$\frac{\log p_{2}}{\log p_{3}} = (i(i_{2}-i_{1})+2(ii_{1})+3(ii_{2}-ii_{3})=0$$

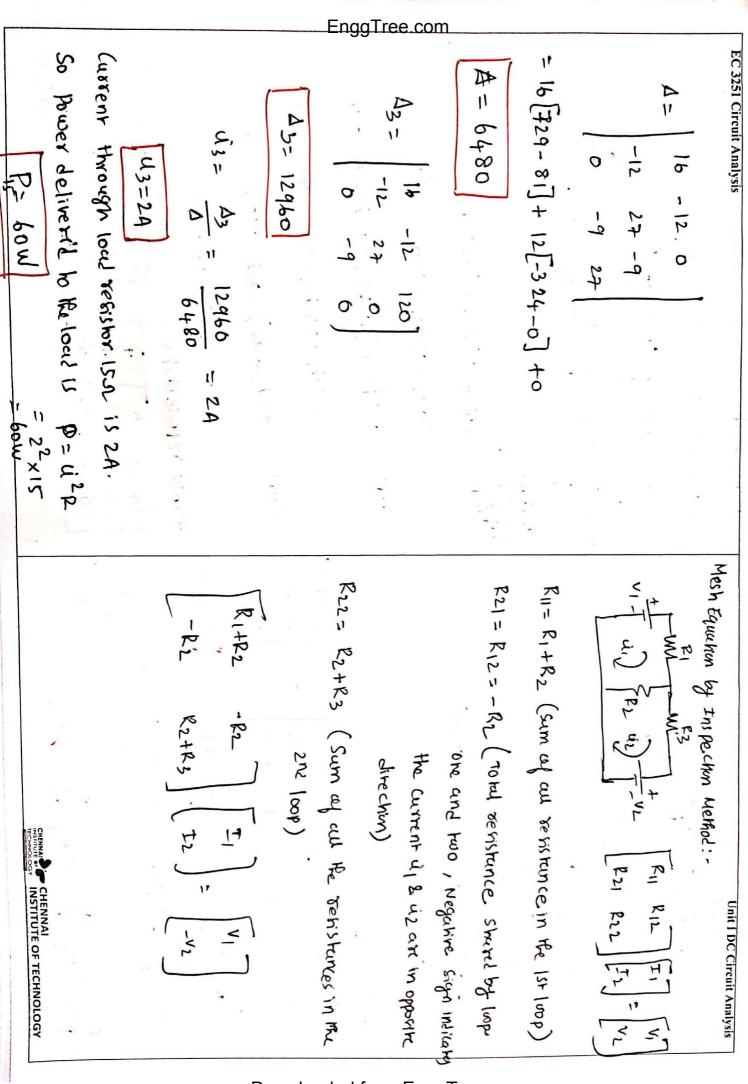
$$-i(1+bii_{2}-3ii_{3}=0$$

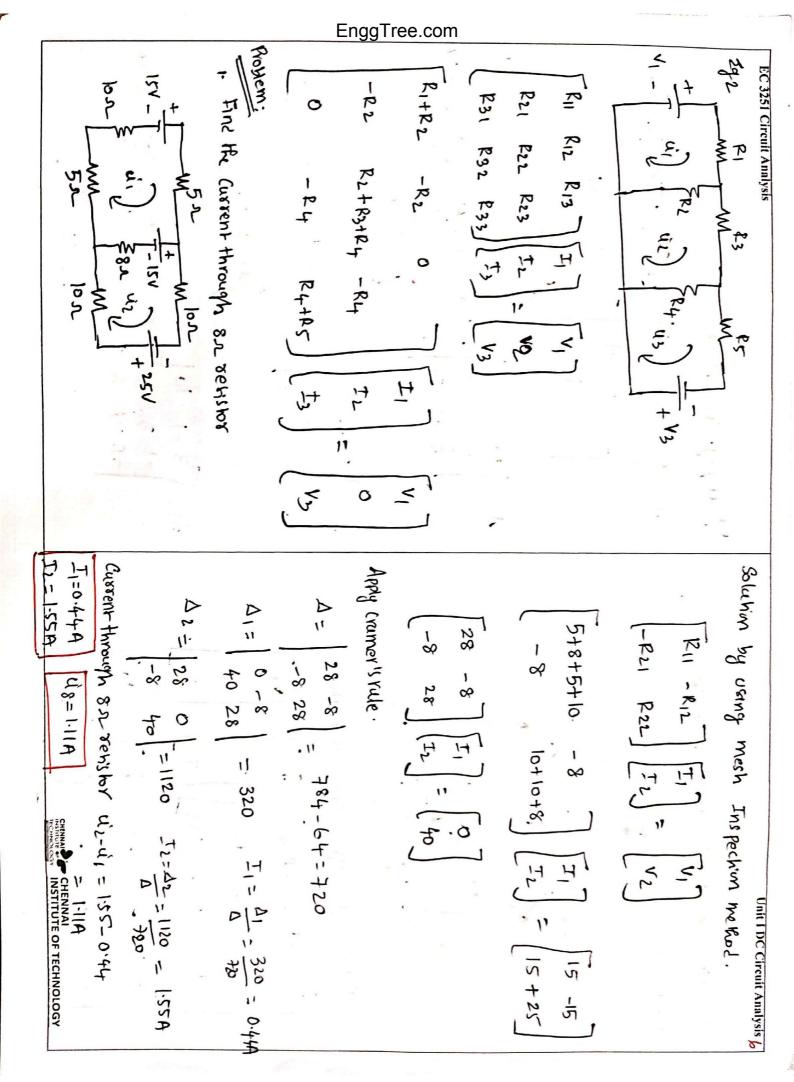
$$-(2)$$

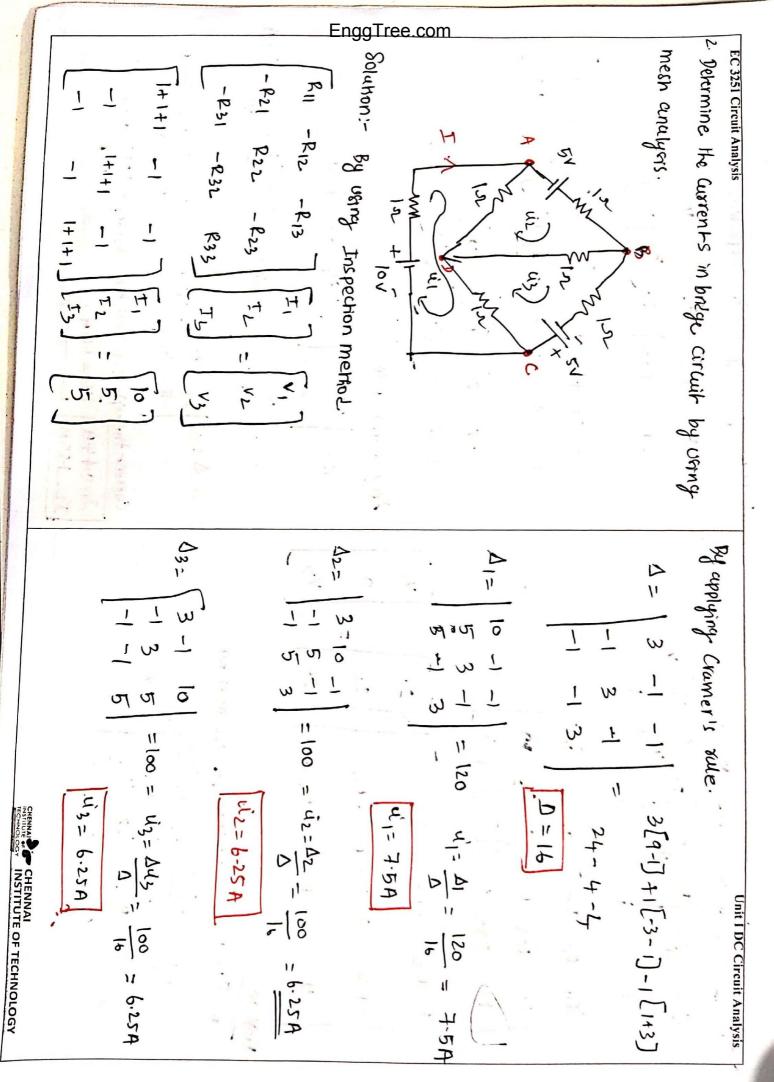
$$\log p_{3}$$

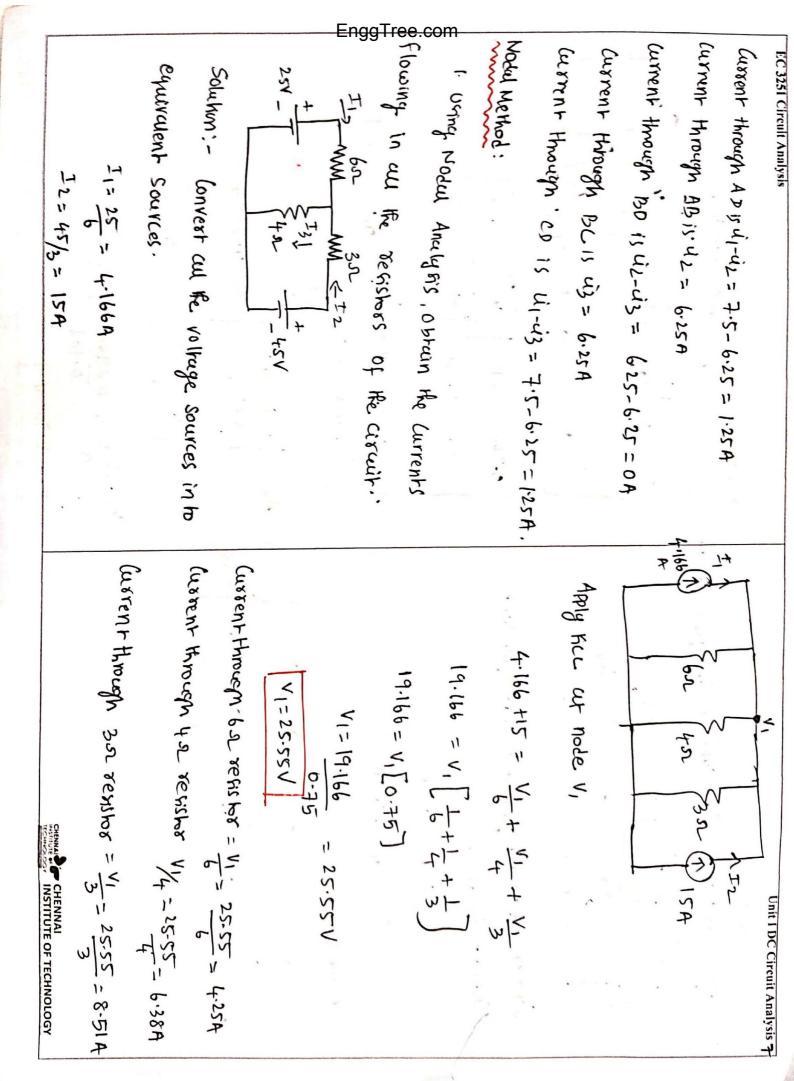
$$3(ii_{3}-ii_{1})+1ii_{3}+2(ii_{3}-ii_{1})=b$$

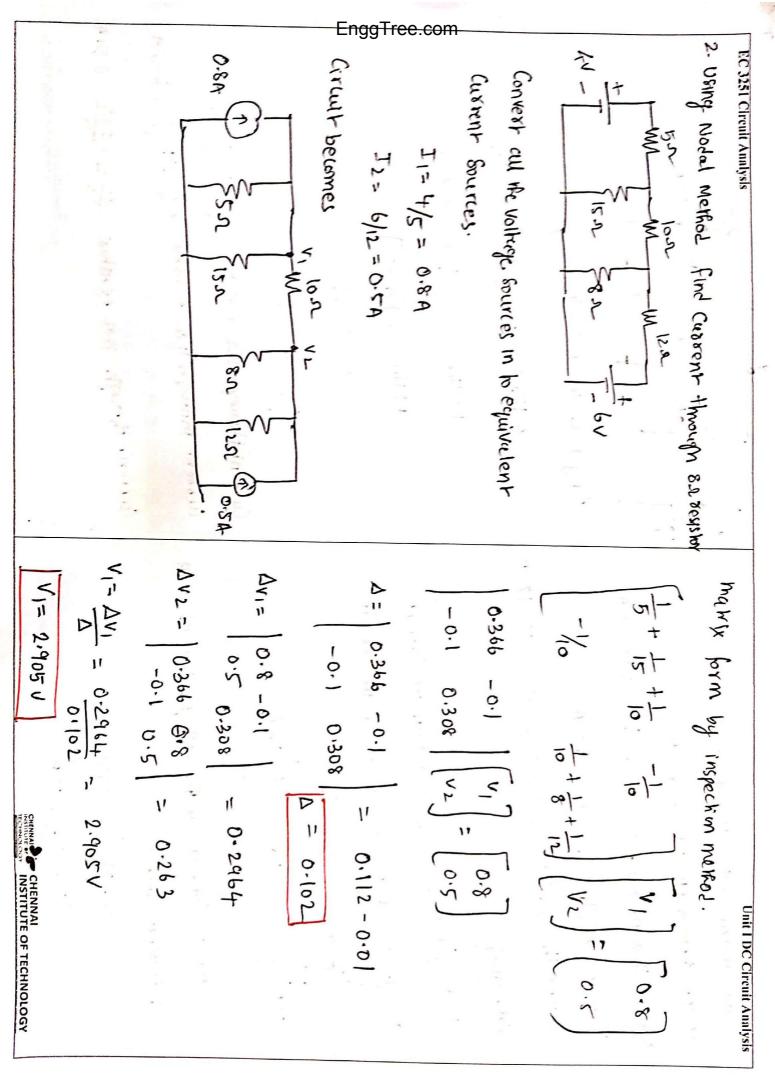


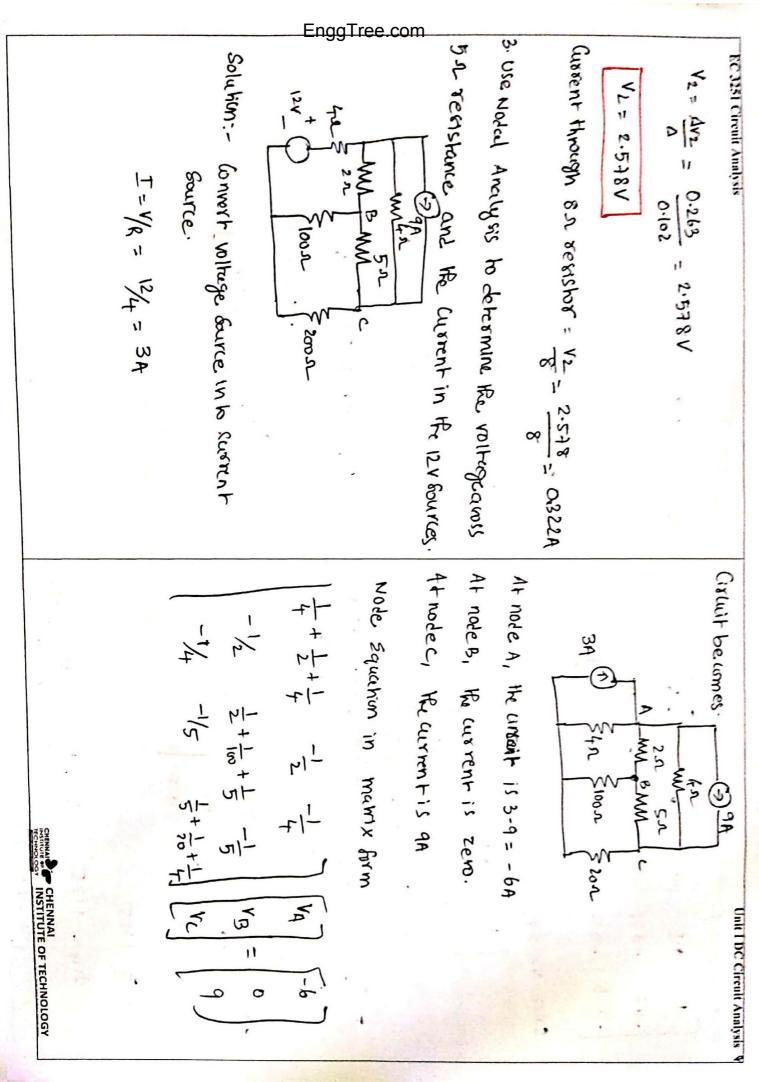


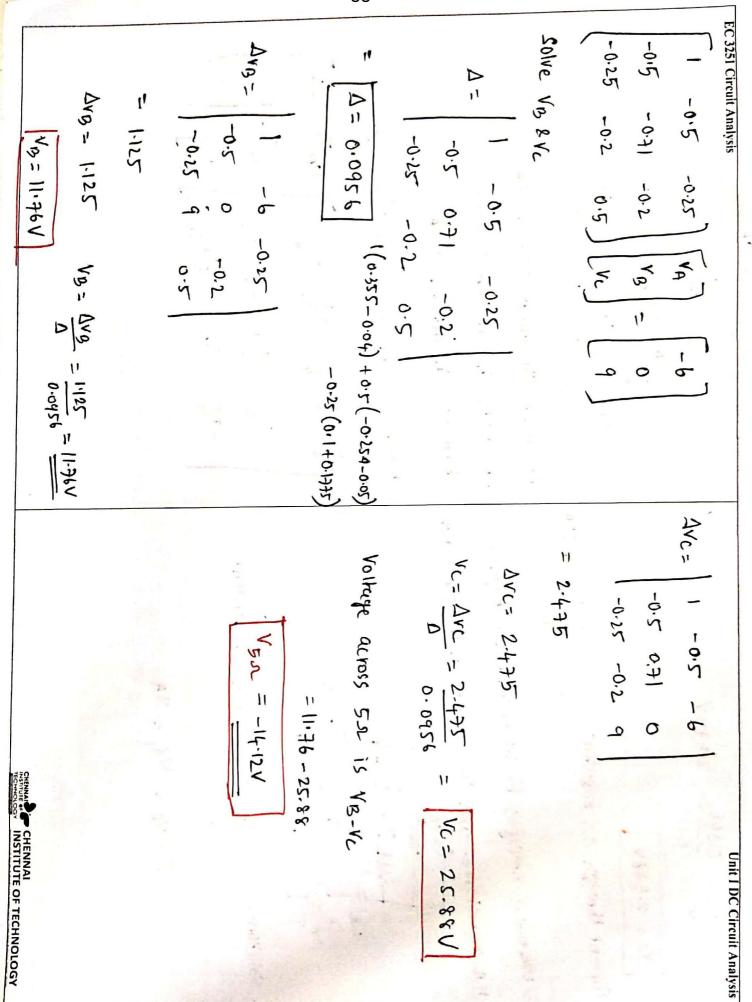


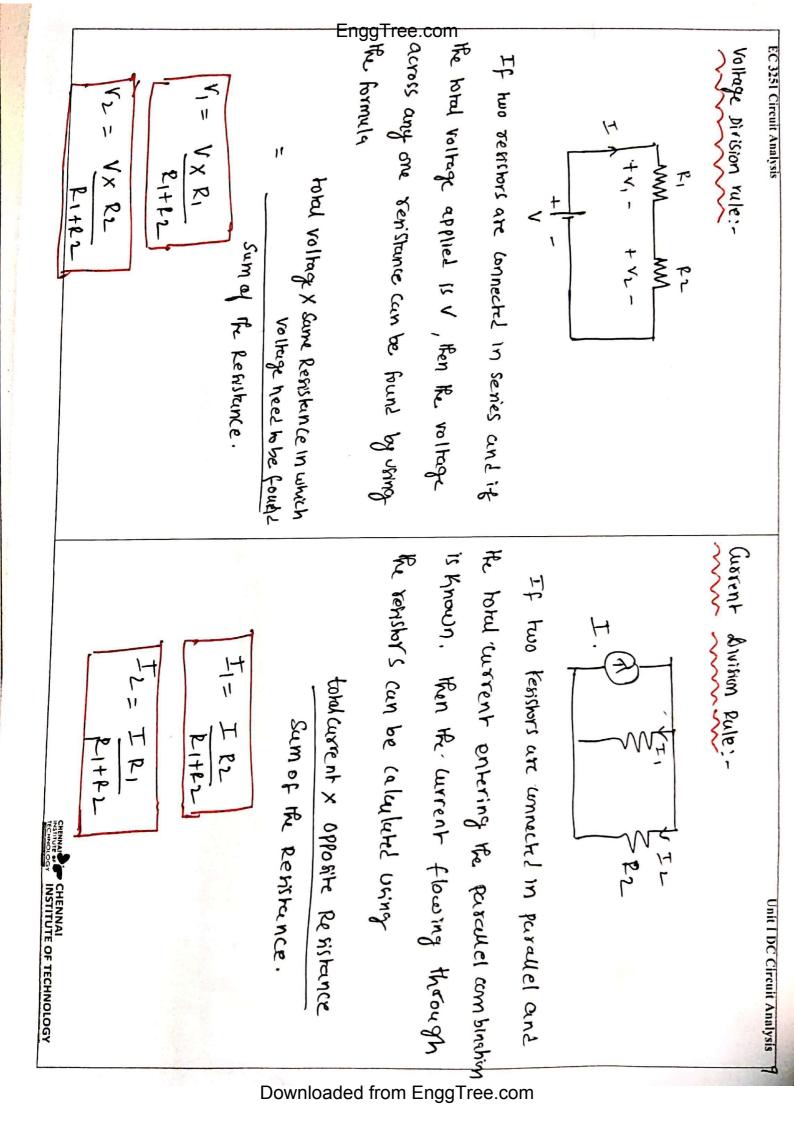












Super Position Theorem:

Super Position Theorem states that the response in a circuit with molitiple sources is given by the algebraic sum of responses due to individual sources acting abone.

