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Reg. No.:			

## Question Paper Code: 41520

B.E./B.Tech. DEGREE EXAMINATIONS, JANUARY 2022.

First Semester

Civil Engineering

## MA 3151 — MATRICES AND CALCULUS

(Common to All Branches (Except: Marine Engineering)

(Regulations 2021)

Time: Three hours

Maximum: 100 marks

Answer ALL questions.

PART A — 
$$(10 \times 2 = 20 \text{ marks})$$

- 1. If 2, -1, -3 are the eigenvalues of a matrix "A", then find the eigenvalues of the matrix  $A^2-2I$ .
- 2. Write down the matrix for the following quadratic form:

$$2x_1^2 - 2x_2^2 + 4x_3^2 + 2x_1x_2 - 6x_1x_3 + 6x_2x_3$$

- 3. Find the domain of the function  $f(x) = \frac{2x^3 5}{x^2 + x 6}$
- 4. Evaluate the limit  $\lim_{x\to 1} \frac{x^2-4x}{x^2-3x-4}$ .
- 5. If  $u = x^3 + y^3$  where  $x = a \cos t$  and  $y = b \sin t$  then find  $\frac{du}{dt}$ .
- 6. If  $u = \frac{2x y}{2}$  and  $v = \frac{y}{z}$  then find  $\frac{\partial(u, v)}{\partial(x, y)}$ .
- 7. Given that  $\int_0^{10} f(x) dx = 17$  and  $\int_0^8 f(x) dx = 12$  then find  $\int_8^{10} f(x) dx$ .

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- 8. Determine whether the integral  $\int_0^\infty \frac{dx}{x^2+4}$  is convergent or divergent.
- 9. Evaluate  $\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \int_{0}^{2\cos\theta} d\theta \ dr$ .
- 10. Evaluate  $\int_0^1 \int_0^2 \int_0^3 [x \ y^2 z] dx dy dz$ .

PART B 
$$-$$
 (5 × 16 = 80 marks)

- 11. (a) (i) Find the eigenvalues and eigenvectors of the matrix  $A = \begin{bmatrix} 2 & 2 & 0 \\ 2 & 1 & 1 \\ -7 & 2 & -3 \end{bmatrix}.$  (8)
  - (ii) Using Cayley Hamilton theorem find the inverse of the matrix  $A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 5 \\ 3 & 5 & 6 \end{bmatrix}.$  (8)

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- (b) Reduce the quadratic form  $3x_1^2 + 3x_2^2 + 3x_3^2 + 2x_1 x_2 + 2x_1 x_3 2x_2 x_3$  to canonical form through an orthogonal transformation. Also find its nature, rank, index and signature. (16)
- 12. (a) (i) If  $x^2 + y^2 = 25$ , then find  $\frac{dy}{dx}$  and also find an equation of the tangent line to the curve  $x^2 + y^2 = 25$  at the point (3,4). (8)
  - (ii) If  $f(x) = xe^x$  then find f'(x). Also find the n-th derivative f''(x). (8)

Or

- (b) (i) Differentiate the function  $f(x) = \frac{\sec x}{1 + \tan x}$ . For what values of x, the graph of f(x) has a horizontal tangent? (8)
  - (ii) Find the absolute maximum and absolute minimum values of the function  $f(x) = 3x^4 4x^3 12x^2 + 1$  on the interval [-2, 3]. (8)

- 13. (a) (i) If  $u = \log \left[ \tan x + \tan y + \tan z \right]$  then find the value of  $\sin 2x \frac{\partial u}{\partial x} + \sin 2y \frac{\partial u}{\partial y} + \sin 2z \frac{\partial u}{\partial z}$ . (8)
  - (ii) Find the minimum value of  $f(x, y) = x^2 + y^2 + 6x + 12$ . (8)

Or

- (b) (i) Expand  $f(x, y) = e^x \sin y$  in terms of powers of "x" and "y" up to third degree terms by using Taylor's series.
  - (ii) Show that the rectangular solid of maximum volume that can be inscribed in a sphere is a cube.

    (8)
- 14. (a) (i) Evaluate  $\int \cos^n x \, dx$  by using integration by parts. (8)
  - (ii) Evaluate  $\int \frac{dx}{\sqrt{3x-x^2-2}}$ . (8)

Or

- (b) (i) Evaluate  $\int \frac{x^2 + 2x 1}{2x^3 + 3x^2 2x} dx$  by using the method of partial fractions. (8)
  - (ii) Evaluate  $\int \frac{2x+3}{x^2+x+1} dx$ . (8)
- 15. (a) (i) Evaluate  $\iint [x \ y] \ dx \ dy$  where the region of integration is bounded by the lines x-axis, x=2a and the curve  $x^2=4ay$ . (8)
  - (ii) Change the order of the integration in  $\int_0^{4a} \int_{\frac{x^2}{4a}}^{2\sqrt{ax}} [x y] dy dx$  and hence evaluate it. (8)

Or

- (b) (i) Evaluate  $\int_0^a \int_y^a \left[ \frac{x}{x^2 + y^2} \right] dx dy$  by changing into polar coordinates.
  - (ii) Evaluate  $\int_0^{2a} \int_0^x \int_y^x [x \ y \ z] \ dz \ dy \ dx.$  (8)