EC 3251 Circuit Analysis

4 - W - W - V 2

Procedure skps:

1) In a live with motherle sources keep only one source active (v, - active, v2-short)

Premove all the other Sources (voitage Sources must be short circuited, wrint Sources must be open

3 find the reformse of the arcuit for the individual sources and label the term as I, 1, Iz 1 & I3 1 etc.

Ji - Shorke

Unit II DC Network Theorem and Duality

@ Now keep the other source active and remove the first

Shorter & Ry Es Tri

B NOW take find the response due to the source ve and label the winent as It, I, I, I' & Iz ".

 $\begin{array}{c|c} & & & & & & & \\ \hline \begin{array}{c} & & & & & \\ \hline \end{array} \\ \begin{array}{c} & & & \\ \end{array} \\ \begin{array}{c} & & \\ \end{array} \\ \\ \begin{array}{c} & & \\ \end{array} \\ \\ \end{array} \\ \begin{array}{c} & & \\ \end{array} \\ \begin{array}{c} & & \\ \end{array} \\ \\ \end{array} \\ \begin{array}{c} & & \\ \end{array} \\ \begin{array}{c} & & \\ \end{array} \\ \\ \end{array} \\ \begin{array}{c} & &$

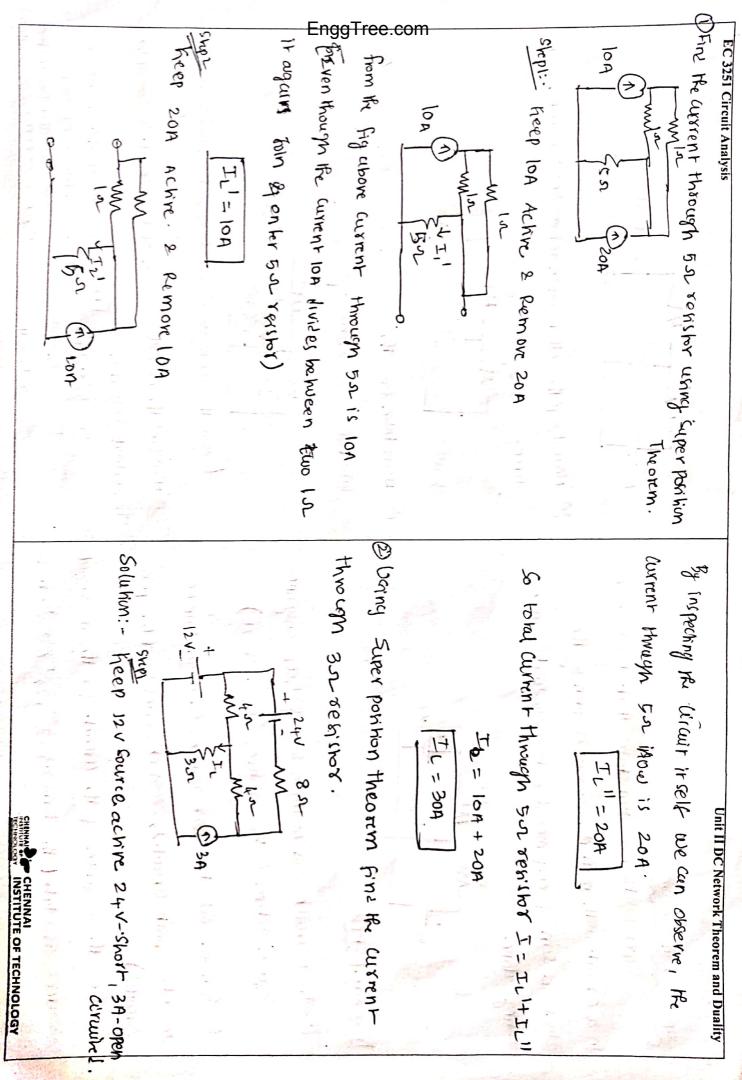
2

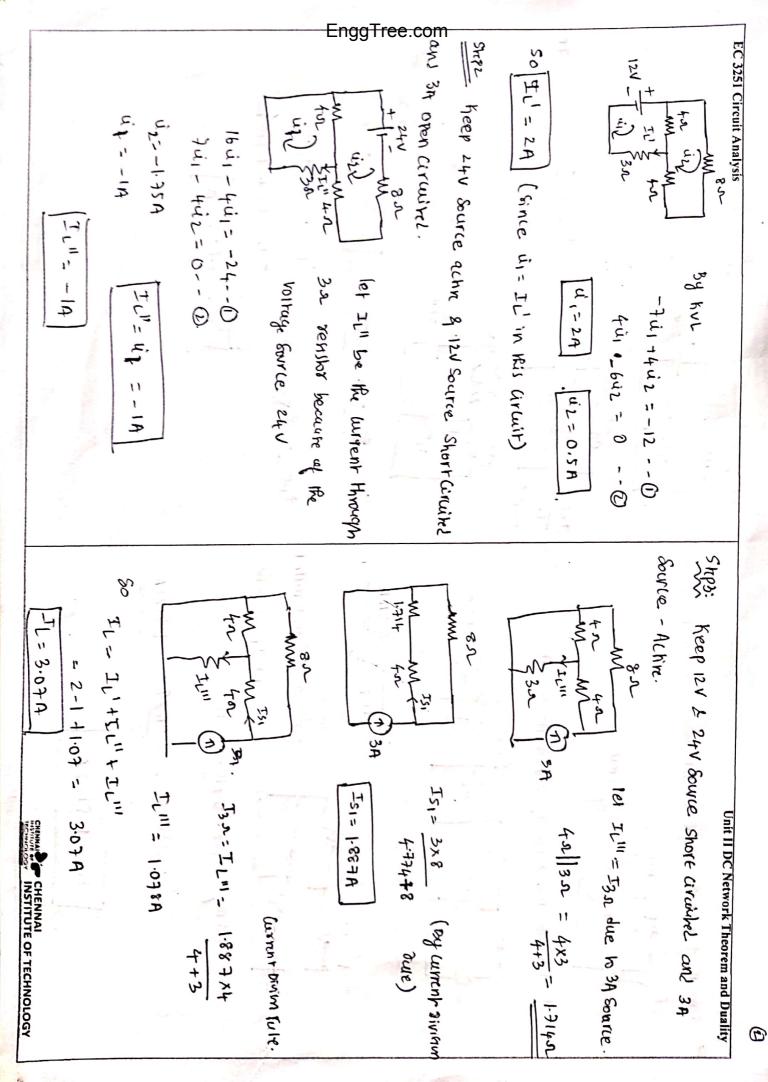
(6) Now find the overall retires of the circuit by sum up the

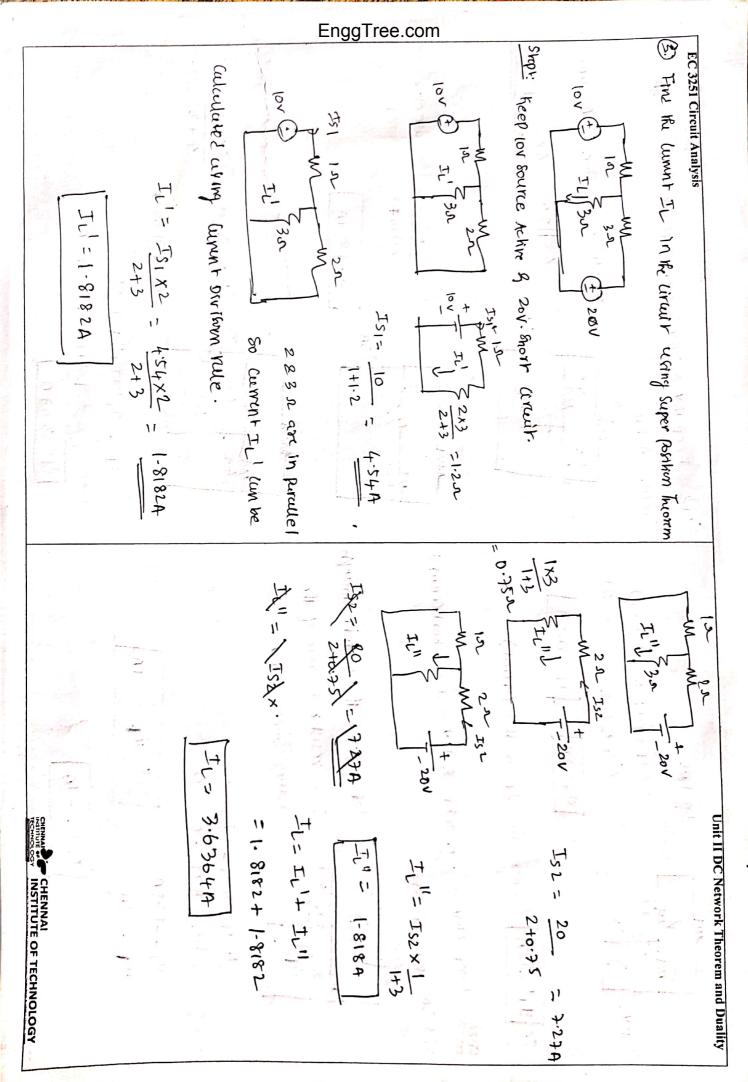
Individual responses:

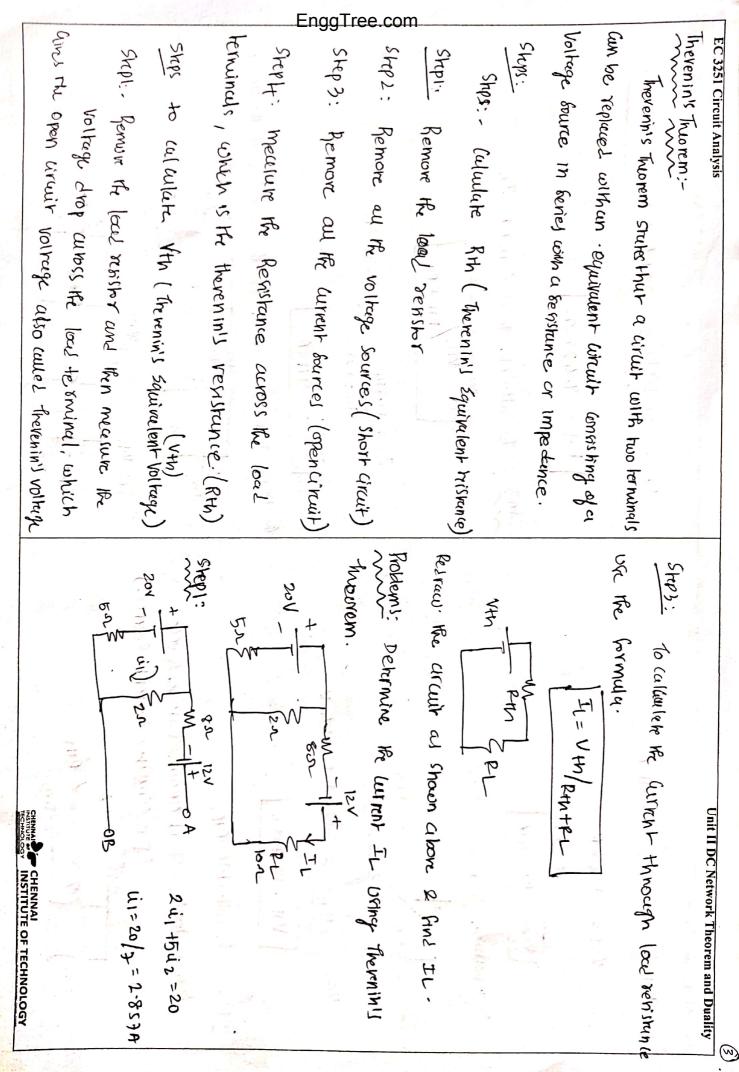
\[\text{Line : Depending apon the direction } \\
\text{T}_1 = \text{T}_1 + \text{T}_1 | \text{Custance con may vary, once} \\
\text{T}_2 = \text{T}_2 | + \text{T}_2 | \text{Custance con may vary, once} \\
\text{T}_3 = \text{T}_3 | + \text{T}_3 | \text{Custance con may vary, once} \\
\text{T}_3 = \text{T}_3 | + \text{T}_3 | \text{Custance con institute of technology} \]

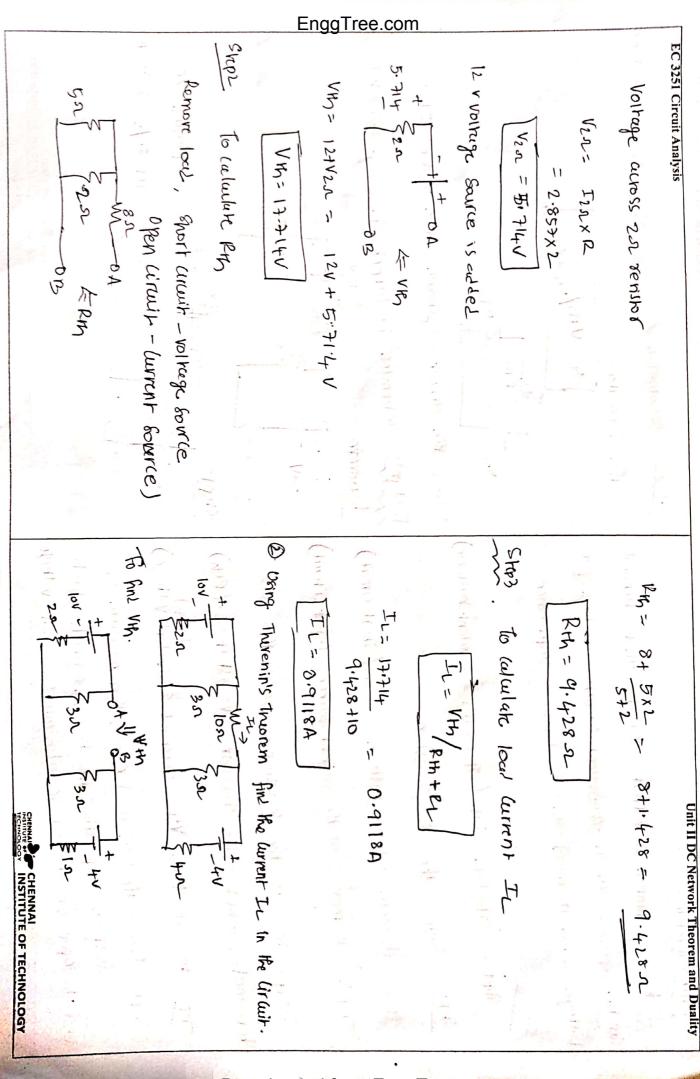
\[
\text{Individual responses:} \]

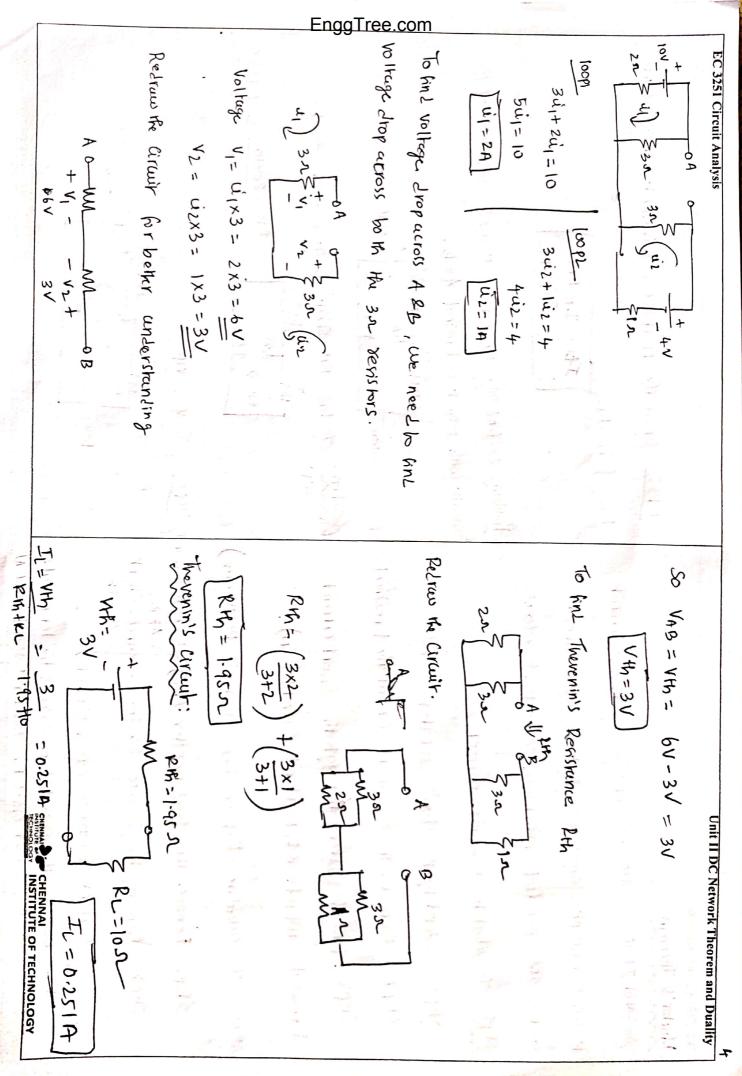


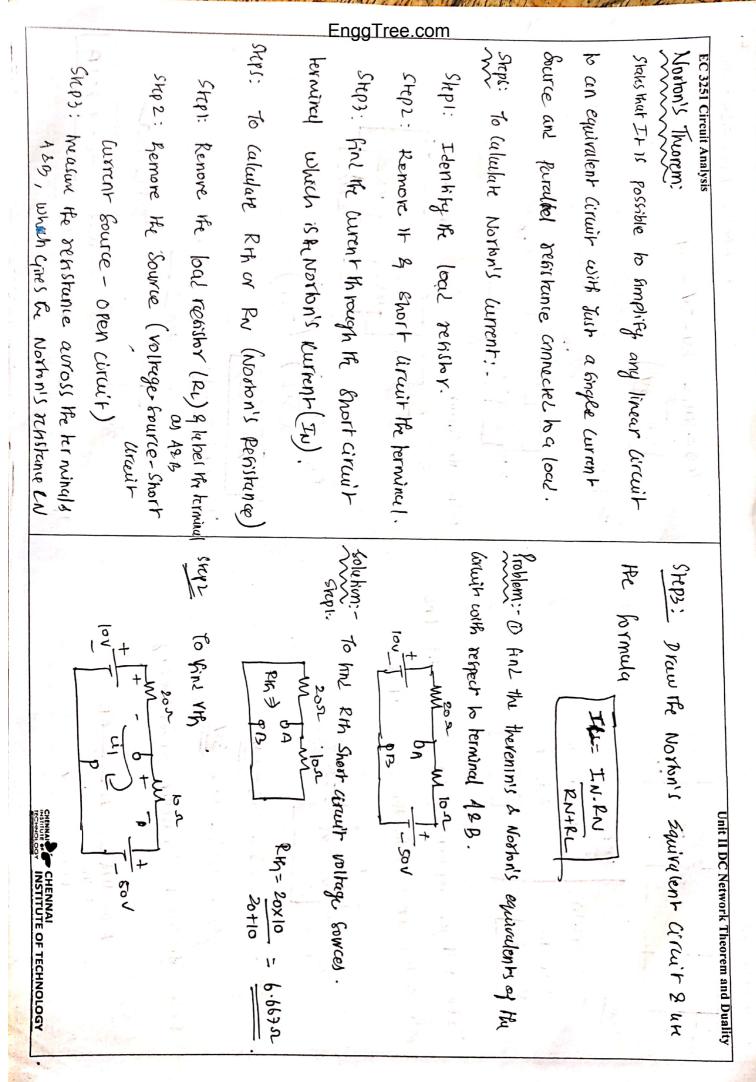


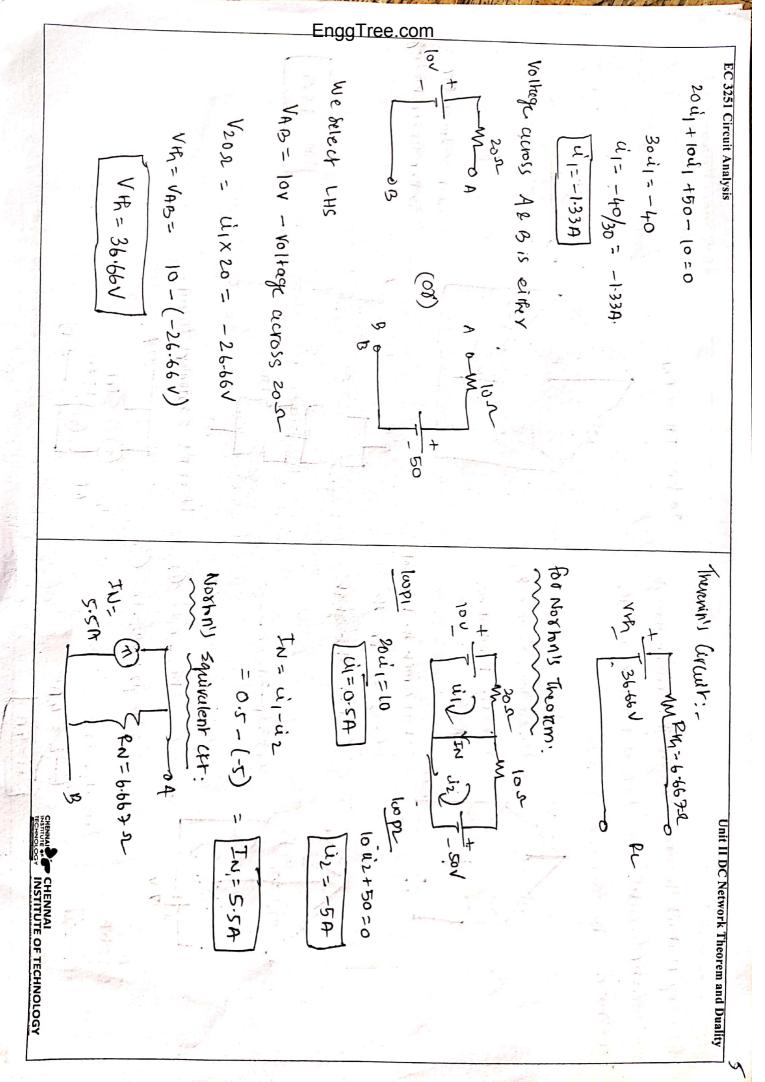


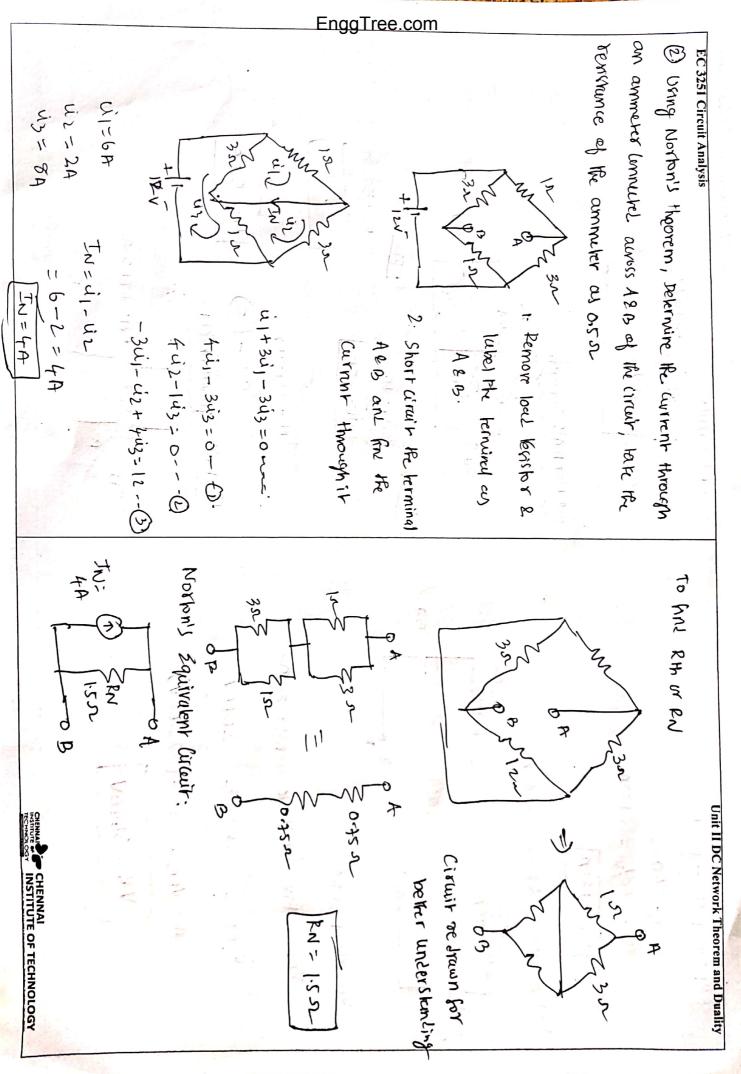


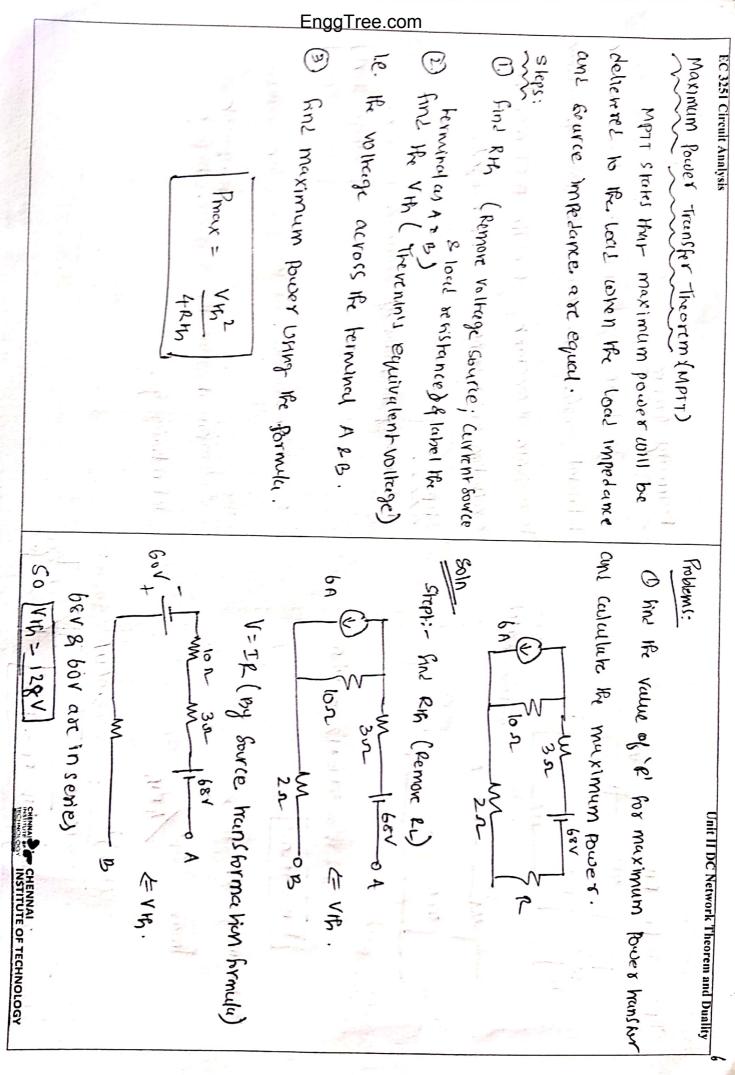


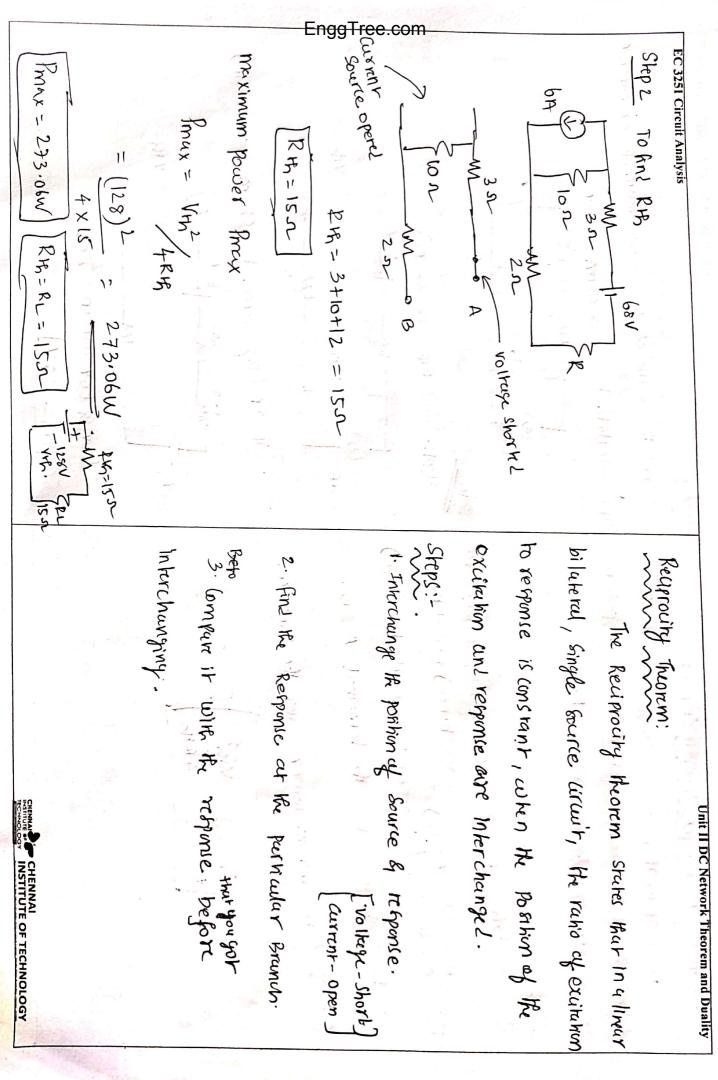


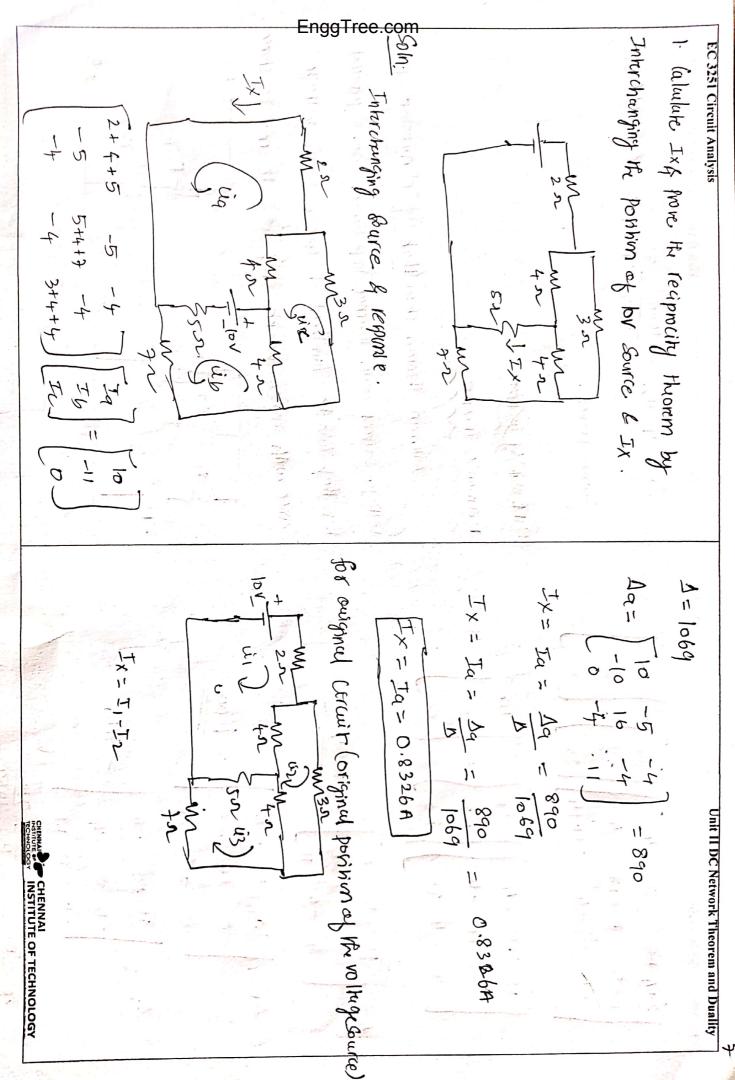


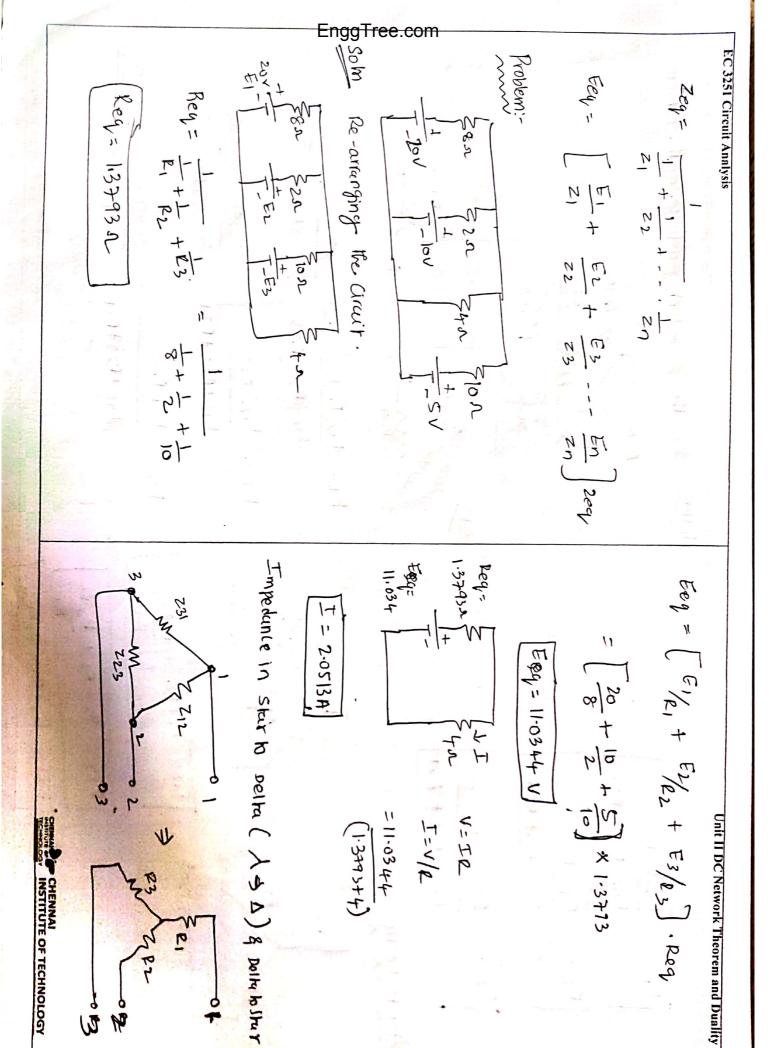






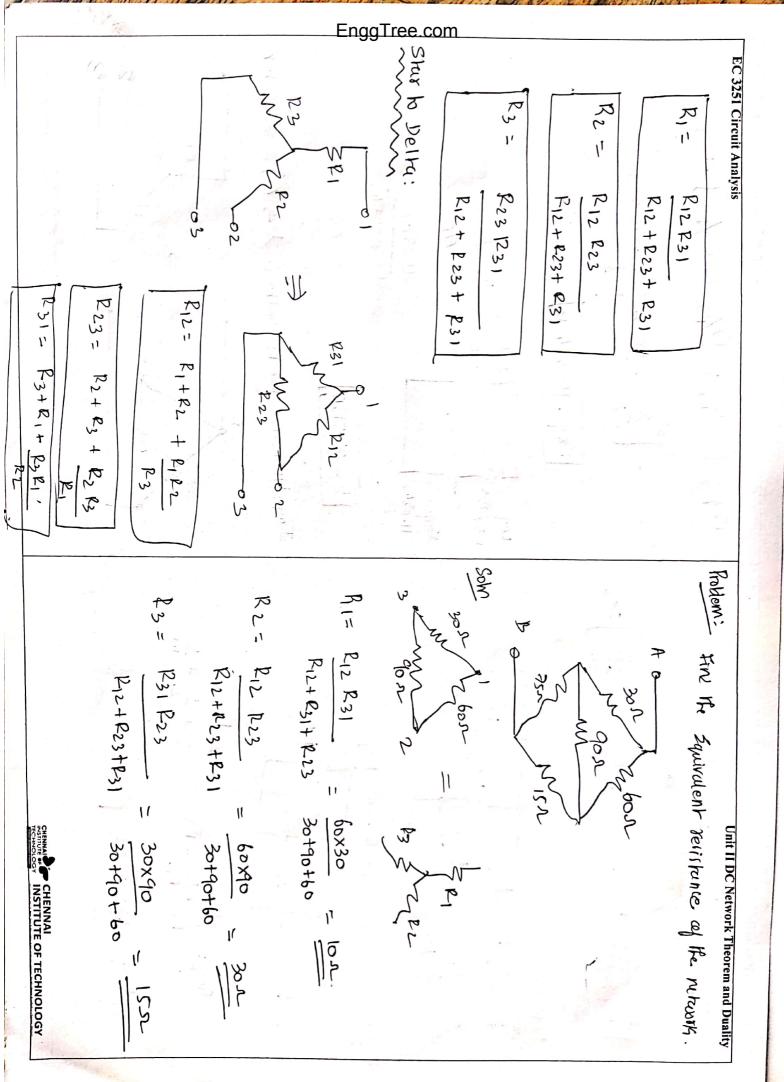


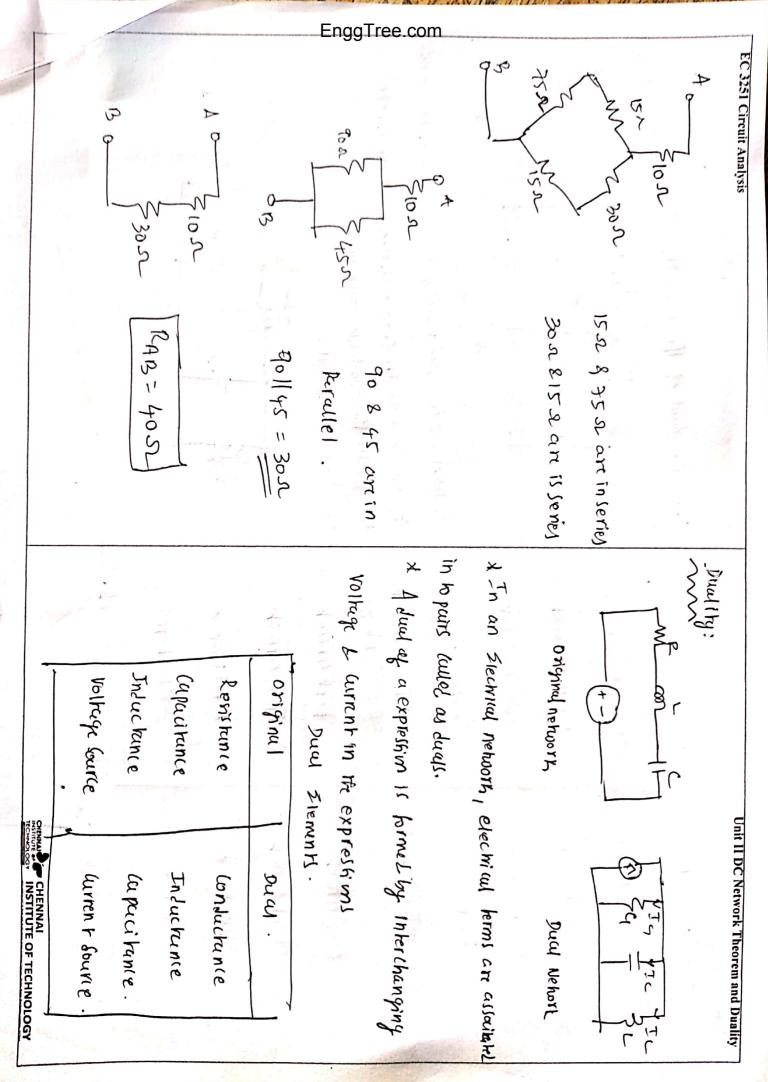




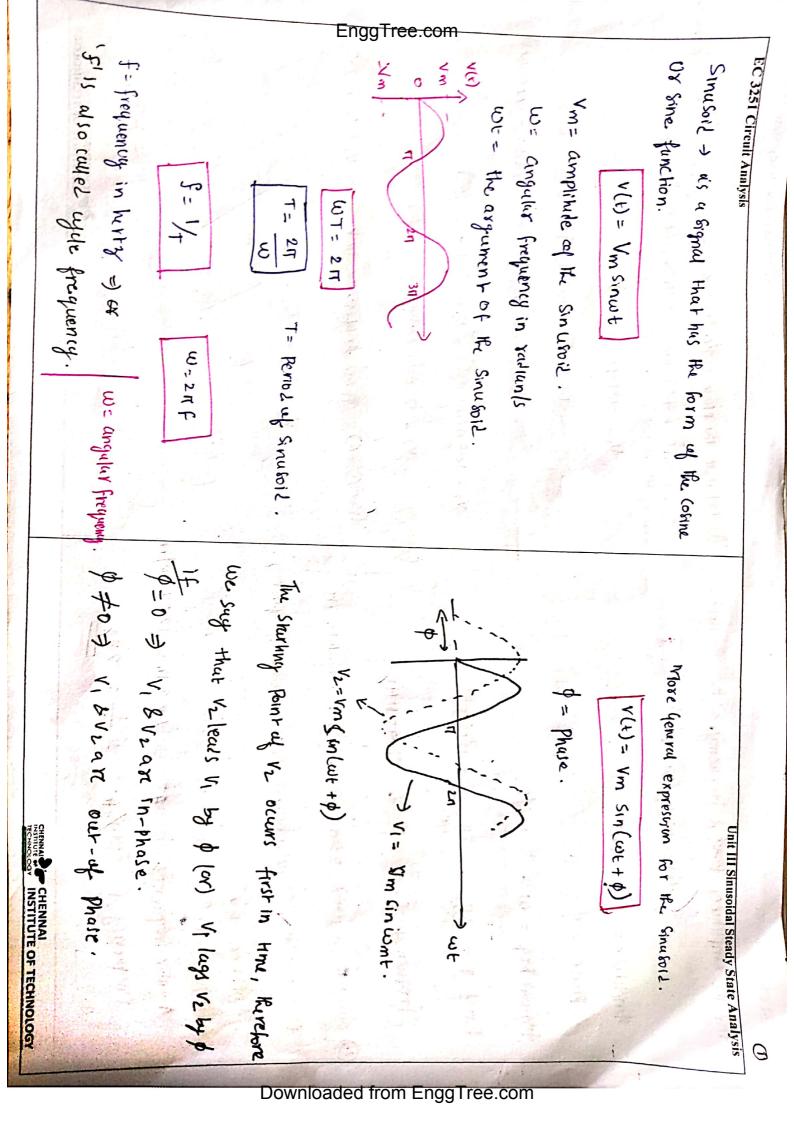
S

B





	EnggTree.com					C 3251 C
	Reachance	Short circuit Impedance	Switch closed at t=0 open aruit	Mesh equation	Current Source Sewe Branch	EC 3251 Circuit Analysis Outiginal
	sus pechance.	open circuit Admithance.	Switch operelar t=0. Short circuit	Note equation hul	Revalled Branch	Dual
CHENNAL CHENNAL CHENNAL OF TECHNOLOGY		100 Joh 32H 562	(2) Draw a dother the from each node to reference node through all the available branches. (3) Draw it Dual.	(1) label 1 & B invide loops & place reformed node outside	(204-0) A	Draw the dual of the network shown.



1) find the amplitude, phase & Frequency of the sinusit.

Amplitude = Vm = 12V

Phase = \$ = 10°

Angular my = w= 50 rac/s

Heriod $T = \frac{2\pi}{w} = \frac{2\pi}{50} = 0.12575$

frequency f' = 1 + 3.958 HZ

fiventhe Sinutal 5 Sin (4tt - 600), reducte 15

amplitude, thuse, angular frequency, period and frequency. Amplike = 5V TOWN NOTES

Phuse = -600

Angulur frequency W= ATT = 4x3.14= 12-56 racher fre frementy f = . Wen = 12.5% = 243

> 1) lululate the phase angle between V1 = -10 (os (we +50°) and V2 = 12 Sin (wt-100) State which Sinu soil is leading.

V1= -1061(w++509)

10 605 (m++500 11800)

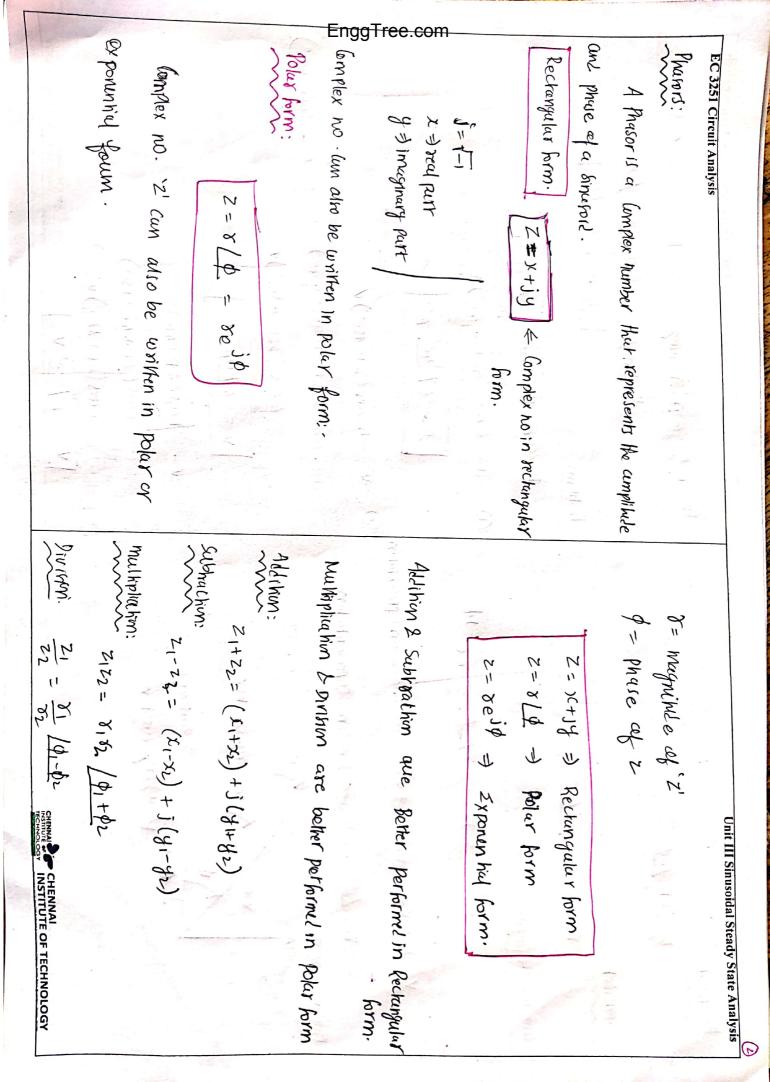
10 cos (wt-130°) (or) 42 posessionethizasos)

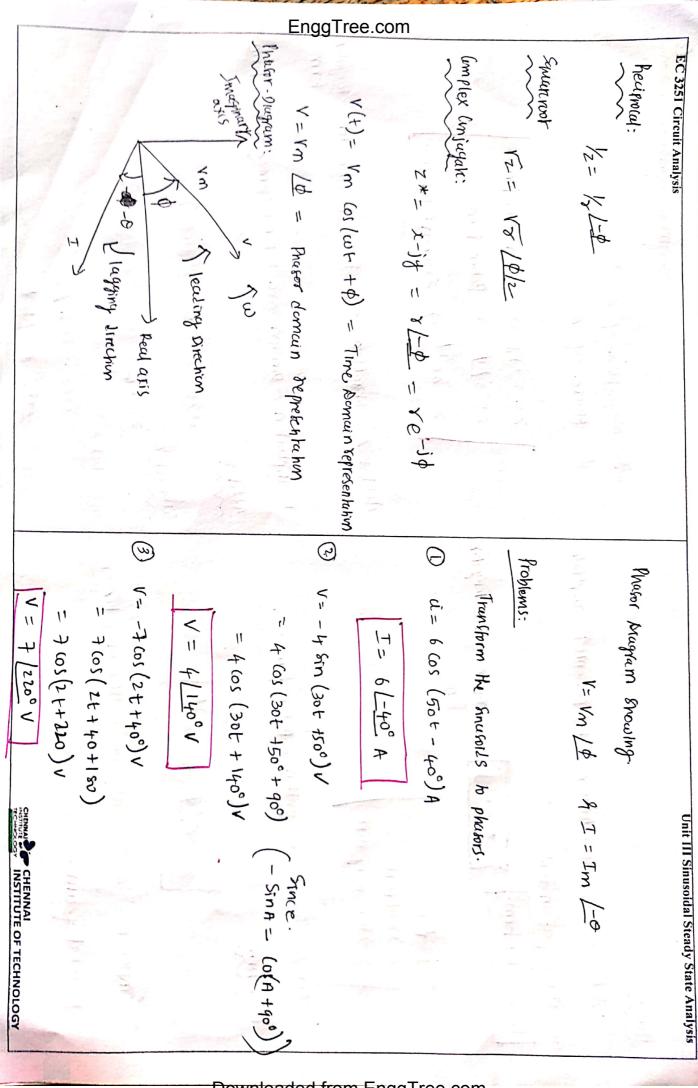
V2 = 12 sin(wt-10°) = 12 (05 (wt-10°-90°)

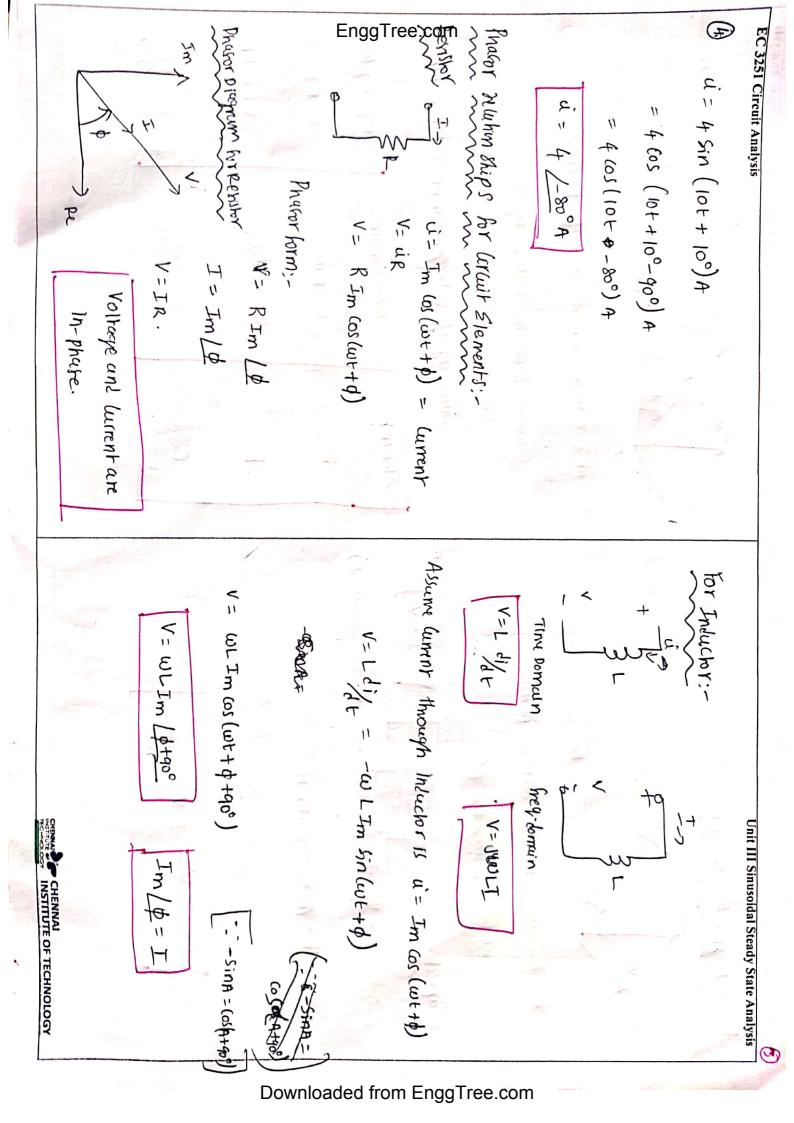
V2 = 12 cos(w +-100°) -- - (2), or

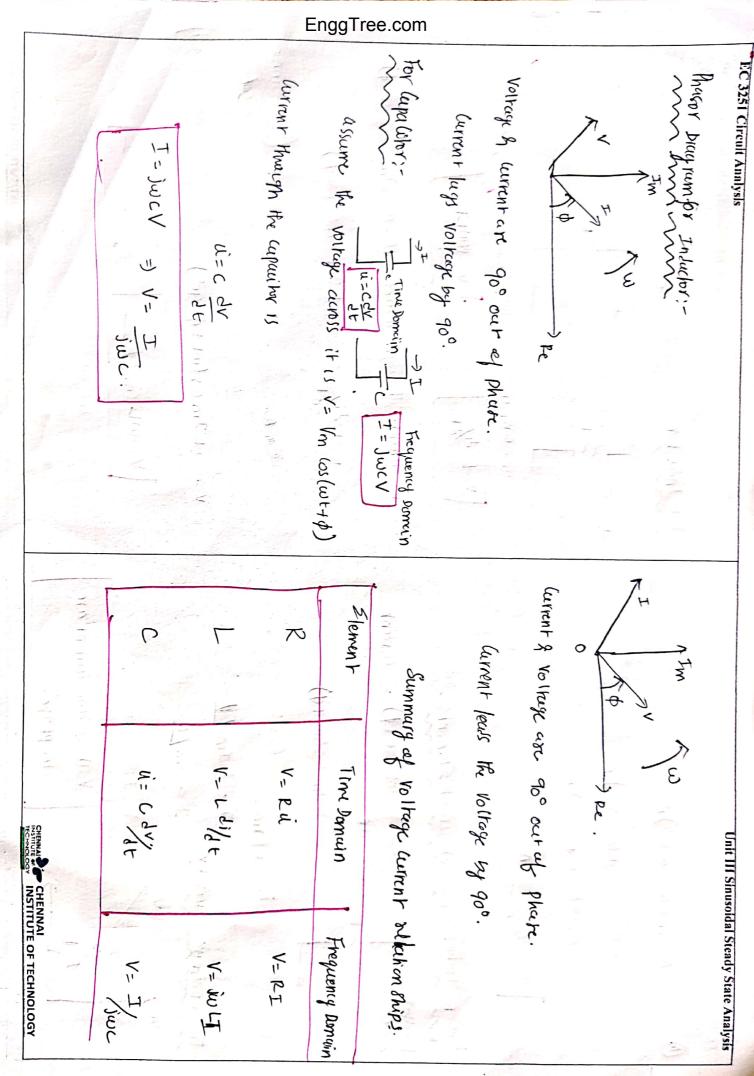
08 () may Phase difference between V, & VZ is 30°.

1/2 leass V, by 30°.









EC 3251 Circuit Analysis

Inductor, Find the Steady state Current through the INJUMPA! The volvey V= 12 65 (bt+450) is applied to a oilt

Solm V=JWLI TI V w= 60 ral/s V= 12/450 V

J60 XO.1 1 2/45°

in morning to the state of the I = 2605 (bot - 450)A 2/-450 All (1) +15

> Capacitos, Calculate the Current through 1t. If voltage v= 6 cos (100t-300) is applied to a some

Unit III Sinusoidal Steady State Analysis

V= Ijwc

I = V jwc

= 6 1-30° x 3 loox 50 x 10-6

30 los (100t + 60°) mA.

Impedance & Admittance of Russia Stements:

Element

Impodunce

2=12

t/ mithunce

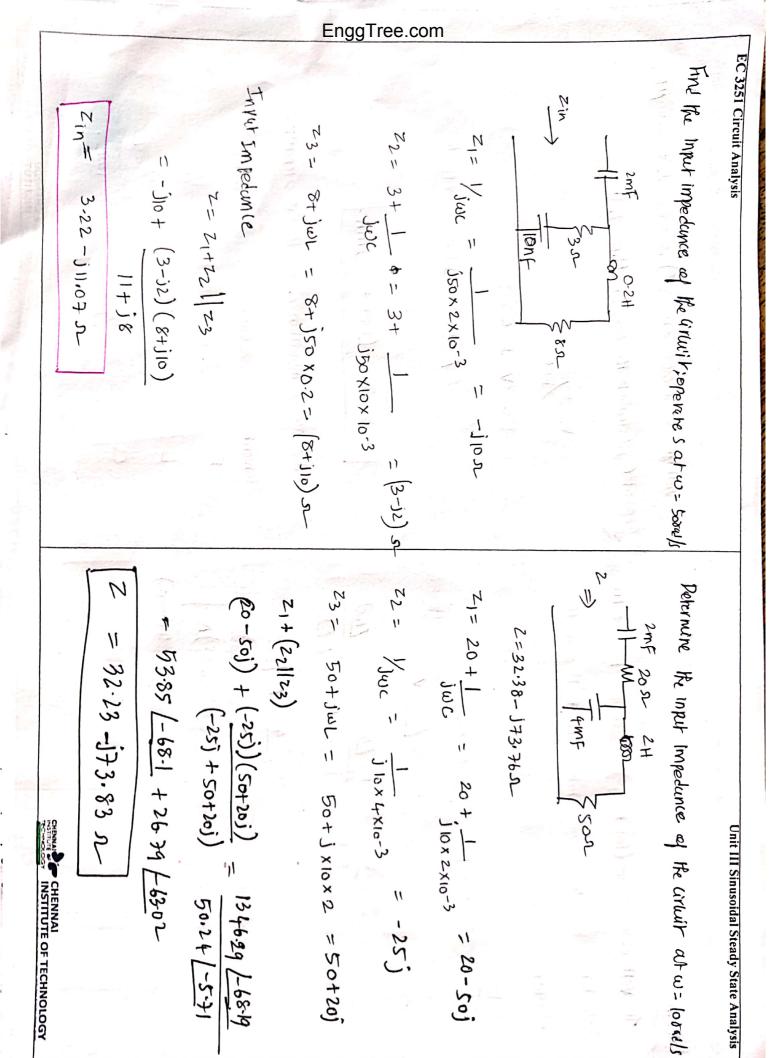
2 = 1/wc

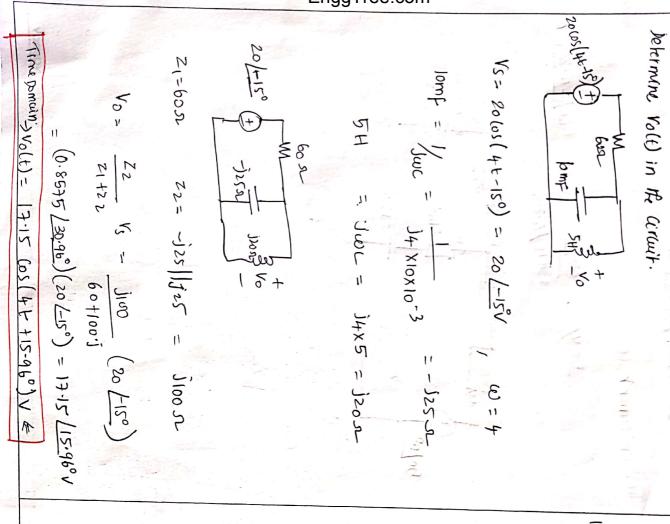
 $\gamma = j\omega C$.

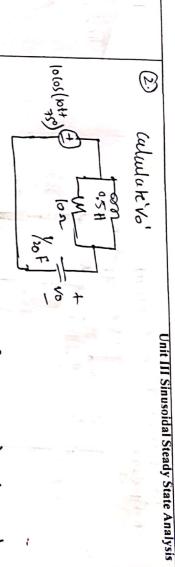
1-1/500

4=1/p

Z= jwL







EC 3251 Circuit Analysis

w= 10 rad/sec N = 10/-120 V

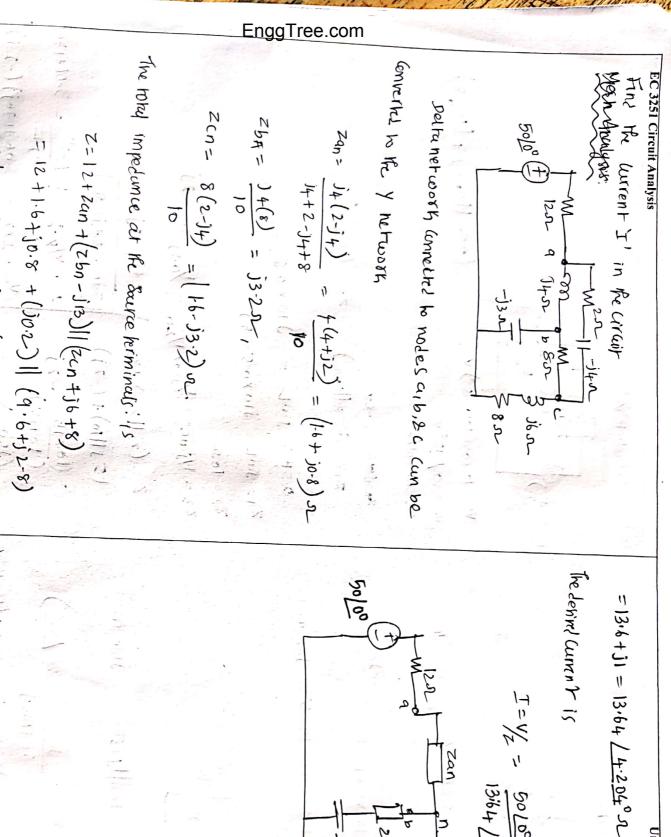
$$Z_{1} = j\omega L = jloxo(5 = 5)$$
 $Z_{2} = los$

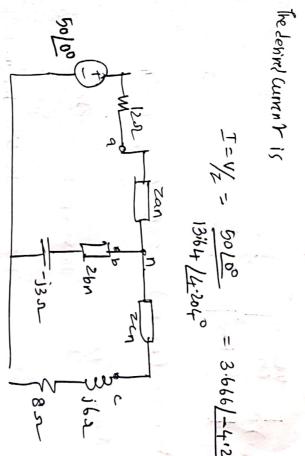
$$\frac{z_{3} = 1/j wc}{z = (z_{1}||z_{2}) + z_{3}} = \frac{1}{2}j = -2j$$

$$\frac{z}{z} = (z_{1}||z_{2}) + z_{3}$$

$$\frac{z+j_{4}-2j}{z-j_{1}} = \frac{1}{2}j = -2j$$

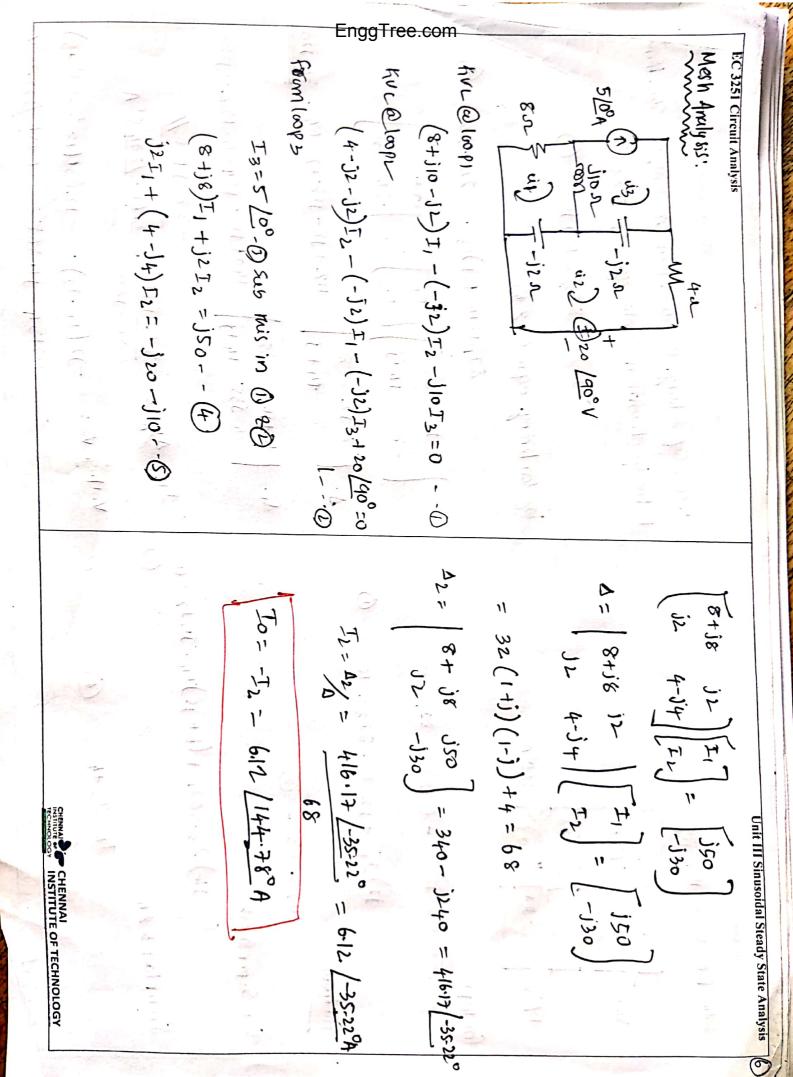
Volt)= 7-06 cos (06-600) V

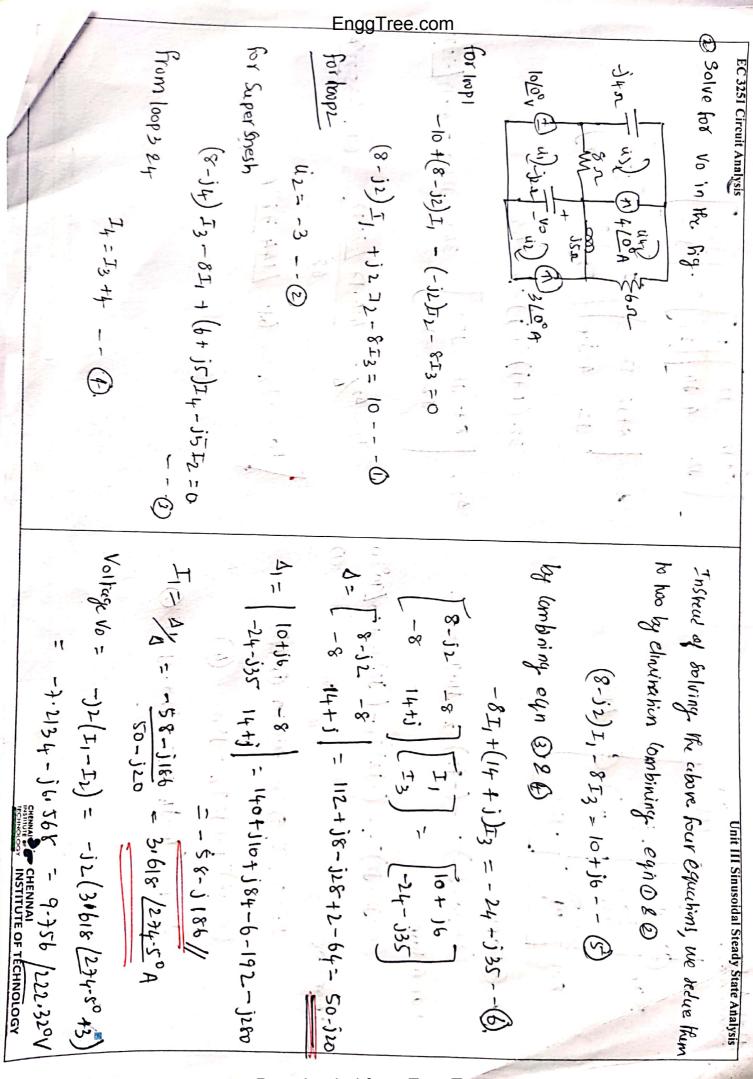


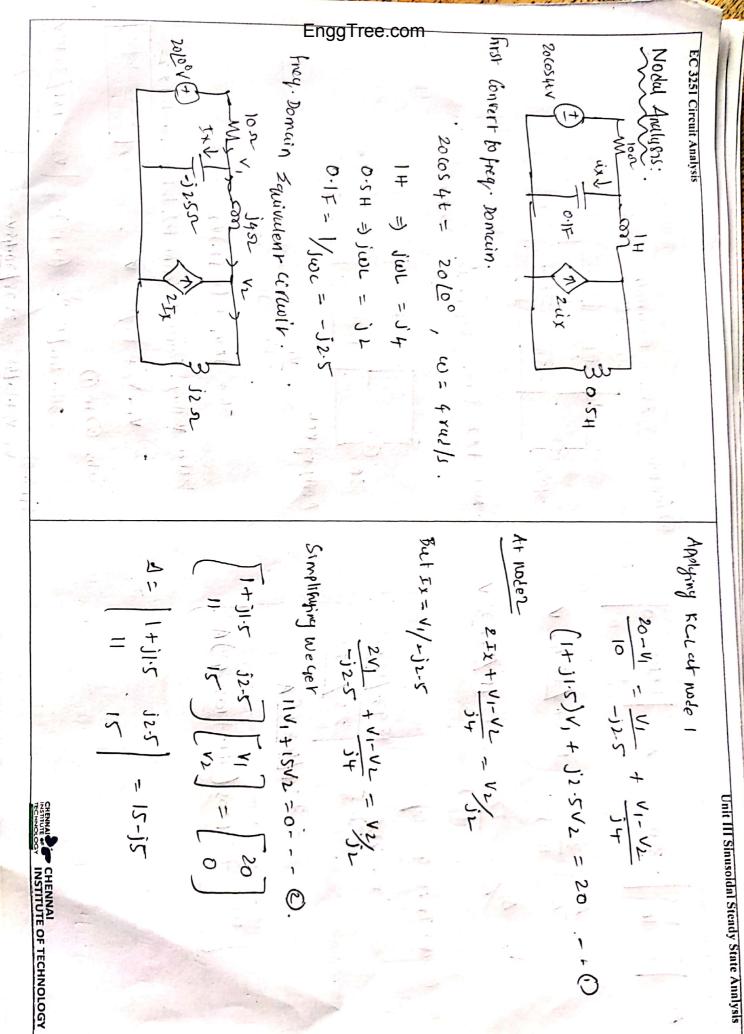


Unit III Sinusoidal Steady State Analysis

= 13.6+ jo.8 + jo.2 (4.6+)2.8)





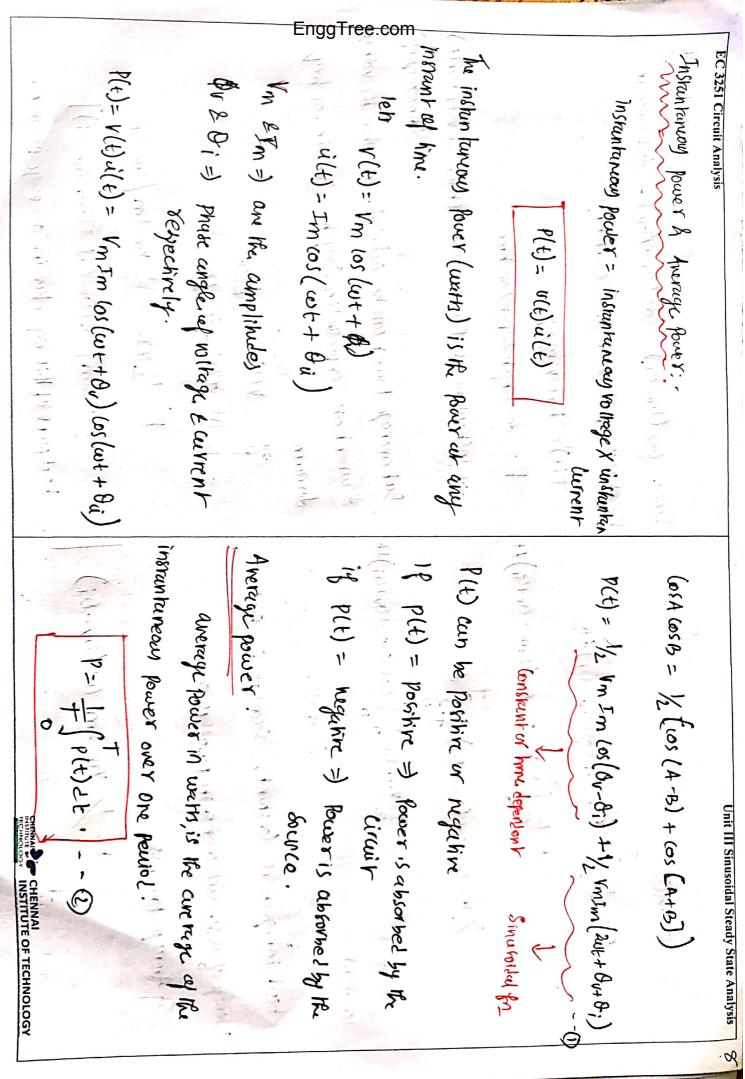


Frim 0. 36-40/1350= (1+jz)V2 / V2=31.41 /87.180V

@ (V1-V2= 10/450)

Downloaded from EnggTree.com

Unit III Sinusoidal Steady State Analysis



average of a stational over a its period 15 zero. EC 3251 Circuit Analysis Sincipit first interpant is Constant, second, is fine ford, in + 1 Vm Im +) (05 (2w6+8v+8) Ut (On: @ 2012 = 1/2 Vm Im (05 (BV x Bi) 1 1 1 dt 11 (11) P= + 12 rm In cos(Ov-Oi)dt + 4 5 = 4m Im 65 (2wt + Br+8) 1+

the phases of the vollage & current. Since 605 (By-Bi) = cos (Bj-By) = difference in & when I are expreshing frog him domain or hay But array power can be culutated in when the voltage for instruments power we must know v(t) & ult P(t) = hime varying Y = does not depend on him

(大は)一寸加し ed. N(+)= Nm/ON.

= = 1 mim [cos(0v-0;) +j fm(0v-0;)] Red purk of this equation in average power. P= 1/2 VI = = = 1 m Im / 8v-8;

So Array power is

P= 1/2 Ym Im (05 (BV-Bi)

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EC 3251 Circuit Analysis

P = 1 Vm In (05 (Ov-81)

When Bu= Bi = 0

P-2 mim = 1 tmie = 1/2/2/2

when ov-0; = 900

(Shows the circuity) Purely resistive)

P= 1 YmIm (05400=0

Shows that the arail is purely reachine. Circuit abords no emerge power

while a recurre load (Lorc) absorbs Zero average hower A resistive load (p) absors power at all times,

Pro blem

Given Kar

find the instructions power & average power V(+)= 120 605 (3) ++ 450) V 4. (001 - 1646) 500 of - (4) in

absorbed by the Pussive hear n+k.

Instantaneal power

(WALOLG = \$ (AS(A+B)+ = Vm Im (05(2W+ +0V+0)) P= Vi = 1200 (05(377+446°) (65(377)-10°)

= 600 [cos (754++ 350) + cos (3544+ 550)

344-2 + 600 65 (754+ 135°) W

are rag fower pary $P = \frac{1}{2} \text{ Vin Im (o)} \left(\theta_V - \theta_i \right) = \frac{1}{2} \left(|ie@\rangle |o| \cos \left(\frac{1}{4} - \frac{1}{2} - \frac{1}{2} \right)$

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Unit III Sinusoidal Steady State Analysis

Tem) - 2 vm Im (05 (0 v - 0i) + 1 vm Im (05 (2w+ + 0v+ 0i)) = 1 600 (05(50°) + + 600 (05(20t 0-10°) = 1/2 80x15 (05(20-(-30))+ 1/2 80x15 (05(2x10t+20-30) (2) Calculate the Instantaneous power & cevering focus p(x) = 385.7 + 600 (20+-100) W aborded by the passive linear note. EC 3251 Circuit Analysis cill) can be written as ult) = 15 cos (10+460-900) V a(t)= 15 sin (10+ 400) u(t)= 15 (05 (10t-300)V V(+)= 8010s (10++200)V Bary = 37.24W (3) Calculate the average power absorbed by un Impedance Pavg = 1 mm m (0s(Bv-0i) = 1 (110) (1.576), (0s(0-66.80) Cat WAR Show STORY DELIVER (COM C) COME THE STORY OF THE POST OF THE 27720-1702 when a witage V=120100 is applied across Arefuge Power Pary 7: 1/2 - 120/0° - 120/0° = 1.596/66.8° A Parg Pavg = 1 vm Im (05 (Bur-Bi) 1 x 80 x 15 (05 (20-(-30)) 385-7W 600 (cos (so)) CHENNAL CHENNAL INSTITUTE OF TECHNOLOGY

Unit III Sinusoidal Steady State Analysis

(4) A current I = 10/20 flows through an impolance 7 = 201-22° 52, Find the average power delivered to He impodunce. V= I.2 = 10/20° x 20/-22°

EC 3251 Circuit Analysis

Ray =
$$\frac{1}{2}$$
 Vm Im (os ($\theta_V - \theta_i$)
= $\frac{1}{2}$ x 200 x 10 (os ($\theta_V - \theta_i$)

we deliked be foug =
$$\frac{1 - 5/30^{\circ}}{4 - j2} = \frac{5/30^{\circ}}{4^{\circ}+32/-26.57}$$

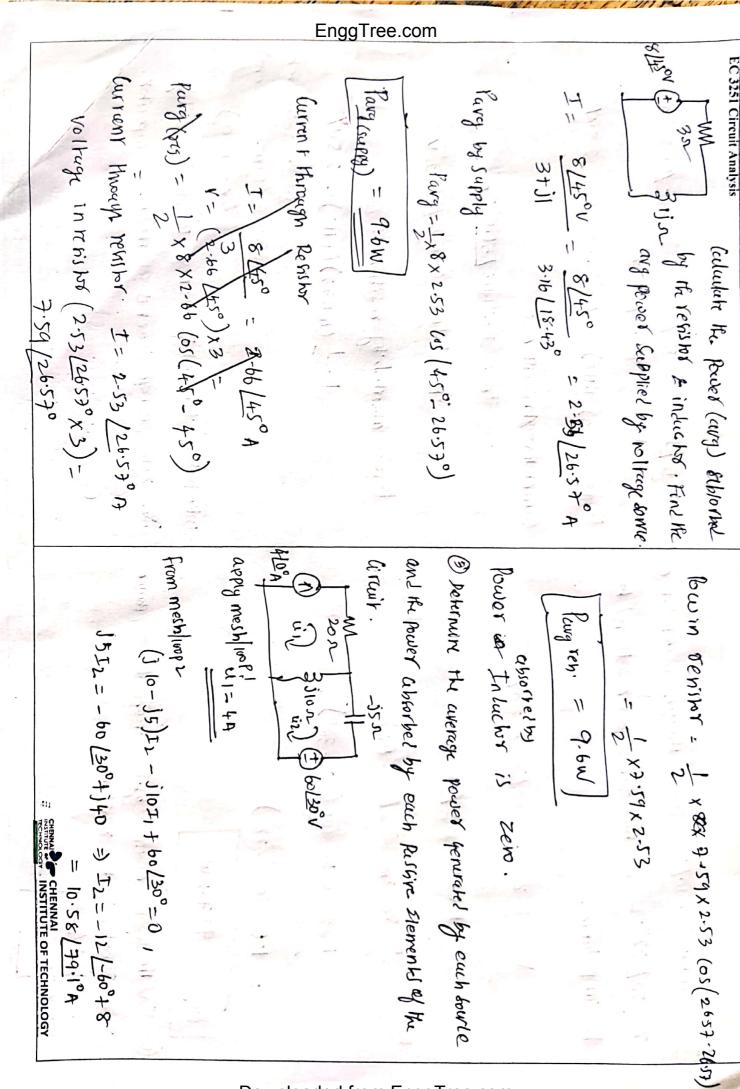
lowerd absorbeb by rehisher is

voltage & current is zero (Since phase diff bet

(Br-8)=0)

Unit III Sinusoidal Steady State Analysis

1.118 156.57°A



Unit III Sinusoidal Steady State Analysis

for the voltage source, the airmst flowing from it is IL

72=010.58/29.104

& volkage is 60/30°V so ung power 13

B= 1 (60) (10.58) (05 (30°-39-10)=

= 207.8W

Thus any power is absorbed by the source, inview

EnggTree of the direction of IL & polarity of the voltage Source the Chris delivering average power to the voltage

for the wornt source: In= 4/00. The Control of the Co

V= 20 I, + 110 (I-1-IZ) = 80+ 110 (4-2-110-39)

= 183.9+j20. = 184.984/6.21°V

The one former supplied by the Germant formers

Unit II DC Network Theorem and Duality

P1- - (184.984) (4) (05(6.210-0) - -367-8W

negative sign indicates the action to source is supplying

buer to the circuit.

FOR the reasons the went through it is II-4200

Vollage across it is 20 I1 = 80/00;

R= 1/80)(4) = 160W

For the lupuitor, the current though it is IZ=10.58/79.10 & the voltage amoss It is & -15I_- (5/-900) (10.58/391-10)

= 52-9/79-10-90°.

and power absorbed by lapacitoris

Ph=1/2 (25-4) (10-28) (05 (-900) =0

Indutor, lurmoris (-II-IL) = 2-j10.39 =10.58 1-39.10 CHENNAL CHENNAL CHENNAL OF TECHNOLOGY INSTITUTE OF TECHNOLOGY

vollege across inis 10(II-II) = 10.58 /- 29.1 +90° EC 3251 Circuit Analysis Hence the average power absorbed by the inductoris

B= 1 (105-8)(10.58) (05 40°=0

Notice that the inductor & the lapacitor absorb zero

the lurrent source equals the power absorbed by the arrivage power and that the tot. Dower supplied by dehiber & the voltage burce or

indicating that power is conserved. P1+P2+ P5+P4+P5= -363-8+160+0+0+0+207.8=0 at No Wage and lument.

Effective of Pms value:

of lument that delivers the same average Rower ba refisher as the penietic lurrent. The effective value of a periodic current is the

Jeff = Irms

Veff = Vams

MY = SURRY

Irms= Im

Unit II DC Network Theorem and Duality

average power law be written in terms of sms value

Vrms

P- I'ms R =

Apparent Power & Power Fuctor:

Apparent power (in va) is the product of the smillalle

Power fuctor: - Ratio of supposemble power to apparent lunity (volt-Amp)

 $P_f = \frac{\rho}{S} = (os(\theta_v - \theta_i))$

Power

Ov-8: = Power fuctor angle.

Wilruge & Lurrent, Itis also the Change of Technology INSTITUTE OF TECHNOLOGY Yower factor is the worker of the Phase difference between

apparent power & the power fuctor of the load, Dokermin when the applied voltage is v(t)=120 cos(100 nt- 20°) V, him the EC 3251 Circuit Analysis

the element values that form the Sevies - compacted laid.

APPRIRENT POWER S= Vrms Irms 120 4 = 240 VA

Rower Fuctor 75 = cos(ev-8,)=

Z=1/2 = 120/-20° = 25-98-3152 = (05(-20-10) = 0.866 (realing) (Remove turnnt leass voitage)

Pf = (05(-30°) = 0.866 (reality)

load impedance Zlan be nodeled by a

25.982 refish in Jeries with Capacital

xc=-15 = -1/wc = 1/2×1000 = 2122M F

1) A Series - Connected load draws a current alt) = 400 (14011+100) (2) Obtain Bower factor & the apparent power of a load whose impadance 15 Z= 60+j40s- V(t)=150(05(3>)++10°) Unit I DC Circuit Analysis

Approximation services:

I(+)= V(+); 150/10° 60+j\$0 72-11/33-69

T(x) = 2.08/-23.69

S= Vams Irms = 150 200 = 156VA

Pf = (05(0,-8;)=

= los(10+23.69) = 0.832 (1495.ng) (Become winn't lays volkage)

EC 3251 Circuit Analysis

Complex power: In (VA)

Complex conjugate of the sons current that, Asa complex munify in seal part is seal power (p) & in Imaginary part is mative power 9: is the product of the sms voltage phasor and the

Complex power = S= p+ja = 1 VIX = Yams Irms / By - B,

APPARNY POWER S= 151 = V8ms IVMS = 1 P2+9 L

Red paner = P = Pe(s) = \$ cos(Bv-Bi)

Reachire power=9= Im(s)=Ssin(dv-di)

Problemi

Rower fuctor = P = (05(0v-8))

Unit I DC Circuit Analysis

The voltage across a loadjult) = 60 Eas lut -100)V

ab the volkey drop is a (t) = 15 los (ω+ +50°) A and the lurent through the element in the direction.

(a) lamplex & appurant powers

6 real & reacher power

(c) Power fuchor & the local impredance

Vims = 60 L-10° Irms = 45 /50°

Complex Burer = 45 /- 60° VA Nams Irms (60 F100) (1.2 7-200)

complex power =

Apparent power

S= |S| = 45VA

CHENNAL OF TECHNOLOGY INSTITUTE OF TECHNOLOGY

(b) we can express the complex power in reldangular form While reaching power is S= 45/-60° = 45 [los(-60)+jsm(-60°)] Red power P= 22.5W Since S= Ptjg , the real powers

EnggTree.com = 22.5-j38.97 Ø l 38.97 VAR

40/-600 real power Complex power in sectangular 15.04+ J41.3 W S= P+jB 15) - 44 VA

 $z = \frac{T}{V} = \frac{60\sqrt{1-100}}{100}$

1.5/+500

1) for a low Vrms = 110/850V, Irms = 0.4/150A Power, reaching power, power factor & load Determine bomplex power, apparent power, real Imperunce.

Complex power S= Voms Irms*

= 110 85° × 0.4 10° / 12°

44/20° VA

Appurent power:

The power factor

Pf = (05 (-60°) = 0.5 (leading)

Ked Power P= 15-04W

Reaching power 9 = 41.3 MAR

Bower Fricher

$$Pf = los(\theta_V - \theta_1)$$
 or

Pf= (05 (0)

from lumplex

Nowe T

= (os (85-15)

Impedance.

@ for arbord, trass = 110/8504, I mas - Or4

(3) A lour Z draws 12 KVA ata P.f. of 0.856 layoning from a 1201 rms finatoted Source, Caludate the average & reactive power sietword to the load,

Power angle as 0 = (05-10.856 = 31.130 firm that PF = LOSO = 0.856, we obtain the

(b) Real lurent and the () load Impedance.

If upparent power is S = 12000 VA the average

or real power is

P= S(0 SB 12000 x 0-856 = 10-272KW

while the Refishing pawer is

9 = Skin8 = 12000 X0.517 = 6-204 KVA

(b) since the PS is lagging, the Complex power is S= Ptjg = 10.272+j6.204 KNA

From S= Voms Irms

4004 +242101 Pal 120100

= 85.6+j51.7A

= 100/31.130A

Thus Isms = 100/-31.130 & the Peak Current is

Im=12 Irms = 12 x100 = 141.4A

The loop impedance

which is an inductive impedance.

Z= Vrms = 120/0° =

= 1.2/51.130

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UNIT-4

TRANSIENTS AND RESONANCE IN PLC CIRCUIT Here We will examine two types of Simple CIECUITS:

-> A araut Comprising a resistor and Capacitor

> and a circuit Comprising a resister and an

There are called RC and RL.

The Source-free Ac Circuit:

HA Source-free RC Circuit Occurs
When its DC source is subbonly dusConnected. The energy already Stored in
the Corpositor is released to the
resistors.

-> Consider a Series Combination of a series consider and an Intially Changed Capaciton.

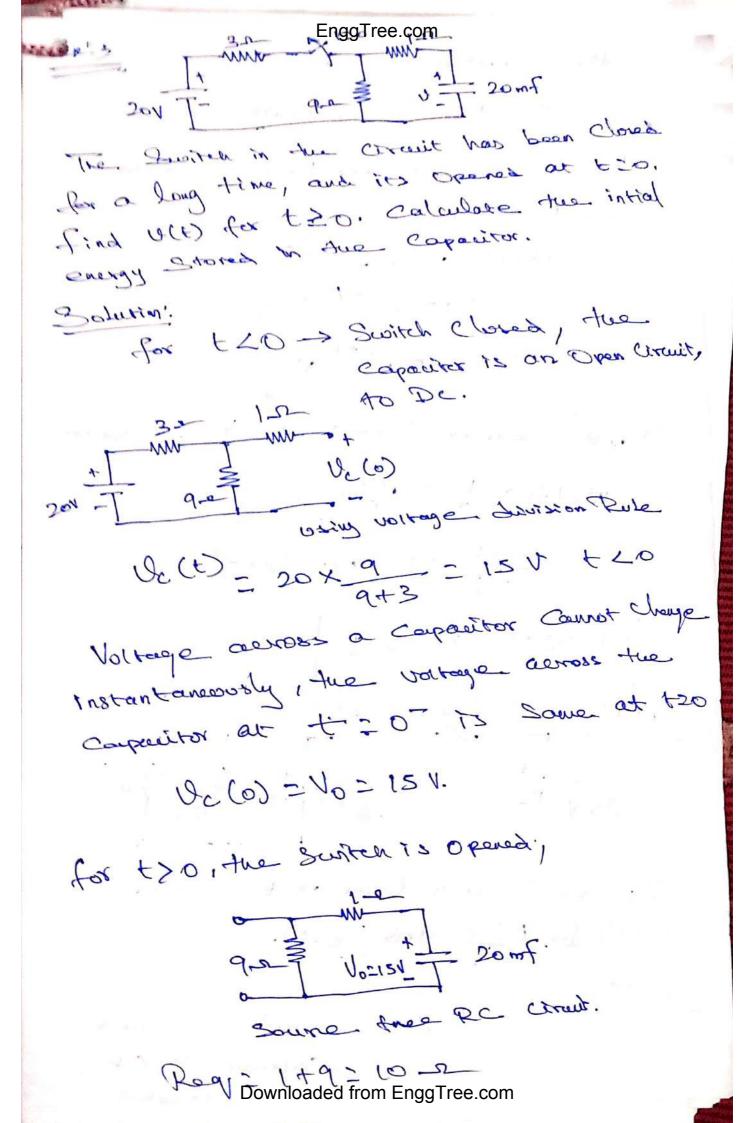
IC T VO MR

→ Objectue is to determine the Gravit response, assome to be the voltage (IE) across the capacitor.

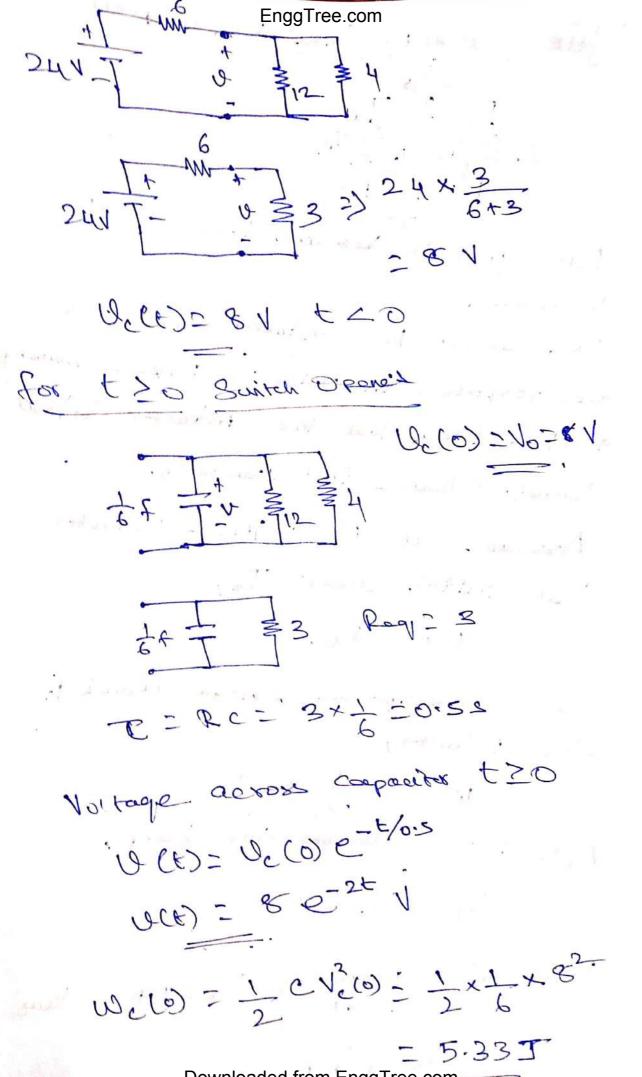
Sine capacitor initially charged, whe can assume that at time tio, the initial voltage TS,

U(o) = √o EnggTree.com Wen the Comerpoiding Value of energy stones 10 co) = = = CV Doplymy ICCL at the node of the Chronis, ic + ir=0 We know that icicdo and ix= 12 C dv + 9 =0 by reamongly du = - Tedt Integrating both Sides. In 0 = - t + ln A A > integration constant, thus, Taking Powers of e produce U = e-t/RC 1. Jet = AetlRC at initial Condution I(0) = A= Vo

This Shows - EnggTree.com the RC Crouitr is an exponential decay of the mitial Voltage. The Resoponse is due to the intal early stored our the physical Characterities of the Circuit and not due to some External voltage or current Source, it 15 Causa tue returner response of the Circuit. from the graph, As t- increases the Voltage Larcosas toward Zeno. The rapidity which the voltage decreases is expressed in terms of tue time Constant (T). that, t=Z tuen V(t)= Vo et/RC Where T=RC TV(+)= Voe- 1/5/2 Voe" 20.368Vo In terms of time convent

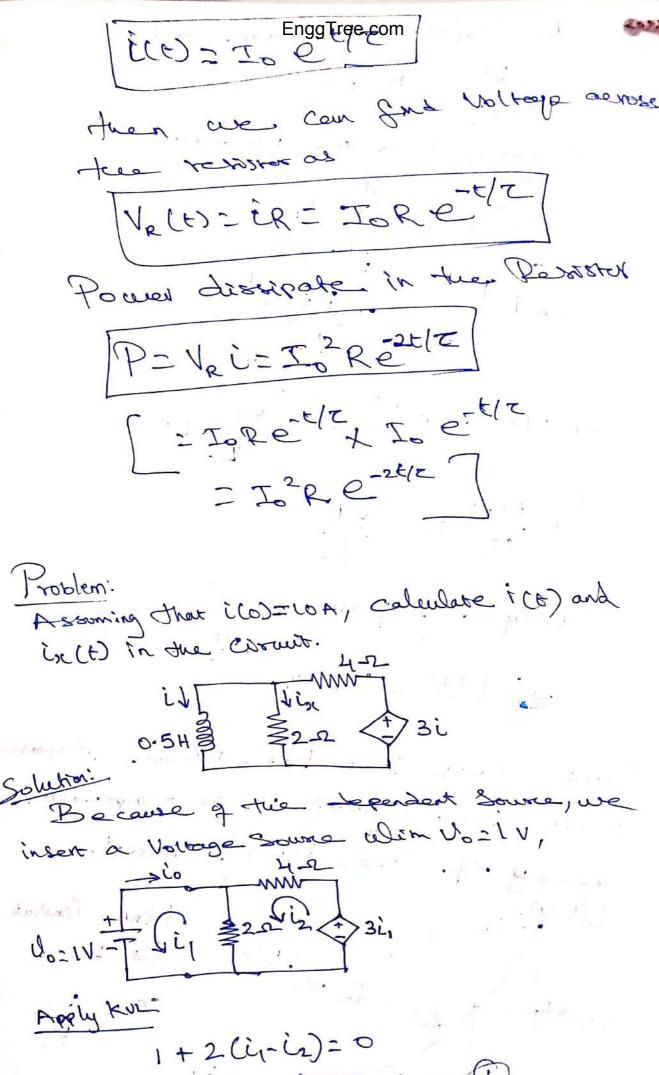


time Constant, T = Roy C = LOX 20X10-3=0.2 S the Voltage across the Copacitor for t 20 12 U(E)=1, (0) e-E/2 215 e- 10.2 V (J(E)=15.e=5EV Initial owingy Stones in the Corporita is Weld = 1 C 12 (0). = 1 x 20 x 10 3 x 152 Wc(0) = 2-25] 24 V T-If the Switch Open at 120, God U(t) for t >0 and we (o). Julia! for ELO -> Switch Closed Conpuestor or Open



Source Enggtreetcom? L. CIRCUIT Leve RATUR Our goal to desenire tue Circuit (Sorbanso. We Salast the Monetor Coment es the response in order to take abundage of the Tobea that the industrier Comment Course Change instantaneously. Desome at the themeter has notial Current Io, C(0)= Io. tue Comerpudiny, Racingy Stored A tue induster, w(0)= 1 1 I2 Apply KUL amount tue Loop, V, + VR =0 but., Wiz Ldi. 7 VRZCR, tens Ldi + Ri 20 Downloaded from EnggTree.com

for SimplificatinggTreescoming by L di + R c=0 Reamonly terms are intergrating giver $\int \frac{di}{t} = -\frac{t}{R} dt$ In i] [(+) = - RE] t ln c(t) - ln Io = - Rt +0 In E(F) = - RE Taking e power - RYL - RYL This Shows that the natural response of the RL Circuit 15 on exponential Locary of the Mittal Current. . time Contract To ette for PL Downloaded from EnggTree.com



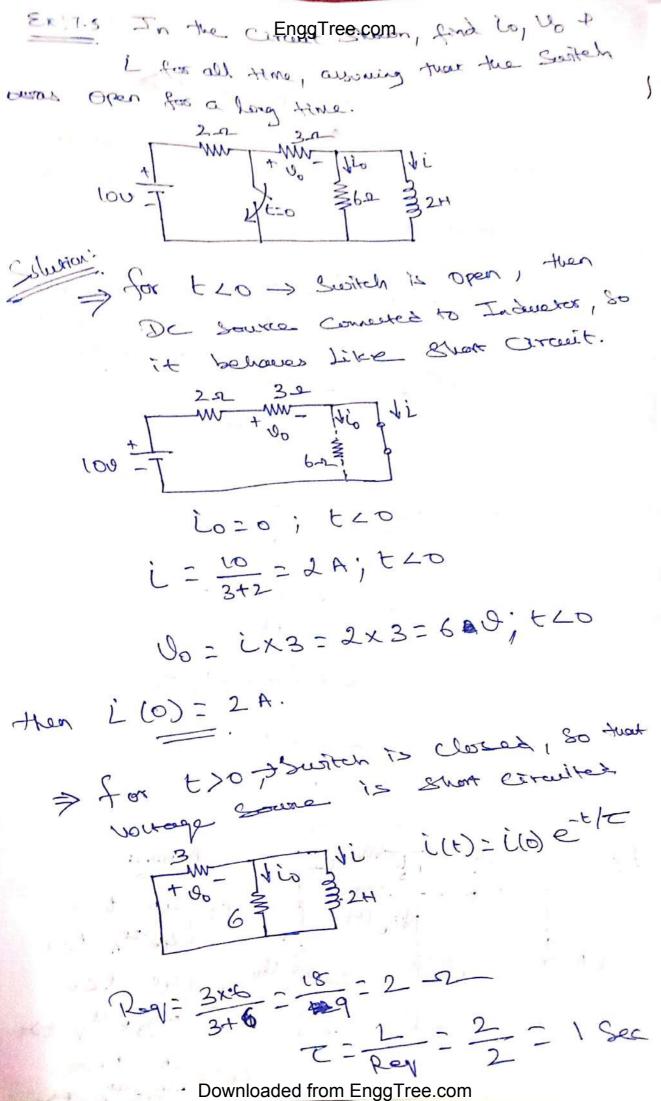
4 6 + 2 (12-1) EnggTiree.com 41/2+21/2-21,-31,=0 6 iz-5 iz=0/2 22,-22=-1 L2 = 5 in Sub iz Naturiar = 2 -2 = 12-10=2 $2i_1-2(\frac{5}{2})i_1=-1$ $2i_1-2(\frac{5}{2})i_1=-1$ -. Lo=- L1=- (-3)= 3A -. Rey= Ron= 10 = 1 3 then the time Constant is T= = 0.5 Rey = 1.58 the Cumant strongs the inductor is, i(t)=i(o)et/c=10e-t/1.5 A +>0 Voltage across the inductor is 0=1 di = 0.5 d 10e- Elis = (0.5)(10)(-1.3) e-+11.5 V Z-3.33 e-t/1.5 M

Since inductor of the Engalmee.com of tenstor are in the Dovallel, ERZ: find i and Vx in the circuit in figure, Let (6)=5A Craven: i(0) =5 find: L and Voc from food Deal , Apoly KNL -1+34+1(iriz)+21/x=0 41,-12+2(32)==-1 102,-12=+1-0 LOOP 2 1[i2-i]+5i2-21x=0 12-4-512-2(34)=0 6i2-7i,20

EnggTree.com in the Switch in the circuit has been closed for a long time. At \$20 the Switch is Opened. calculate 1(1) for 6>0. \$12 \$16 \$ 2H Solution: at t<0 > Switch closed, Inductor act as Short Circuit. 7 16 en Resistor is Shor Circuited. 201-T = 3-2 21= 50 = 8 A and i(t) Obtain by Current Livian rule ict) = 8 × 12 = 6A t < 0 Strea Convert through an inductor Cannot Change instantaneously. 0== t = (0) = (0) = (0) = (0) = when t20 -> Switch Opened, voltage Source dis Connected.

Source free RL Circuit = 16x1P = 8-2 · time Constant Thees i(t) = 6 e 4 20 28 D 20-24 A

i(t) 3 5-0



EnggTree.com ict)= 2et A at t>0 Need to find to 1.e. current though 6-se by Current Livisian Rule, is or is=(-2e-t) x 3 [i(t) is revene when Lo(+)= 2 et A 00(t)= 02= 2 di = 2 x d(-2e-t) = 2x[-2(-1)e-t] = 2 x 2 e-t 00(t)=4 e-t V 12 00002 i: Pha tho 120 14 the 2th the 21 = 4v tco Downloaded from EnggTree.com

EnggTree.com

UNIT STEP LONCTION:

The Unit Step function alt) is O for Negative values of t' and I' for positive Values of t'.

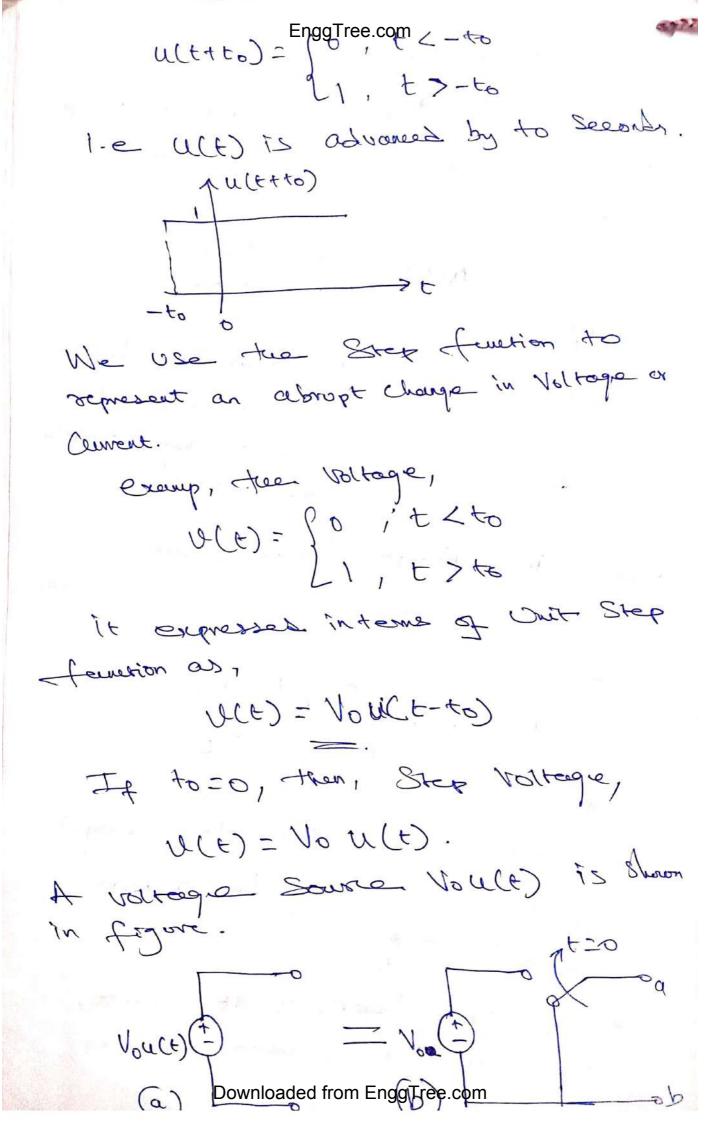
> If the abropt Changes Oceans at t=to, then the Out Step function

becomes,

$$u(t-to) = \begin{cases} 0, t < to \end{cases}$$
 $u(t-to) = \begin{cases} 1, t > to \end{cases}$
 $u(t-to) = \begin{cases} 1, t > to \end{cases}$

that $u(t)$ delayed by to Seconders.

If the change is at $t=-to$,



from the figure (b) it is evident that terminals a-b are Short Circuited Uno for t<0, and Un Vo at teminals for t >0. Studenty, a Current Source of Iou(+) TS Shown in Joque, (a) from From (b), Norice & that teminal a 4 b Open circuited (=0 for t20, and i= Io flow for

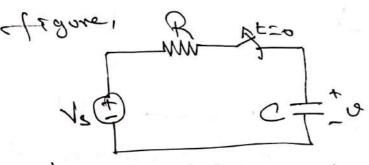
七>0.

STEP RESPONSE ENGETTEE COM RC CIRCUIT

When the dc Source of an Ac Cermit
IS Suddenly applied, the Voltage or
Current source can be modeled as a
Step function and the response 12
Known as a Step response.

of the Step response is the response of the circuit due to Suddon application of a de voltage or Course.

- Consider the RC Cercuit Showen in



Which can be replaced by the

Vsu(E) (*)

Vs -> is a Constant de Voltage dure Assome an initial Voltage Vo On tree Capacitor, tree voltage on tree Capacitor Count change motantaneously,

1(0-)=1(0+)=10

Apply KCZ, LR+ Lc = La R+Cdy= Vsuce) R-Vouce)+cdv =0 U-150(6)+C 21 20 divide by "C" U-Vouce) + dv =0 dv + U = Vsu(e) Whene I is voltage across capacites at t>0. So UCE)=1 at t>0. dy + 9 = Vs Dearroughy tems, dv = - [U-Vs] dv = - dt 11-v. = RC Integrating both Rides Juck) = 1- 90 Downloaded from EnggTree.com

EnggTree.com It we assome capacities is Orchanged initially Vozo, so the equation becomes, U(t): 0, tx0 Can be contren alternatively as, (UCE) = Vs (1-e-+/2) ult) This is the Complete Step response of the RC Chronit when the Comparitor is initially Orcharged. > The Convert through the Carponier is Obtained from above equation, by oring ICE) = Cayle, [(t)= cdv = cdvs(1-e-t/2) u(t) T= RC +>0, U(1)=1 [(+)= (C)(1)[-(-+)e-+127 では)=こりをして ((t) = V= e-t/z ult)

Complete Response - Natural response + ferced
(Stored energy)
(independence) Rasponse (independent Sura)

Complete Parporse: Transient Laponse + Steady Stake
(Lemporary port) (parmount part)

Natural Rasponse = Transient Rasponse forced Furposse : Steady State Dasponse

Demplete Parpoise May be committee as,

U(t) = V(0) + [V(0) - U(0)]e-t/T

UCOD -> initial voltage

U(a) -> final or Steady State Value.

To find Step Rosponse of an RC analt Dogumes twee things,

1. The withol Capacitor Voltage, U(0). the

2. The final Constant T. The time constant T.

Ex: 1 The Switch in figure has been in position A for a long time. At t=0, the switch moves to B. Determine Olt) for the and Calculate its value at t=15 and les. SKA UTT O.SMF T-30 V For too > Switch is at position, A. spould outs like Open Circuit. 2HV-T SKE TO.C Voltage auross Ste is Using vortage division Rule 0(0-)= 24 x = = 151 the capacitos voltage comot chaye mountomounty, So, 0(0) = 0(0) = 0(0t) = 15 V t>0 -> Switch is in position B', 4 0.cl 7-300 Rtu=4k-2

٨

Hime Constant,

T: Rmc = Lexios x O. Sxlo = 2 2 2

-> the capacitor acts like Open Chruit,

to de at Steady State.

1(00)= 30V. t>0

Thur,

0(4) = 1(a) + (v(o) - v(a)) e-t/2

= 30+[15-30]e"0.5t

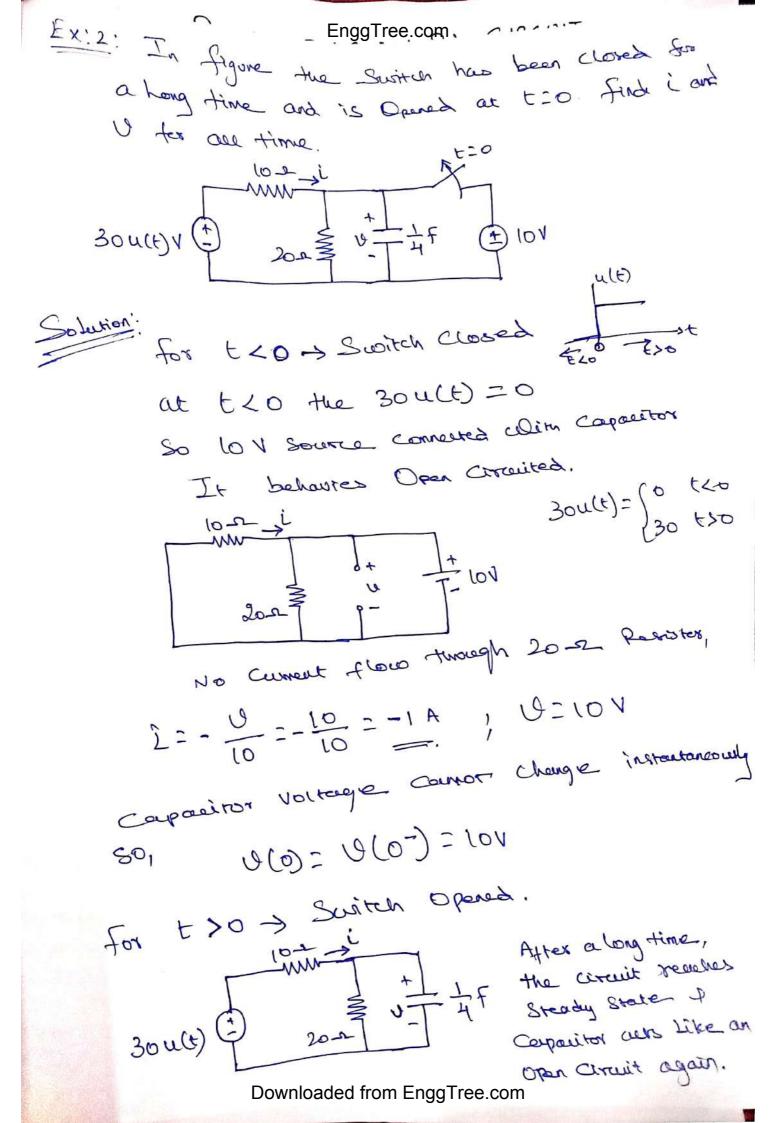
UCF) = 30-15e 0.56 V

At 5=1

U(1) = 30-15e = 20.9 4

At t=4,

U(4)= 30-15e-2= 27.97 U



Steady State bloge, U(a) Obtain Umy Vollage durision,

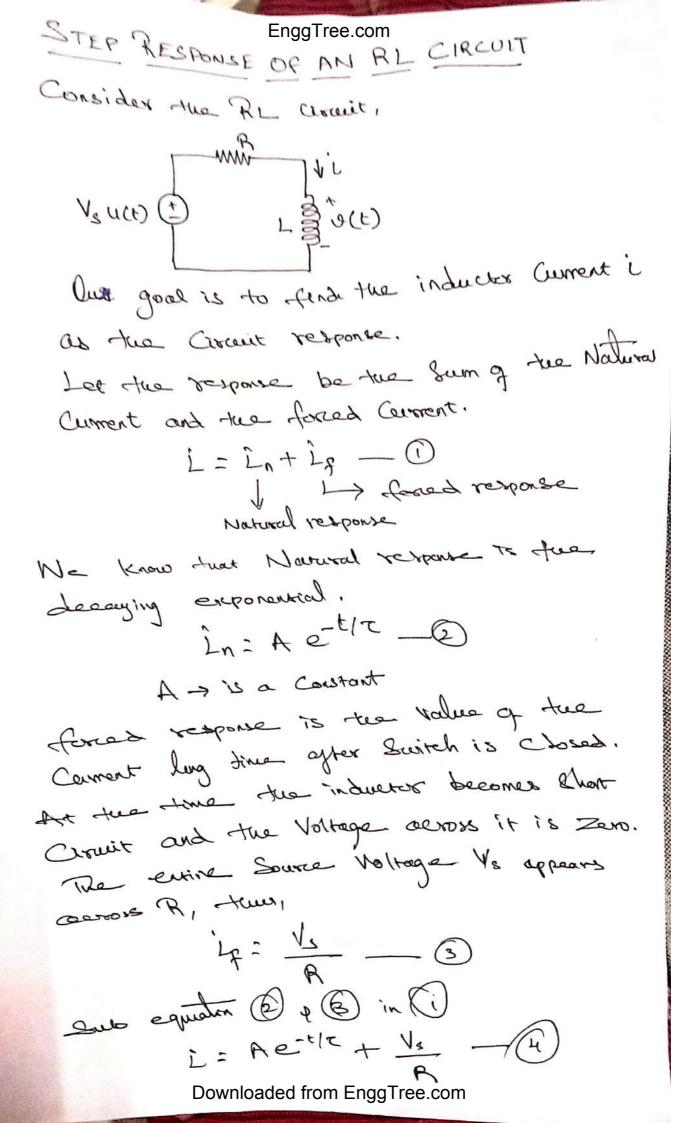
Finds Rom by,

time Constant,

Theis,

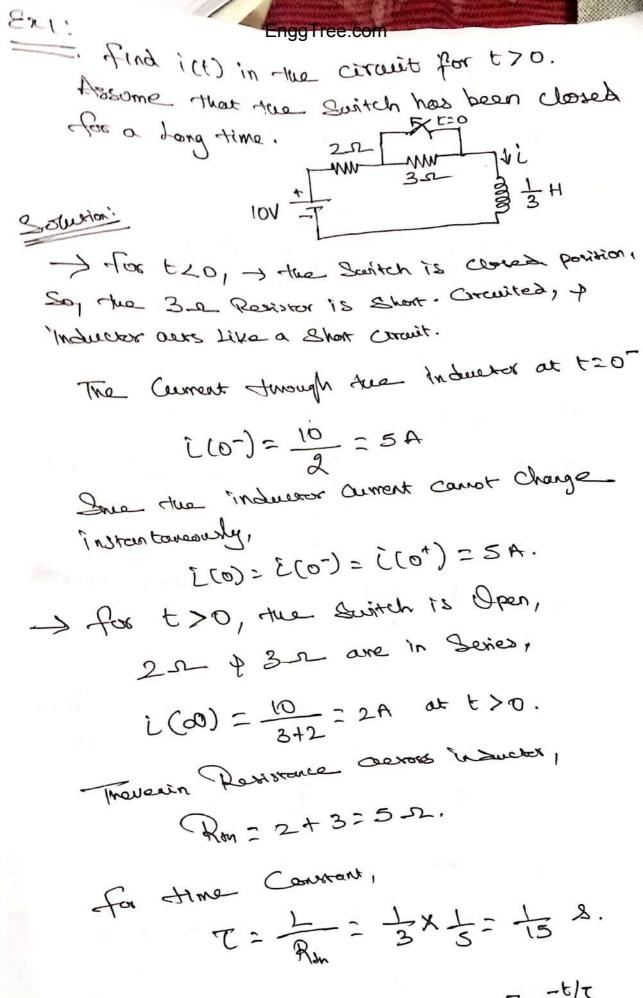
To Obrain L,

i -> Som of armer through 20-12 and Capacita.

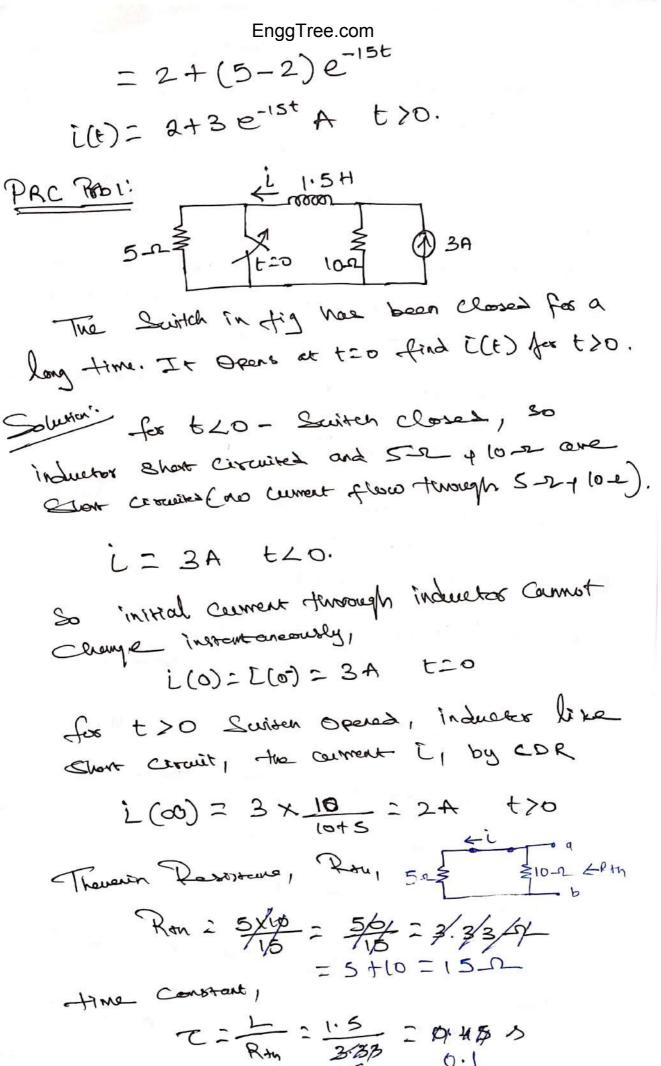


We now determine the constant of from the value of it. Let Jo be initial current, The Current through the inductor count Change instantaneously, i(o+)=i(o-)=Io -5 Thus are tio, Juan Equation (11) To = A + Us then, A= Io- 1/2 Sobribuny A' in equation (12) L(t) = 1/2 + [70-1/5] e-t/2 This is the Completes response of the RL circuit. The Desponse in equation (3) may be Written as, L(O) -> initial value L(00) - final Value

To find the EnggTree.com porse of an RL Circuit requires three things, 1. The initial inductor current i(0) as too 2. final inductor Current i (00).) t>0 3. The time constant T. If Suitching taxos place at time tito Instead of t=0, equation becomes, i(t)= i(∞)+[i(to)-i(ω]e-(t-to)/τ If Io=0, then $L(t) = \begin{cases} 0, & t < 0 \\ \frac{V_s}{R} C_1 - e^{-t/\tau}, & t > 0 \end{cases}$:. [(t)= Vs (1-e-t/z) u(t) This is the Step Response of the RL Circuit alim no initial inductor cument. The Voltage aerose the inductor is Obtained by, U(e) = L di = Vs L et/T where T= = : U(t)= Vs e-t/2 u(t) Downloaded from EnggTree.com

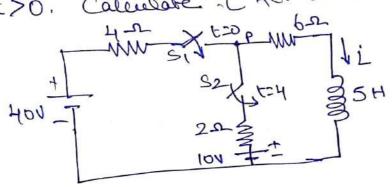


Thus; i(E) = i(a) + [i(a) - i(a)] e-t/t



EnggTree.com $i(t) = i(\infty) + i(\infty) - i(\infty) = -t/2$ = 2+ [3-2] e-t/0.14 L(E) = (2+e-10E) A, t>0.

Erz: At t=0, Switch 1 in fig is closed, and Switch 2 is closed 49 lacer, find i(E) for t>0. Calculate i for t=2s and t=55



Solution! Need to Consider Aure time Internals, t20, 02tc4, t>4 Separarely.

> fex t 20 > Switches S14 S2 come Open, 80

>> for 0 2 + 2478, 12 closed So 4-9-4

for 02 core in Series.

Garage in Series.

$$i(a) = \frac{40}{446} = \frac{4}{4}$$

RAM = 4+6=10-52

EnggTree.com 2(10) = E(00) + [1(0) - E(0)] = E/E (1)=4+(0-4)e=2+=4(1-e-2+)A OLTCH -> for t>4,52 is closed, lovar Source is commented. The Gosden Change doses not affect the industrie Current become the Connet Count Change abriphy. The initial Current is, 2(4)= i(4)= 4(1-e-5)~ 4A To find i (a), Let I be tea Wage at node P in bi), Using KCL, 40-1 + 10-1 = 1 42-4-12-6 10+5-1-4-4=0 - リ[エ+シャン]=-15 => リニ16.3636 1. L(0)=2.727A Therein resistance at maucres teminal,

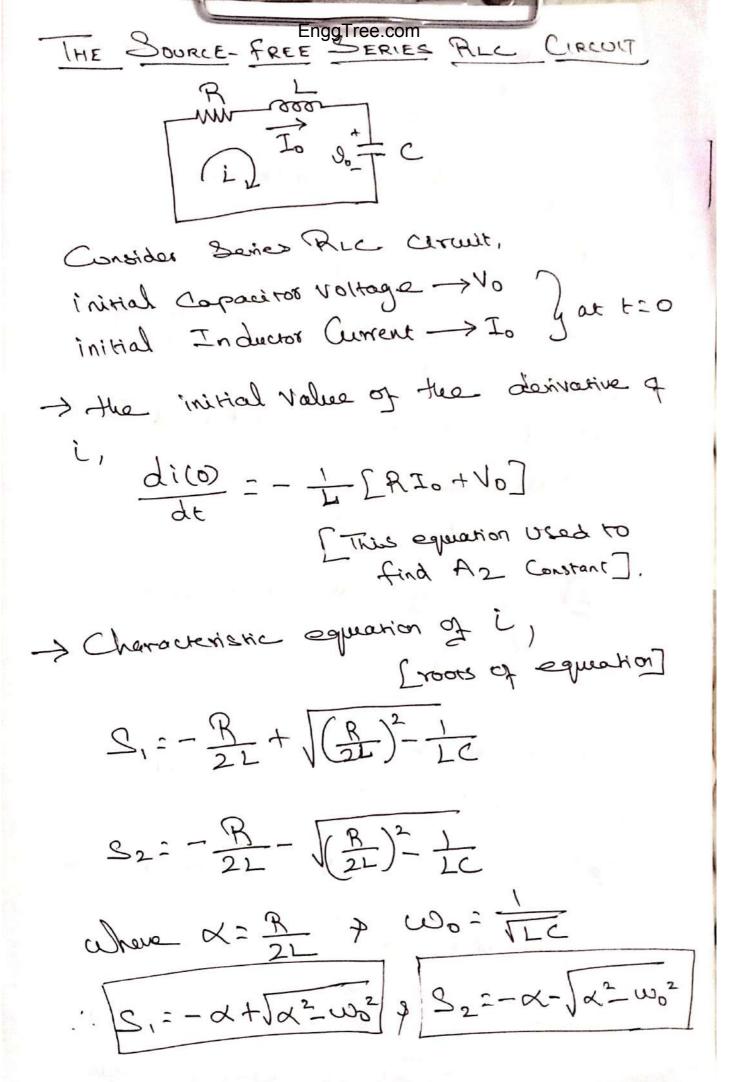
 $R_{m} = \left(\frac{4}{2}\right) + b = \frac{4x^{2}}{6} + b = \frac{22}{3} \cdot \Omega$ Downloaded from EnggTree.com

EnggTree.com
$$C = \frac{15}{RH} = \frac{15}{22/3} = \frac{15}{22}$$

$$\frac{15}{RH} = \frac{15}{22}$$

$$\frac{15}{22/3} = \frac{15}{22}$$

$$\frac{15}{22/3}$$



Thus, Natural response of the Series RLO
Circuit 1s, L(t) = A, es,t + A2 eszt
A, find by initial value ((0)
Az find by dico)
Based of S, 452 there are thee
types of Salutions
(1) If $\alpha > \omega_0 \rightarrow Overdamped Case$
Response 15, $L(t) = A_1 e^{S_1 t} + A_2 e^{S_2 t}$
2) Critically Damped Rosponse
$\frac{\alpha = \omega_0}{S_1 = S_2 = -\alpha = -\frac{R}{2L}}$
Response 181
c(t) = (A2+A,t)e
(3) X < Wo Under damped Case
$S_1 = - \alpha + \sqrt{-(\omega_0^2 - \alpha^2)} = - \alpha + j\omega_d$
$S_2 = -\alpha - \sqrt{-(\omega_0^2 - \alpha^2)} = -\alpha - \omega_0$

Wa = pownioaded from EnggTree.com ing frequency.

Wo -> Undompetree.comequeaux

() (t) = e at (B, coswat +B2 Sinwat)

time Contact -> 1/2 Period -> T = 211/Wd

Example Problem 1:

find i(E) in the Carouit. Assume that the Circuit has reached Steady State at t=07.

(W -T 0.02F T- 32 30.5H

Solution: for t20 -> Switch is closed. The Capacitor behaves like Open Circuit, 4 Inductor outs like Short Circuit, they tue equivalent coronit is,

10八十 第二个

Thiral

Though Inductor

Though Inductor

The property of the

((0) -> Convert though inductor U(0) -> Voltage across Capacità. * for t>0, -> Switch Opered, equilate 6-2- 43-5 am M Circult 19, Sevies. 0.024 Tio \$ 90.5H Source free PLC Cércuit Poots one Coloubare 2 as, $\alpha = \frac{R}{21} = \frac{9}{2 \times 0.5} = 9$ Wo= 120 = 10 S1, 2 = - x + J x = Woc $=-9\pm \sqrt{9^2-10^2}=-9\pm \sqrt{81-100}$ S1,2=-9±j4,359 [S12=-01=10] X < Wo -> Underdamped ilt)= e-at (10, coswat + 102 Sinwat) L(t) = e-9t (A, cors 4.359t + A2 Sin 4.359t)

A, y Az findinggrupe comitial conductions. VE FOO' i(0)=1=A, then Az ford by, $0 \rightarrow \frac{di}{dt} = -\frac{1}{2} \left[R(\omega) + U(\omega) \right]$ =-2[9-6] = -6A/s (10)=10=-6 -> become of Opposite direction of capaciter voltage > 6-2 resister voltage.] Now, Larrabe (CE) 2) -> di = - 9e at (A, cos 4,359t + 1/2 Sm + e-9+ (4,359) [-A, Sin 4,359+ +A2 Cos 4,359+) Imposing the two equations, (1) 4(2) at tio -6=-9[A1+0]+4.359[0+A2] -6=-9[]+4.359[A2] Az= -6+9 - -3 = -0.6862 Sub on values A, y Az in i(F) Downloaded from EnggTree.com

Complete 8000001.

Line to grade and y fact in the con-

EnggTree.com

In the parameter Cef and V(t) is for the assuming V(0) = 5V, U(0) = 0, L = 14 & $C = 10m_F$ bushles there (ales: $R = 1.923 \, a$, R = 5a, $R = 6.27 \, a$

Sin atub

2 the corresponding response is

Mikal Unlinhun loget Ale Az

$$\frac{dV(6)}{dr} = -V(0) + Ri(0) = -540$$
RC
$$1423 \times 10\times 10^{-3} = -260$$

By different herhay

Atto

EnggTree.com

Subs 412 MZ

ajez R-500

$$x = \frac{1}{2RC} = \frac{1}{2x5x10x10^{-3}} = 10$$

while wo = to remains the Same.

to yet A12A2

$$\frac{dV(0)}{dt} = -\frac{V(0) + Ra(0)}{RC} = -\frac{5+0}{5 \times 10 \times 10^{-3}} = -\frac{100}{5}$$

Byet diff.

$$A_1 = 5$$

 $A_2 = -50$ $V(x) = (5-50t)e^{-10t}V$

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We response is underlarged. The woors of the chandwells on

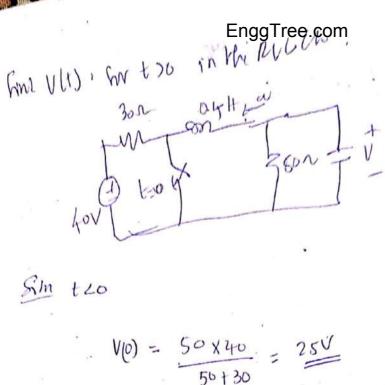
he obtain 918AZ

$$\frac{dV(0)}{dt} = -V(0) + Ru(0) = -5+0$$

$$RC \qquad 625 \times 10 \times 10^{3} = -80$$

But differenti sur

At +=01



$$V(0) = \frac{50 \times 40}{50 + 30} = \frac{250}{50}$$

50 Switch is closel, 30.2 & vige are begen.

$$51,2 = -\alpha \pm \sqrt{\alpha^2 - \omega_0^2}$$

= $-500 \pm \sqrt{250000 - 124,997-6} = -500 \pm 354$

EnggTree.com

Since of two. We have durdunge / refin

At 1:0

Turing the durante of v(E)

Example 13.3

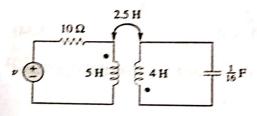


Figure 13.16 For Example 13.3. Consider the circuit in Fig. 13.16. Determine the coupling coeff. cient. Calculate the energy stored in the coupled inductors at ime $t = 1 \text{ s if } v = 60 \cos(4t + 30^\circ) \text{ V}.$

Solution:

The coupling coefficient is

$$k = \frac{M}{\sqrt{L_1 L_2}} = \frac{2.5}{\sqrt{20}} = 0.56$$

indicating that the inductors are tightly coupled. To find the energy stored, we need to calculate the current To find the current, we need to obtain the frequency-domain equivalent of the circuit.

$$60 \cos(4t + 30^{\circ}) \Rightarrow 60/30^{\circ}, \quad \omega = 4 \text{ rad/s}$$

$$5 \text{ H} \Rightarrow j\omega L_1 = j20 \Omega$$

$$2.5 \text{ H} \Rightarrow j\omega M = j10 \Omega$$

$$4 \text{ H} \Rightarrow j\omega L_2 = j16 \Omega$$

$$\frac{1}{16} \text{ F} \Rightarrow \frac{1}{j\omega C} = -j4 \Omega$$
ivalent is shown in Fig. 12 to

The frequency-domain equivalent is shown in Fig. 13.17. We now apply mesh analysis. For mesh 1,

For mesh 2,

$$(10 + j20)\mathbf{I}_1 + j10\mathbf{I}_2 = 60/30^{\circ}$$
 (13.31)

or

$$j10\mathbf{I}_1 + (j16 - j4)\mathbf{I}_2 = 0$$

$$I_1 = -1.2I_2 \tag{13.32}$$

Substituting this into Eq. (13.3.1) yields
$$I_2(-12 - j14) =$$

$$I_2(-12 - j14) = 60/30^{\circ}$$
 \Rightarrow $I_2 = 3.254/160.6^{\circ}$ A

and l

$$I_1 = -1.2I_2 = 3.905 / -19.4^{\circ} A$$

In the time-domain,

$$i_1 = 3.905 \cos(4t - 19.4^\circ), \quad i_2 = 3.254 \cos(4t + 160.6^\circ)$$

At time t = 1 s, 4t = 4 rad = 229.2°, and

$$i_1 = 3.905 \cos(229.2^{\circ} - 19.4^{\circ}) = -3.389 \text{ A}$$

$$i_2 = 3.254 \cos(229.2^{\circ} + 160.6^{\circ}) = 2.824 \text{ A}$$

The total energy stored in the coupled inductors is

$$w = \frac{1}{2}L_1i_1^2 + \frac{1}{2}L_2i_2^2 + Mi_1i_2$$

= $\frac{1}{2}(5)(-3.389)^2 + \frac{1}{2}(4)(2.824)^2 + 2.5(-3.389)(2.824) = 20.73 J$

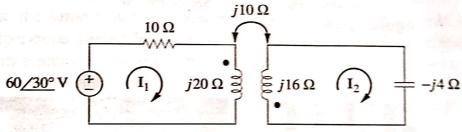


Figure 13.17

Frequency-domain equivalent of the circuit in Fig. 13.16.

Practice Problem 13.3

For the circuit in Fig. 13.18, determine the coupling coefficient and the energy stored in the coupled inductors at t = 1.5 s.

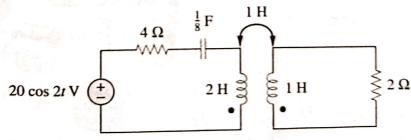


Figure 13.18

For Practice Prob. 13.3.

Answer: 0.7071, 9.85 J.

Example 13.7

An ideal transformer is rated at 2400/120 V, 9.6 kVA, and has 50 turns on the secondary side. Calculate (b) the number of turns on the primary side, and (c) the current ratings for the recordary side. An ideal transformer is rated at 2400/120 v, 9.0 kvc, and ideal transformer is rated at 2400/120 v, 9.0 kvc, and (c) the current ratings for the primary side, and (c) the current ratings for the primary side.

(a) This is a step-down transformer, since $V_1 = 2,400 \text{ V} > V_2 = 120 \text{ V}$.

$$n = \frac{V_2}{V_1} = \frac{120}{2,400} = 0.05$$

(b)

$$n = \frac{N_2}{N_1} \implies 0.05 = \frac{50}{N_1}$$

$$N_1 = \frac{50}{0.05} = 1,000 \text{ turns}$$

(c) $S = V_1 I_1 = V_2 I_2 = 9.6 \text{ kVA}$. Hence,

$$I_1 = \frac{9,600}{V_1} = \frac{9,600}{2,400} = 4 \text{ A}$$

$$I_2 = \frac{9,600}{V_2} = \frac{9,600}{120} = 80 \text{ A} \quad \text{or} \quad I_2 = \frac{I_1}{n} = \frac{4}{0.05} = 80 \text{ A}$$

Practice Problem 13.7

The primary current to an ideal transformer rated at 3300/110 V is 3 A. Calculate: (a) the turns ratio. (b) iz kVA rating, (c) the secondary current.

Answer: (a) 1/30, (b) 9.9 kVA, (c) 90 A.

Example 13.8, and approximate survey from one For the ideal transformer circuit of Fig. 13.37, find: (a) the source current I₁, (b) the output voltage V. and (c) the complex power supplied by the source.

Figure 13.37 For Example 13.8,

Solution:

(a) The 20- Ω impedance can be reflected to the primary side and we get

$$\mathbf{Z}_{R} = \frac{20}{n^2} = \frac{20}{4} = 5 \,\Omega$$

Thu

(b)

(c)

Calc

Solu Refle

betw

Ideal Transformers

Thus,

$$\mathbf{Z}_{\text{in}} = 4 - j6 + \mathbf{Z}_{R} = 9 - j6 = 10.82 / -33.69^{\circ} \Omega$$

$$\mathbf{I}_{1} = \frac{120/0^{\circ}}{\mathbf{Z}_{\text{in}}} = \frac{120/0^{\circ}}{10.82 / -33.69^{\circ}} = 11.09 / 33.69^{\circ} \Lambda$$
and \mathbf{I}_{2} leave the dotted terminals,

(b) Since both I1 and I2 leave the dotted terminals

$$I_2 = -\frac{1}{n}I_1 = -5.545/33.69^{\circ} \text{ A}$$
 $V_o = 20I_2 = 110.9/213.69^{\circ} \text{ V}$

(c) The complex power supplied is

$$\mathbf{S} = \mathbf{V}_s \mathbf{I}_1^* = (120 \underline{/0^\circ})(11.09 \underline{/-33.69^\circ}) = 1,330.8 \underline{/-33.69^\circ} \text{ VA}$$

Practice Problem 13.8

In the ideal transformer circuit of Fig. 13.38, find V_o and the complex power supplied by the source.

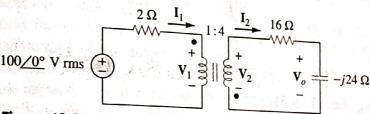


Figure 13.38

For Practice Prob. 13.8.

Answer: 178.9/116.56° V, 2,981.5/-26.56° VA

Example 13.9

Calculate the power supplied to the $10-\Omega$ resistor in the ideal transformer circuit of Fig. 13.39.

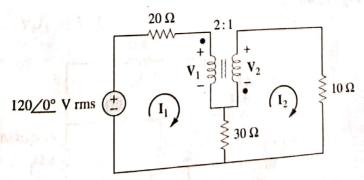


Figure 13.39

For Example 13.9. Perfection to the secondary or primary side cannot be done with this circuit: there is direct connection to the secondary or primary side cannot be done with this circuit: there is direct connection to the secondary or primary side cannot be done with this circuit: there is direct connection to the secondary or primary side cannot be done with this circuit: there is direct connection to the secondary or primary side cannot be done with this circuit: there is direct connection to the secondary or primary side cannot be done with this circuit: there is direct connection to the secondary or primary side cannot be done with this circuit: there is direct connection to the secondary or primary side cannot be done with this circuit: there is direct connection to the secondary or primary side cannot be done with this circuit: there is direct connection to the secondary or primary side cannot be done with this circuit: there is direct connection to the secondary or primary side cannot be done with this circuit: there is direct connection to the secondary or primary side cannot be done with this circuit: there is direct connection to the secondary or primary side cannot be done with the secondary or primary side cannot be done with the secondary or primary side cannot be done with the secondary or primary side cannot be done with the secondary or primary side cannot be done with the secondary or primary side cannot be done with the secondary or primary side cannot be done with the secondary or primary side cannot be done with the secondary or primary side cannot be done with the secondary or primary side cannot be done with the secondary or primary side cannot be done with the secondary or primary side cannot be done with the secondary or primary side cannot be done with the secondary or primary side cannot be done with the secondary or primary side cannot be done with the secondary or primary side cannot be done with the secondary or primary side cannot be done with the secondary or primary side cannot be done with the baween the primary and secondary sides due to the 30-Ω resistor. We apply mesh analysis. For mesh 1,

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$$-120 + (20 + 30)\mathbf{I}_1 - 30\mathbf{I}_2 + \mathbf{V}_1 = 0$$

or

$$50\mathbf{I}_1 - 30\mathbf{I}_2 + \mathbf{V}_1 = 120$$

For mesh 2,

$$-\mathbf{V}_2 + (10 + 30)\mathbf{I}_2 - 30\mathbf{I}_1 = 0$$

or

$$-30\mathbf{I}_1 + 40\mathbf{I}_2 - \mathbf{V}_2 = 0$$

At the transformer terminals,

(13.9.1)

(13.92)

$$\mathbf{I_2} = -2\mathbf{I_1} \tag{13.9}$$

(Note that n = 1/2.) We now have four equations and four unknowns, but our goal is to get I_2 . So substitute for V_1 and I_1 in terms of V_2 and I_2 in Eqs. (13.9.1) and (13.9.2). Equation (13.9.1) becomes

$$-55\mathbf{I}_2 - 2\mathbf{V}_2 = 120 \tag{1395}$$

V. 2081.5/+26.56 VA

Vi Johnson 12. E. Centrale and the

and Eq. (13.9.2) becomes

$$15\mathbf{I}_2 + 40\mathbf{I}_2 - \mathbf{V}_2 = 0 \quad \Rightarrow \quad \mathbf{V}_2 = 55\mathbf{I}_2$$

Substituting Eq. (13.9.6) in Eq. (13.9.5),

$$-165I_2 = 120$$
 \Rightarrow $I_2 = -\frac{120}{165} = -0.7272 \text{ A}$

The power absorbed by the $10-\Omega$ resistor is

$$P = (-0.7272)^2(10) = 5.3 \text{ W}$$

Practice Problem 13.9

Find V_o in the circuit of Fig. 13.40.

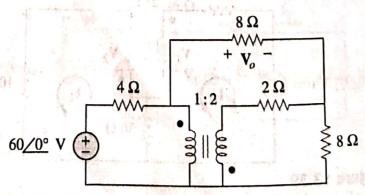


Figure 13.40

For Practice Prob. 13.9.

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Example 13.4

In the circuit of Fig. 13.24, calculate the input impedance and current I_1 . Take $Z_1 = 60 - j100 \Omega$, $Z_2 = 30 + j40 \Omega$, and $Z_L = 80 + j60 \Omega$.

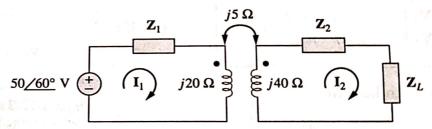


Figure 13.24 For Example 13.4.

Solution:

From Eq. (13.41),

$$\mathbf{Z}_{in} = \mathbf{Z}_1 + j20 + \frac{(5)^2}{j40 + \mathbf{Z}_2 + \mathbf{Z}_L}$$

$$= 60 - j100 + j20 + \frac{25}{110 + j140}$$

$$= 60 - j80 + 0.14 / -51.84^{\circ}$$

$$= 60.09 - j80.11 = 100.14 / -53.1^{\circ} \Omega$$

ves

47)

18)

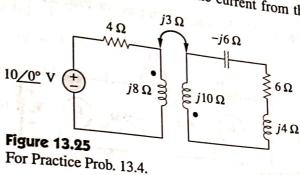
ng ga-

 Ω

Find the input impedance of the circuit in Fig. 13.25 and the current from the voltage source.

 $I_1 = \frac{V}{Z_{in}} = \frac{50/60^{\circ}}{100.14/-53.1^{\circ}} = 0.5/113.1^{\circ} A$

Practice Problem 13.4



Answer: $8.58/58.05^{\circ}$ Ω , $1.165/-58.05^{\circ}$ A.

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Example 13.5

Determine the T-equivalent circuit of the linear transformer in Fig. 13.26(a).

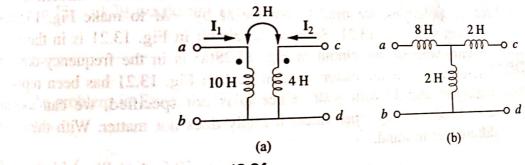


Figure 13.26

For Example 13.5: (a) a linear transformer, (b) its

II | - = M - = T-equivalent circuit.

Given that $L_1 = 10$, $L_2 = 4$, and M = 2, the T-equivalent network has the following parameters:

$$L_1 = 10$$
, $L_2 = 4$, and $M = 2$, the requirement $L_a = L_1 - M = 10 - 2 = 8 \text{ H}$

$$L_a = L_1 - M = 10 - 2 = 8 \text{ H}$$

$$L_b = L_2 - M = 4 - 2 = 2 \text{ H}, \quad L_c = M = 2 \text{ H}$$

$$L_b = L_2 - M = 4 - 2 = 2 \text{ H}, \quad L_c = M = 2 \text{ H}$$

The T-equivalent circuit is shown in Fig. 13.26(b). We have assumed that reference directions for currents and voltage polarical voltage polarical response conform to those in Fig. 13.21. Otherwise, we and voltage polarities in the primary and secondary windings conform to those in Fig. 13.21. Otherwise, we may need to replace the primary and secondary windings conform to those in Fig. 13.21. may need to replace M with -M, as Example 13.6 illustrates.

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Practice Problem 13.5

For the linear transformer in Fig. 13.26(a), find the Π equivalent network.

Answer: $L_A = 18 \text{ H}, L_B = 4.5 \text{ H}, L_C = 18 \text{ H}.$

Example 13.6 salay and arreal pressure and bein &

Solve for I₁, I₂, and V_o in Fig. 13.27 (the same circuit as for Practice Prob. 13.1) using the T-equivalent

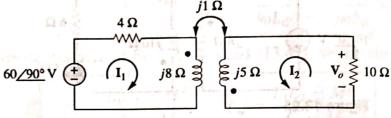


Figure 13.27 For Example 13.6.

Solution:

Notice that the circuit in Fig. 13.27 is the same as that in Fig. 13.10 except that the reference direction for current I₂ has been reversed, just to make the reference directions for the currents for the magnetically coupled coils conform with those in Fig. 13.21.

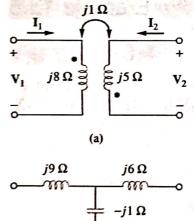


Figure 13.28

For Example 13.6: (a) circuit for coupled coils of Fig. 13.27, (b) T-equivalent circuit.

We need to replace the magnetically coupled coils with the T-equivalent circuit. The relevant portion of the circuit in Fig. 13.27 is shown in Fig. 13.28(a). Comparing Fig. 13.28(a) with Fig. 13.21 shows that there are two differences. First, due to the current reference directions and voltage polarities, we need to replace M by -M to make Fig. 13.280 conform with Fig. 13.21. Second, the circuit in Fig. 13.21 is in the time domain, whereas the circuit in Fig. 13.28(a) is in the frequency-domain The difference is the factor $j\omega$; that is, L in Fig. 13.21 has been replaced with $j\omega L$ and M with $j\omega M$. Since ω is not specified, we can assume $\omega = 1$ rad/s or any other value; it really does not matter. With these two differences in mind.

$$L_a = L_1 - (-M) = 8 + 1 = 9 \text{ H}$$

 $L_b = L_2 - (-M) = 5 + 1 = 6 \text{ H}, \quad L_c = -M = -1 \text{ H}$

Thus, the T-equivalent circuit for the coupled coils is as shown Fig. 13.28(b).

Inserting the T-equivalent circuit in Fig. 13.28(b) to replace the two coils in Fig. 13.27 gives the equivalent in Fig. 13.29 which can be colved as in Fig. 13 circuit in Fig. 13.29, which can be solved using nodal or mesh analysis. Applying mesh analysis, we obtain 13.61 (13.6.1)

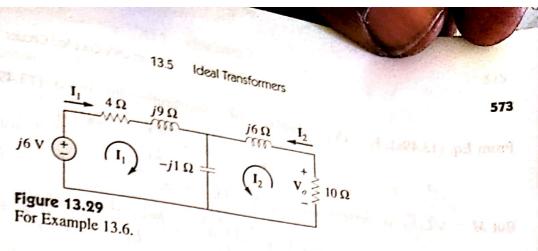
$$i = I_1(4 + j9 - j1) + I_2(-j1)$$

and

The
$$j=0$$
 to the second of $j=0$ to the second $j=0$ to the secon

From Eq. (13.6.2),

$$I_1 = \frac{(10+j5)}{j}I_2 = (5-j10)I_2$$



Substituting Eq. (13.6.3) into Eq. (13.6.1) gives

$$j6 = (4 + j8)(5 - j10)I_2 - jI_2 = (100 - j)I_2 \approx 100I_2$$

ge compared with 1, the imaginary

Since 100 is very large compared with 1, the imaginary part of (100 - j) can be ignored so that

$$I_2 = \frac{j6}{100} = j0.06 = 0.06/90^{\circ} \text{ A}$$

From Eq. (13.6.3),

$$I_1 = (5 - j10)j0.06 = 0.6 + j0.3 \text{ A}$$

and

$$V_o = -10I_2 = -j0.6 = 0.6/-90^{\circ} V$$

This agrees with the answer to Practice Prob. 13.1. Of course, the direction of I₂ in Fig. 13.10 is opposite to that in Fig. 13.27. This will not affect V_o , but the value of I_2 in this example is the negative of that of I₂ in Practice Prob. 13.1. The advantage of using the T-equivalent model for the magnetically coupled coils is that in Fig. 13.29 we do not need to bother with the dot on the coupled coils.

Practice Problem 13.6

Solve the problem in Example 13.1 (see Fig. 13.9) using the T-equivalent model for the magnetically coupled coils.

Answer: $13/-49.4^{\circ}$ A, $2.91/14.04^{\circ}$ A.